

1 **Mechanical challenges to freshwater residency in sharks**
2 **and rays**

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19 **Running head: Mechanical challenges to freshwater residency**

50 **Summary**

51 Major transitions between marine and freshwater habitats are relatively infrequent, primarily
52 as a result of major physiological and ecological challenges. Few species of cartilaginous fish
53 have evolved to occupy freshwater habitats. Current thought suggests that the metabolic
54 physiology of sharks has remained a barrier to the diversification of this taxon in freshwater
55 ecosystems. Here we demonstrate that the physical properties of freshwater provide an
56 additional constraint for this specious group to occupy freshwater systems. Using
57 hydromechanical modelling, we show that occurrence in freshwater results in two- to three-
58 fold increase in negative buoyancy for sharks and rays. This carries the energetic cost of lift
59 production and results in buoyancy dependant mechanical power requirements of swimming
60 and increase optimal swim speeds. The primary source of buoyancy, the lipid-rich liver,
61 offers only limited compensation for increased negative buoyancy as a result of decreasing
62 water density; maintaining the same submerged weight would involve increasing the liver
63 volume by very large amounts, namely, 3 to 4 fold in scenarios where liver density is also
64 reduced to currently observed minimal levels, and 8 fold without any changes in liver density.
65 The first data on body density from two species of elasmobranch occurring in freshwater
66 (bull shark *Carcharhinus leucas* and largetooth sawfish *Pristis pristis*) support this
67 hypothesis, showing similar liver sizes as marine forms but lower liver densities, but the
68 greatest negative buoyancies of any elasmobranch studied to date. Our data suggests that
69 mechanical challenges associated with buoyancy control may have hampered the invasion of
70 freshwater habitats in elasmobranchs, highlighting an additional key factor that may govern
71 the predisposition of marine organism to successfully establish in freshwater habitats.

72

73 **Keywords:** Buoyancy, liver, tissue density, locomotion, lift, drag

74

75 **Introduction**

76 A wide range of physiological, ecological, and evolutionary processes determine the capacity
77 of animals to invade and adapt to novel environments. For major transitions, such as those
78 between aquatic and terrestrial or marine and fresh water environments, successful invasions
79 are relatively infrequent in most plant and animal taxa except for tetrapods (Vermeij and
80 Dudley, 2000). However, transitions from saltwater to freshwater habitats can facilitate
81 radiation and speciation events, which in some systems manifest as rapid and repeated
82 invasions worldwide (Lee and Bell, 1999). The Chondrichthyes have proven relatively
83 unsuccessful at invading freshwater habitats despite their worldwide distribution in marine
84 ecosystems. Of the >1000 species of the Elasmobranchii, only approximately 5% are thought
85 to reside in freshwater (Ballantyne and Fraser, 2013; Martin, 2005). Moreover, most of these
86 species only utilise freshwater habitats for part of their lifecycle. Explaining the mechanism
87 behind this stark pattern in biogeography has received significant attention in the literature
88 for the last half century (e.g. Ballantyne and Robinson, 2010; Ballantyne and Fraser, 2013;
89 Pillans and Franklin, 2004; Thorson, 1962).

90
91 Current hypotheses suggest that metabolic organisation of elasmobranchs is responsible for
92 their poor penetration into freshwater, resulting in metabolic costs associated with
93 osmoregulation (Ballantyne and Robinson, 2010; Meloni et al., 2002). Whereas the
94 difference in solute concentrations has a significant impact on the physiological biochemistry
95 of elasmobranchs, the potential impact of the changing density of seawater and freshwater
96 has not been adequately considered. Although the difference in density between seawater
97 (SW $\sim 1026 \text{ kg m}^{-3}$ at 20C°) and freshwater (FW $\sim 996 \text{ kg m}^{-3}$ at 20C°) may seem trivial, it
98 may nevertheless have significant ramifications for the buoyancy control of these animals.
99 Animal tissue is generally denser than both SW and FW, so that marine animals without any

100 organ providing buoyancy would be heavily negatively buoyant (Alexander, 1990;
101 Davenport, 1999; Pelster, 2009). Elasmobranchs utilise lipid-rich livers to increase the
102 buoyant force relative to their mass (commonly referred to as static lift) (Baldrige Jr, 1970;
103 Bone and Roberts, 1969; Corner et al., 1969). Due to the minor difference in density of liver
104 tissue ($900 - 1000 \text{ kg m}^{-3}$) to that of marine waters ($\sim 1027 \text{ kg m}^{-3}$), large livers are required to
105 provide necessary force to approach near neutral buoyancy. Indeed, neutrally buoyant sharks,
106 which are commonly found in the deep sea may have livers which comprise 30% of whole
107 body volume (Corner et al., 1969) compared to only 1-7% swim-bladder volume required to
108 provide neutral buoyancy in ray-finned fishes (Alexander, 1966; Davenport, 1999; Weitkamp,
109 2008).

110

111 Despite the use of the liver as a means to increase buoyancy, the majority of elasmobranch
112 species remain negatively buoyant (Baldrige Jr, 1970; Bone and Roberts, 1969; Gleiss et al.,
113 2011b). Counteracting this negative buoyancy represents one of the two major forces that
114 govern the energetics of locomotion in aquatic environments (Alexander, 1990; Alexander,
115 2003). In elasmobranchs, the heterocercal caudal fin and the pectoral fins and/or the body
116 generate vertical forces that balance this negative buoyancy (Fish and Shannahan, 2000;
117 Wilga and Lauder, 2002). This in turn results in drag due to lift by the body and pectoral fins
118 (known as induced drag, Alexander, 1990; Alexander, 2003) and the vortex jet of the
119 heterocercal caudal fin to have a vertical component (Wilga and Lauder, 2002) making
120 excessive negative buoyancy unfavourable. The use of a buoyancy organ, such as a large
121 lipid rich liver, reduces this cost, but increases parasite drag, due to greater surface area and
122 reduced streamlining (Alexander, 1990). Negative buoyancy is favourable for those animals
123 travelling fast while neutral buoyancy provided by large livers favours lower travel speeds, as
124 a result of decreasing costs of lift production at higher speeds (Alexander, 1990). For

125 instance, Greenland sharks (*Somniosus microcephalus*) have substantial liver sizes and are
126 close to neutral buoyancy cruise at speeds of only 0.1 lengths/s (Watanabe et al., 2012). In
127 contrast, sharks that are more negatively buoyant tend to travel at 0.2-0.7 lengths/s (Watanabe
128 et al., 2012).

129

130 The close relationship between the locomotor performance and body density may represent a
131 fundamental influence on the lifestyle of elasmobranchs (Bone and Roberts, 1969; Gleiss et
132 al., 2011a) and a key aspect to understanding how the constraints of water density and
133 buoyancy shape the lives of those species that occur in freshwater. However, this has
134 received no attention in the literature thus far (Ballantyne and Robinson, 2010). In this paper,
135 we aim to clarify the impacts of changing water density on the buoyancy and energetics of
136 elasmobranchs. We model the expected change in buoyancy by calculating the theoretical
137 buoyancies of marine species of shark occurring in freshwater. We then simulate the required
138 change in liver size and density to compensate for the decrease in environmental density and
139 calculate the energetic costs associated with different hypothetical scenarios of compensation.
140 In a second part of this work, we present the first measurements of buoyancy of two species
141 of elasmobranchs naturally occurring in freshwater and compare those to marine forms.

142

143 **Results**

144 *Modelling the Morphological Implications of Water Density*

145 Changes in water density drastically alter the submerged weight of an elasmobranch, in this
146 case our modelled bull shark (Fig. 1), as calculated by eq. 1 described in *Materials and*
147 *Method*. Submerged weight increases linearly with a decline of water density. A reduction of
148 liver density to the low values observed in deep-sea sharks (920 kg m^{-3}) can off-set this
149 increase to brackish waters of density of 1022 kg m^{-3} (Fig. 1). An additional mode of

150 compensating for the reduced environmental density is to change the size of the liver, with
151 larger livers providing more upthrust. Assuming no adjustments in liver density, liver volume
152 would have to increase 8-fold to maintain a similar submerged weight in freshwater as in
153 marine waters (Fig. 1), resulting in a liver comprising ~60% of whole body volume. In the
154 hypothetical scenario where a shark has the ability to reduce its liver density, liver volume
155 would only have to increase 3-fold, resulting in a liver comprising ~35% of body volume,
156 compared to 14% in marine waters to achieve the same submerged weight as in marine
157 waters. We have to note here that these calculations assume that all other tissues maintain the
158 same volume. This assumption is discussed below.

159 **Fig. 1**

160

161 *Modelling the Energetic Consequences of Salinity*

162 Negative buoyancy compensation via lift production by the body, pectoral fins and
163 heterocercal tail, and attendant metabolic costs, was carried out using a standard approach to
164 aircraft performance modelling - see eqns. 2 – 6a in *Materials and Methods* (Cole 1981, Pope
165 1951). Components of this model were validated with the shear stress drag data of smooth
166 dogfish (*Mustelus canis*) measured by Anderson et al (2001) (further discussed in the
167 Electronic Supplement). Swimming performance is assessed herein with the expended
168 metabolic power (P_{total}) and Cost of Transport (COT) incurred from (parasite) drag
169 production and from negative buoyancy compensation via lift (see eqns. 6a and 7). Herein
170 these metabolic costs are based on two representative swim speeds, namely, the so-called
171 *minimum speed* (u_{min}) used to minimize total drag (eqn. 5); and the optimal speed (u_{opt})
172 maximizing travel distance with a fixed energy store (Weihs, 1973). Teleosts and
173 elasmobranchs also travel over long distance in manners to reduce energy consumption. But
174 biological organisms incur metabolic costs at $u = 0$ (known as Standard Metabolic Rate)

175 resulting from the other energy intensive functions of the body; this cost demands that
176 metabolic efficiency is achieved at higher velocities than u_{min} – hence the larger u_{opt} .
177 Typically, sharks swim at average speeds in the range of 0.3 - 0.8m/s (Watanabe et al 2012) -
178 presumably near optimal speed – which amounts to twice (or less) the minimal speed (as
179 shown further here). Not surprisingly, both minimal and optimal speeds, and corresponding
180 metabolic costs, increase with larger negative buoyancies (see eqns. 6a and 6b). This trend
181 will be shown quantitatively here using u_{min} since it can be assessed with a minimum of
182 assumptions. Given that the calculation of u_{opt} involves several inputs characteristic of
183 metabolism, which predictably vary between species and encountered temperature, the
184 dependence of optimal speed and metabolic expenditures shall be shown algebraically rather
185 than numerically (see eqn. 6b below, and eqns. ES13-ES20 in the Electronic Supplement).
186 Note finally that other optimized swimming speed concepts have been proposed (e.g. Castro-
187 Santos, 2006; Videler and Nolet, 1990; Ware, 1978). Although optimizing different metrics,
188 most, if not all, should show similar trends with regards to adding more negative buoyancy,
189 due to the increasing mechanical cost associated with a given speed.

190

191 We simulated four hypothetical scenarios that could be a response to changing water
192 density; no compensation, increasing liver size, decreasing liver density and the two
193 combined. These four scenarios markedly differed in the parameters used in our modelling
194 exercise (Table 1) and resulted in an increase of negative buoyancy compared to marine
195 waters. The scenarios do not encompass all possible morphological adaptations, such as body
196 and fin profiles to improve lift (of which an evolution into a ray-like lifting body profile
197 would be one example). They aim instead at evaluating the effects of liver density and size
198 modifications separately from those leading specifically to lift enhancement. Although the
199 latter wasn't considered here, it should be clear from the modelling that, despite possible

200 reductions in parasitic drag, lift increase always come at a cost, either in extra induced drag
 201 and/or loss of turn rate performance in unsteady manoeuvring. All scenarios resulted in an
 202 increase of negative buoyancy compared to marine waters. We found a marked increase of
 203 the speed at which drag is minimised, primarily as a result of the increased negative
 204 buoyancy of those scenarios (Fig. 2).

205

206 An increase in liver size and a decreasing liver density resulted in the smallest increase of
 207 either cost of transport or metabolic power at minimum cost speed (u_{min}), but also resulted in
 208 less streamlining, with lower body depth over body length ratio (t/SL) and body wetted area
 209 both increased by 13% (Fig. 3). Our numerical work to solve u_{opt} also showed that optimal
 210 speed is dependent on buoyancy and mechanical power requirements increase with increasing
 211 negative buoyancy (see Methods and Electronic Supplement). Namely, both u_{opt} and P_{total}
 212 increase with negative buoyancy (W) as $u_{opt} \propto W^0$ & $u_{opt} \propto W^{1/2}$ at small and large negative
 213 buoyancy respectively, which, interestingly, compares with u_{min} as $u_{min} \propto W^{1/2}$ (eqn. 5); and
 214 $P_{total}^{opt} \propto W^2$ & $P_{total}^{opt} \propto W$ again at small and large W .

215

216 **Table 1**

217

218 **Fig. 2, 3**

219 *Densities of freshwater elasmobranchs*

220 All sawfish (n=17) and bull sharks (n= 5) captured in the Fitzroy River were negatively
 221 buoyant in the water they were captured in, with calculated body densities of $1065 \pm 5 \text{ kg m}^{-3}$
 222 for the bull sharks and $1065 \pm 3 \text{ kg m}^{-3}$ for the sawfish. The ratio of W_{sub} and weight in air
 223 W_{Air} ($\text{Mass} \times 9.81 \text{ m/s}^2$) was $6.44 \pm 0.39\%$ in bull sharks and $6.48 \pm 0.33\%$ in sawfish. For
 224 the individuals where liver size and density could be measured, the liver represented $6.21 \pm$

225 0.64 % of whole body mass in the sawfish (n=2) and 7.82 ± 1.73 % in the bull shark (n=3).
226 Liver density was 980 ± 2 kg m⁻³ in the sawfish and 920 ± 3 kg m⁻³ in the bull sharks (Table
227 3).

228

229 *Comparative Data*

230 Comparisons of the ratio between weight in air and submerged weight shows that the 22
231 individuals of the two species we studied show some of the greatest negative buoyancies (6.4
232 %), compared to the 113 individuals sampled in other studies in marine waters (3.95 ± 1.2 %,
233 see supplementary Table ES1). Our statistical model of mass and submerged weight supports
234 this, with the most parsimonious model indicating that habitat and mass are the strongest
235 predictors of submerged weight (Table 4, Fig. 4). The comparison of liver size scaling
236 between elasmobranchs sampled in marine waters from previous research and those sampled
237 in freshwater revealed that there was little difference in the size of livers, with the highest
238 ranked model only including logMass as an explanatory factor. Lifestyle did not appear to
239 affect liver size in our data-set; this however is a result of excluding deep-water sharks from
240 our analysis, which are known to have large livers (Bone and Roberts, 1969; Corner et al.,
241 1969). Liver density on the other hand is best predicted by the inclusion of lifestyle and
242 habitat. Pelagic sharks have livers of lesser density than those species that are generally
243 associated with the seabed. The five individuals for which livers could be sampled showed
244 liver densities that were below or near the lower 95th percentile of individuals of similar
245 lifestyle sampled in marine waters (Fig. 4). Density of lean tissue was not predicted well by
246 any of the covariates we tested the model for (Table 4).

247

248 **Table 4**

249 **Fig. 4**

250

251 **Discussion**

252 Our comparison of body composition of sharks sampled in marine waters and those in
253 freshwater suggest that liver size has not drastically increased to produce more upthrust and
254 compensate for the lower density of freshwater. Liver density on the other hand was
255 measured to be close to the lowest values observed in any species of shark, suggesting that
256 this may be a response to reduced water density. We emphasize, however, that these
257 conclusions do not stem from experimental data of how liver size and density responded to
258 changing salinity in a controlled experiment, but rather a large comparative analysis of liver
259 sizes and densities of a range of species. We can, however, safely say that no substantial
260 increase in liver size appears to have occurred in the individuals we studied. The same caveat
261 also applies to our assessment of liver density; however in this case, the liver densities were
262 lower than the 95th percentile of those studied to date, indicating that liver density may be
263 readily lowered. There is precedence for such a process in the literature – experimentally
264 weighted spiny dogfish (*Squalus acanthias*) increase their fraction of DAGE (a low density
265 lipid) in liver tissue (Malins and Barone, 1970). Although not explicitly quantified in their
266 study, greater amount of DAGE will increase the upthrust provided by the liver and
267 compensate for the increased negative buoyancy. No change in liver size was found in the
268 experimentally weighted spiny dogfish.

269

270 Our analysis makes one important assumption; we have assumed that all lean tissue is fixed
271 in its volume. A reduction in the volume of dense tissue (e.g. muscle, viscera, skeleton),
272 would reduce any increases in surface area and therefore the energetic consequences we
273 outline here. However, any reduction in the volume of these tissues must invariably decrease
274 some form of performance. For instance, a reduction of white muscle volume (the most

275 voluminous tissue in most fish) would be expected to lead to a proportional decline in burst
276 swimming performance. A simple example, for a shark to maintain similar hydrodynamic
277 characteristics (fineness ratio, buoyancy, wetted area, Table 1) the liver would have to occupy
278 ~45% of the whole fish, reducing lean tissue volume by >50% in freshwater. Assuming white
279 muscle comprises 70-40% of the animals volume (Bone, 1978; Greek-Walker and Pull,
280 1975), this would result in a 76 - 100% reduction in available white muscle for burst
281 swimming, with obvious deleterious effects to fitness (Ghalambor et al., 2003; Walker et al.,
282 2005). Even though it may be possible to maintain similar hydrodynamic properties,
283 compensation by reduction of volume of other tissue should have additional deleterious
284 effects.

285

286 *Optimal compensation – a paradox?*

287 Our field data indicate that the reduction of liver density is the prevalent mechanism by
288 which sharks achieve more upthrust. Yet our modelling approach suggests that in addition to
289 decreasing liver density, increasing liver size to 30% body volume (Scenario 4) provides a
290 more efficient alternative in our hypothetical shark (see Fig. 2), due to the reduced negative
291 buoyancy. However, increasing liver size will increase body fineness ratio (t/SL), and thus
292 wetted area (by ~13%), as well as parasitic drag force (by >25%, see eqn. 2, 3); but
293 interestingly it would also *decrease* u_{min} (by ~ 18%; see eqn. 5) and overall COT (Figure 2)
294 compared to the scenario lacking compensation. However, less streamlining by increased
295 liver volume would also degrade the performance of burst swimming as well as of foraging at
296 supra-optimal speeds [44] since, with $u > u_{min}$, the resulting drag force would become even
297 higher and to the point of *increasing* COT, perhaps at levels too high for the given fixed
298 amount of muscle power and energy available. In other words, combining lower liver

299 densities with larger liver volumes could only be advantageous in environments where the
300 prey is easy to find and catch (at u_{min}) and predation pressure is low.

301

302 An additional explanation for this discrepancy is the metabolic cost of growing and
303 maintaining such large livers. The low-density lipids contained in the liver responsible for
304 providing upthrust are energy dense. For instance, triacylglycerols, a class of lipid found in
305 shark livers (Wetherbee and Nichols, 2000), contains 38 kJ g^{-1} whereas muscle tissue
306 contains approximately $2\text{-}4 \text{ kJ g}^{-1}$. This may make a substantial difference for the juvenile
307 sharks studied here, which are in a period of rapid somatic growth. Indeed, Priede et al.
308 (2006) have suggested that the metabolic cost associated with large livers may be responsible
309 for the absence of sharks from the oligotrophic abyssal depths of the oceans. Moreover, liver
310 tissue has some of the fastest turnover time of any tissue in elasmobranchs (Hussey et al.,
311 2010), therefore increasing the cost of not only growing but also maintaining such tissue.
312 Although it may be argued that $\sim 30\%$ liver volume is encountered in deep-sea sharks and
313 some very large pelagics (e.g. basking, tiger or white sharks) and is therefore unlikely to
314 provide an overwhelming metabolic burden, the warm tropical waters occupied by our study
315 subjects already significantly increase standard metabolic rates (Carlson and Parsons, 1999).
316 The increasing metabolic cost of growing a large liver may therefore not be sustainable for
317 juvenile elasmobranchs in tropical waters.

318

319 *Ecological Implications*

320 Activity represents an important component of the energy balance of most fish (Boisclair and
321 Leggett, 1989) and our results indicate that greater negative buoyancies will result in
322 increased costs, as shown by our modelled increases in u_{min} and u_{opt} . Such behavioural
323 modification will increase the energetic cost of locomotion because such power costs increase

324 with swimming speed at exponents of 2-3 (Alexander, 2003; Lowe, 2001). Our results
325 confirmed that despite some compensation by liver density, the negative buoyancies of the
326 two species we studied are approximately twice as great as those of a typical marine
327 elasmobranch of similar mass and lifestyle. At u_{min} the power required to swim is
328 approximately doubled compared to marine water. At u_{opt} , on the other hand, the power
329 would be expected to increase by as much, if not more, depending on the value of GW^2/β .
330 The increased activity costs will depend on a variety of species-specific factors including the
331 ecology of the species, typical swimming speeds, and the amount of time spent resting on the
332 bottom.

333

334 *Evolutionary Implications*

335 Increasing costs of locomotion associated with freshwater residency itself does not preclude
336 elasmobranchs from occupying freshwater habitats, but it may act as a constraint. Teleost fish
337 often compete for the same ecological space with elasmobranchs, but the utility of a gas
338 bladder as a source of upthrust largely negates the buoyancy problem faced by sharks and
339 rays. Juvenile coho salmon (*Oncorhynchus kisutch*) collected along a salinity gradient display
340 compensation in swim-bladder volume; in marine waters a bladder comprising 5% of whole
341 body volume is adequate to provide near neutral buoyancy and in freshwater this volume only
342 increases to 7% (Weitkamp, 2008). This difference is unlikely to affect parasite drag, as
343 surface area and fineness ratio will remain largely unchanged (Alexander, 1966). Indeed, the
344 extraordinarily low density of air ($\sim 5 \text{ kg m}^{-3}$ at 10 m depth at 25 C°) compared to that of
345 lipid ($\sim 900 \text{ kg m}^{-3}$), results in water density not having a great effect on upthrust provided in
346 fish using gas filled bladders. This suggests that elasmobranchs (and by extension all fish
347 that utilise lipid only to provide upthrust) are disadvantaged in freshwater over those using
348 gas.

349

350 Paleontological records also show that early elasmobranchs were not always scarce in
351 freshwater, but dominated marine and freshwater environments by the late Devonian, ~400
352 million years ago, whereas ray-finned fishes only evolved into efficient swimmers in the
353 Mesozoic, approximately 200 million years ago (Long, 1995). We therefore argue that the
354 innovations by modern teleosts, the gas-bladder and its role in buoyancy control in particular,
355 have resulted in a competitive edge over elasmobranchs and contributed to the contemporary
356 low abundance and diversity of freshwater sharks and rays. The material constraints of tissues
357 providing lift in elasmobranchs will inevitably result in greater negative buoyancies in
358 freshwater and result in lower locomotory performance compared to those groups able to use
359 gas. This effect can be somewhat offset, however, it appears that sharks are unable to escape
360 the constraints of lipid-produced upthrust.

361

362 The patterns of diversity in freshwater elasmobranchs also supports our conclusions; ~76 -
363 84% of all elasmobranchs known to occupy freshwater are part of the order Myliobatiformes
364 (Ballantyne and Fraser, 2013; Martin, 2005). Myliobatiforms are a group of largely benthic
365 rays, such as whiptails (*Himantura* spp.) and stingrays (*Dasyatis* spp.). Individuals within this
366 group are largely confined to movement close the substratum (with some exceptions) and
367 often occur over flat sandy or muddy substrates. The costs of increased negative buoyancy
368 would be drastically reduced in those species, due to benthic resting and the majority of
369 swimming being performed close to the substrate. Swimming close to the bottom reduces the
370 induced drag by a lifting surface as a result of increased pressure forming on the ventral side
371 of the lifting surface, known as the ground effect (Webb, 1988). Indeed, in gliding bird flight,
372 the ground effect may be responsible for a 49% reduction of drag due to lift (Hainsworth,

373 1988). The generally higher density of liver tissue in benthic elasmobranchs supports this, as
374 there is less of an energetic incentive to reduce submerged weight in this group.

375

376 Our paper is the first to demonstrate that the reduced density of freshwater represents a
377 significant physical challenge for elasmobranch locomotion that manifests as greatly
378 increased negative buoyancy. These results indicate that freshwater sharks partially
379 compensate with lower density liver tissue, rather than increasing overall liver volume. Given
380 these data, elasmobranchs in freshwater habitats experience significant negative buoyancy
381 and can only compensate by generating more lift through forward locomotion. Such
382 behavioural compensation will result in greater energy expenditure from increased drag and
383 we argue that buoyancy may have been an important factor constraining the reinvasion of
384 freshwater by sharks and their relatives that may act in concert with osmoregulatory
385 challenges. Additional data on the organismal biology of elasmobranchs occupying salinity
386 gradients as well as paleontological records will be necessary to test these competing, but not
387 mutually exclusive hypotheses.

388

389 **Methods**

390 **Modelling the morphological consequences of environmental density**

391 The following section largely follows the arguments by Alexander (Alexander, 1990), who
392 tested the optimal means of producing lift as a function of swimming speed. Our model is
393 constrained to a single means of producing increased buoyant force (liver lipid), while
394 considering the implications of changing density of the occupied medium. The primary
395 source of increasing the buoyant force in elasmobranchs is the liver, which is characteristic of
396 lower density ($\sim 900 - 1000 \text{ kg m}^{-3}$) than other tissues of a shark ($\sim 1070 \text{ kg m}^{-3}$), the ratio of

397 liver-tissue to non-liver tissue is a major determinant of the buoyancy of a shark. According
 398 to Archimedes,

399

$$400 \quad W = ((V_{\text{Lean}} \rho_{\text{Lean}} + V_{\text{Liver}} \rho_{\text{Liver}}) - (V_{\text{Lean}} + V_{\text{Liver}}) \rho_{\text{Water}}) g \quad \text{eqn. 1}$$

401 where W refers to the submerged weight (or negative buoyancy) and g to the acceleration of
 402 gravity (9.81 m/s^2). Moreover, V_{Lean} and V_{Liver} are the volume of lean and liver tissue
 403 respectively and ρ_{Lean} and ρ_{Liver} are their respective densities. Thus the overall volume and
 404 density of the shark are given by $V_{\text{Shark}} = V_{\text{Lean}} + V_{\text{Liver}}$ and $\rho_{\text{Shark}} = (V_{\text{Lean}} \rho_{\text{Lean}} + V_{\text{Liver}}$
 405 $\rho_{\text{Liver}})/V_{\text{shark}}$, respectively.

406

407 Here we define lean tissue to be all tissue excluding the liver. This set of equations in turn
 408 permits us to estimate the physical consequences of changing water density, i.e. changing
 409 ρ_{Water} to 996 kg m^{-3} , representing the density of freshwater at $28 \text{ }^\circ\text{C}$ compared to 1026 kg m^{-3}
 410 of marine water on submerged weight and the liver size required to off-set the reduced
 411 upthrust provided by the environment. These two phenomena were also investigated under
 412 the assumption that sharks could alter the density of their livers, which has been
 413 experimentally shown for *Squalus acanthias* (Malins and Barone, 1970). A low value for
 414 liver density was taken to be 920 kg m^{-3} , representing the livers of deep-sea sharks (Bone and
 415 Roberts, 1969; Corner et al., 1969) as these animals must face similar constraints in reducing
 416 their submerged weight, while presumably minimizing liver size.

417

418 **Modelling the energetic consequences of changing water density**

419 We investigated, from first principles, the energetic consequences of a hypothetical shark
 420 moving into freshwater, and considered a range of mechanisms that could be employed to
 421 compensate for the decreasing water density as compared to the marine conditions. Changing

422 buoyancy impacts the attendant metabolic expenditures given the changes in swimming
 423 speed, as well as in body lift and drag, which are required to maintain a level trajectory. Such
 424 changes are being assessed herein with the type of aerodynamic modelling that is common in
 425 aircraft design (Dole, 1981; Pope, 1951). The basics of this modelling, along with the most
 426 important results will be discussed in this section, and the mathematical details further
 427 explored in the Appendix and Electronic Supplement (ES1).

428

429 Although the inclusion of low-density lipids in the liver reduces negative buoyancy,
 430 hydrostatic forces are not sufficient to achieve neutral buoyancy in most species. In
 431 elasmobranchs (and many other obligate swimmers) this is achieved through forward motion-
 432 generated lift, which in turns increases drag. Swimmers face two general (physical) energetic
 433 costs incurred by moving through their environment, namely, those related to *parasite* drag
 434 ($F_D^{parasite}$), as generated by the fluid's friction against the body, as well as from the low
 435 pressure of the wake turbulence behind the body; and to *induced* drag ($F_D^{induced}$), as created
 436 by the lift production arising from the upward-angling of the anterior portion of the body and
 437 pectoral fins, and also from the downward thrust component created by the asymmetric
 438 caudal tail. For leopard shark (*Triakis semifasciata*) the balance of lift production is estimated
 439 at approximately 45% from the pectoral fins and 55% from the caudal fin (Fish and
 440 Shannahan, 2000), and we note that these values represent the only force balance estimates
 441 for dynamic equilibrium in sharks.

442

443 Parasite drag applied to a shark moving at speed u can be generally calculated as

444

$$445 \quad F_D^{parasite} = \frac{1}{2} \rho_{water} u^2 \cdot SA \cdot C_D^{parasite} \quad \text{eqn. 2}$$

446

447 Here SA is the reference surface area used when extracting the parasite drag coefficient

448 ($C_D^{parasite}$) from experimental data (usually, by inverting eqn. 2). In comparative

449 biomechanics SA is the body wetted area, approximated here as two joined paraboloids,

450 namely $SA = 0.71(\text{girth} \times \text{pre-caudal length})$, as further discussed in the Electronic

451 Supplement (ES1, eqn. ES.5). On the other hand, the parasite drag coefficient is modelled as

452 the sum of the parasite drag (i.e., friction plus pressure drag) arising separately from the body

453 and from all fins: $C_D^{parasite} = C_D^{parasite}|_{body} + \sum C_D^{parasite}|_{fins}$ (“ \sum ” symbolizes a sum over each454 fin’s contribution). The body parasite drag ($C_D^{parasite}|_{body}$) is expressed in a form developed by

455 Hoerner in his drag studies of bodies of revolution (Blevins, 1992) :

456

$$C_D^{parasite}|_{body} = \frac{K}{Re^\alpha} \left[1 + 1.5 \left(\frac{t}{SL} \right)^{3/2} + 7.0 \left(\frac{t}{SL} \right)^3 \right] \quad \text{eqn. 3}$$

458

459 The parasite drag due to all fins can be expressed similarly, albeit in a more complicated

460 form, and is further discussed in the Appendix and Electronic Supplement (ES 1, see eqns.

461 A.1.and A.2; and ES.6, ES.8 and ES.9). Here the effects of *pressure* drag are represented by462 the terms in t/SL , with t representing the body’s maximum diameter without the fins and SL 463 the pre-caudal length. The coefficient K/Re^α represents the effects of the fluid’s shear stress464 on the body, with Re as the body’s Reynolds number, $Re = SL \cdot u/v$, and with v as the fluid’s465 kinematic viscosity (1.15×10^{-6} and $1.13 \times 10^{-6} \text{ m}^2/\text{s}$ for sea water and fresh water (16°C)

466 respectively)). The fins’ parasite drag coefficient likewise includes a similar friction factor.

467 The coefficient K and exponent α (>0) parameterize the fluid’s friction as the combined result

468 of a shark’s denticulated skin and swimming motions on the body (Oeffner and Lauder, 2012;

469 Shelton et al., 2014). Recent studies of shark hydrodynamics make it clear that the

470 interactions of the boundary layer generated by the skin's denticles interacts with the flows
 471 created by the tail's motions in ways that do not always minimize body drag, and moreover in
 472 ways that are difficult to quantify in simple formulas such as in eqn. 3 (Shelton et al., 2014).
 473 In the interest of simplicity, the values of K and α correspond to those of a smooth flat plate
 474 in longitudinal flow and supporting a turbulent boundary layer ($K = 0.072$ and $\alpha = 0.2$
 475 (Blevins, 1992)). It should be stressed that using flat plate drag data should not be viewed as
 476 approximating shark skin as smooth; but rather, as a proxy for translating the complex
 477 interactions between denticulated skin and tail motions, as suggested by the averaging of the
 478 few rigid body and active swimming drag data so far available on a single shark species
 479 (Anderson et al., 2001).

480

481 The total drag exerted on the body is calculated by adding induced drag to the parasite drag
 482 of eqn. 2. The former is derived from the fact that the induced drag coefficient is proportional
 483 to the square of the lift force (Dole, 1981) and is given by

$$484 \quad F_D^{induced} = \frac{(1 + \delta)}{\pi AR} \cdot \frac{(F_{lift})^2}{\left(\frac{1}{2} \rho_{water} u^2\right) \cdot LS \cdot WD} \quad \text{eqn. 4}$$

485 Parameter AR is an overall body aspect ratio, here defined as that of the body's maximum
 486 width, plus combined pectoral fin span, over pre-caudal body length SL (or $AR = WD/SL$).

487 The force F_{lift} is the total lift generated by *all parts of the body*. Since it is assumed that the
 488 shark is swimming horizontally and at constant speed, lift thus equals negative buoyancy (F_{lift}
 489 $= W$). Finally, δ is an aerodynamic efficiency factor that is set to zero [14] (with aircraft, δ is
 490 typically less than 0.05).

491

492 Estimation of the metabolic expenditures connected to increased drag-production involves a
 493 metric of speed. Postponing the study of expenditures generated at the optimal speed (Weihs,

494 1973), we first consider metabolic expenditures incurred at speeds $u = u_{min}$ where total drag is
 495 *minimal* (Alexander 1990). As discussed further in (Dole, 1981), a point of minimum drag
 496 exists in cases where lift equals weight in aircraft (or body lift equals negative buoyancy in
 497 sharks), as parasite and induced drag are proportional to u^2 and $1/u^2$ respectively.
 498 Furthermore, u_{min} is also the point at which *induced drag is equal to parasite drag*. Thus
 499 solving the latter constraint with equation eqn. 2 and 4 yields a way to calculate u_{min} :

500

$$501 \quad (u_{min})^4 = \frac{1}{\frac{1}{2} \rho_{water} \cdot WD \cdot LS \cdot C_D^{parasite}} \cdot \frac{2W^2}{\pi(WD)^2 \rho_{water}} \quad \text{eqn. 5}$$

502

503 Note that from eqns. 3, A.1 and A2 (and ES.7 and ES.8), it follows that $C_D^{parasite}$ is also
 504 proportional to $(1/u_{min})^\alpha$, with α defined by eqn. 3, so that the final dependence on negative
 505 buoyancy will be as $u_{min} \sim W^{1/(4-\alpha)}$ (or $\sim W^{1/3.8}$ using the flat plate proxy). This result, used
 506 along with eqn. 2, thus suggest that increasing negative buoyancy will indeed lead to higher
 507 swim speed and thus to higher drag.

508

509 The total metabolic power (P_{Total}) required for a shark to move its body through the water at
 510 u_{min} will be given by:

$$511 \quad P_{total} = \frac{1.5F_D^{total}}{\eta} u_{min} = \frac{1.5F_{thrust} \cos \theta}{\eta} u_{min} \quad \text{eqn. 6a}$$

512

513 The second equation highlights the fact that the thrust has a vertical component due to the lift
 514 produced by the heterocercal caudal fin. In cases where the latter $\sim 0.55W$ (Fish and
 515 Shannahan, 2000) the thrust's angle θ with respect to the horizontal would be calculated from
 516 $\tan \theta = 0.55W/F_D^{total}$. The factor 1.5x arises from those effects of lateral tail-beat undulations

517 (which increase the required thrust) that remained unaccounted for by the proxy factor
 518 $K/Re^{0.2}$ above (this proxy averages friction drag of rigid and swimming scup and dogfish in
 519 Anderson et al. (Anderson et al., 2001)). (In comparison, a factor of 2.5 – 3 fold has been
 520 used in fish as compared to a rigid model (Webb, 1971b)). Finally, the factor η measures both
 521 metabolic and propulsive inefficiencies of the tail and body, and set here to $\eta \sim 0.20$ (Webb,
 522 1971a).

523

524 Being oriented perpendicularly to a shark's motion at all times means that the lift force used
 525 to compensate for negative buoyancy does not perform any mechanical work on the body.
 526 However, lift generation *does* involve metabolic energy production since lift production
 527 *always* incurs additional drag in comparison to an identical body generating no lift. This can
 528 be done by re-writing P_{total} as resulting from the power used to compensate for *total* drag, i.e.,
 529 from the sum of parasite drag (eqn. 2) and induced drag (eqn. 4). As discussed further in the
 530 Electronic Supplement (ES1), and evaluated for any arbitrary speeds u , one has:

531

$$532 \quad P_{total} = \frac{1}{\eta_{sw}} \left[\left(\frac{1}{2} \rho_{water} \cdot SA \cdot C_D^{parasite} u^3 \right) + \frac{2W^2}{\pi(WD / SL) \rho_{water} (WD \cdot SL) \cdot u} \right] + W_m \quad \text{eqn. 6b}$$

533

534 Here η_{sw} is a speed-dependent function ($\eta_{sw} = \beta u$) representing both metabolic and propulsive
 535 efficiency of the tail's propulsive apparatus, and the constant W_m the Standard Metabolic Rate
 536 corresponding to the internal metabolic processes that are independent of speed during active
 537 swimming (Weihs 1973). The second term in eqn. 6b is what distinguishes a fish swimming
 538 horizontally while neutrally buoyant ($C_L = 0$), and an elasmobranch doing the same but at C_L

539 $\neq 0$. With the latter and at minimum speed, this second term shows an explicit dependence
 540 on, and an increase with, negative buoyancy ($\sim W^2$).

541

542 The increased metabolic cost of swimming at the optimal speed (u_{opt}) while experiencing
 543 increased negative buoyancy can be assessed by using eqn. 6b along with the approach
 544 proposed by Weihs (1973). This is done by optimizing the distance travelled (l) at fixed
 545 stored energy ($E = P_{total} l/u$), i.e., as a solution of the differential equation $dl/du|_{opt} = 0$ under
 546 the constraint of lift-compensated negative buoyancy. As shown in the Electronic
 547 Supplement (ES1) P_{total} would increase with negative buoyancy (W) as

548 $P_{total}^{opt} = 2W_m + 4GW^2 / \beta u_{opt}^2$ with $G \equiv 2(1 + \delta) / (\pi AR \cdot \rho_{water} \cdot SL \cdot WD)$. The optimal speed increases

549 with W as well, namely as $u_{opt} \propto W^0$ & $u_{opt} \propto W^{1/2}$ at small and large negative buoyancy

550 respectively, after solving the algebraic equation $3GW^2/\beta = \left(\tau/\beta u_{opt}^4 - u_{opt}^2 W_m \right)$ where

551 $\tau \equiv \frac{1}{2} \rho_{water} SAC_D^{parasite}$. Here the parameter GW^2/β determines the regime where the negative
 552 buoyancy can be considered as “small” or “large”. Using typical shark morphological inputs,
 553 this ratio is estimated at $\sim 0.3 - 0.6 \text{ Watts } m^2 s^{-2}$, which places sharks somewhere in between
 554 the two limits. With both β and W_m being unknown in sharks, a quantitative assessment of the
 555 increased costs associated with higher negative buoyancy is currently out of reach.

556

557

558 Equations 2-6a,b and ES 14 now allow us to calculate a power-velocity relationship, i.e.,
 559 where velocity = u_{min} and = u_{opt} respectively for hypothetical sharks in water of different
 560 densities. It has to be noted, that these equations are not analogous to the metabolic rate-
 561 swimming speed relationships (where u is an independent variable), but rather are designed to
 562 provide the lowest hypothetical costs of swimming at a given water density even though no

563 single shark can have an ideal pectoral fin (or body angling) to maximise lift-to-drag ratio
 564 over the range of speeds simulated. Indeed, some species will feature morphological
 565 adaptations for faster cruising whereas others for slower speeds. We have also reflected this
 566 in our efficiency term η , which would be expected to vary with swimming speed of an
 567 individual, but here we will assume that the muscle geometry and tail-beat kinematics are so
 568 that η is maximised at u_{min} , mimicking a fish adapted to the cruising speed that minimises
 569 required power. Muscular efficiency has been experimentally determined for rainbow trout
 570 (*Onchorhynchus mykiss*) and showed that maximum efficiency achieved was 20% (Webb,
 571 1971a).

572

573 Finally, to facilitate comparisons of the energetic impact of changing water density, we
 574 computed the net cost of transport (COT_{net}) to reflect the energetic cost of moving the animal
 575 (and its variable mass depending on liver size) 1 m in distance.

576

$$577 \quad COT_{net} = \frac{P_{total}}{u_{min} m} \quad \text{eqn. 7}$$

578

579 With regards to the drag calculations, the necessary input morphometric data for the bull
 580 shark and smooth dogfish discussed in the sections below are listed in Tables ES1 – ES4.

581

582 We decided to model 4 hypothetical scenarios (see Table 1 for all parameters used in the
 583 models described previously) that sharks could use to counteract changing buoyancies:

584

585 *Scenario 1 – No compensation*

586 Elasmobranchs do not alter their morphology in response to changing environmental density
587 and the mechanical costs of swimming change in accordance with the increasing negative
588 buoyancy.

589

590 *Scenario 2 – Reduced Liver Density*

591 Elasmobranchs have been shown to respond to experimentally increased negative buoyancy
592 by decreasing the density of their livers (Malins and Barone, 1970), effectively increasing the
593 buoyant force and reducing negative buoyancy. This scenario would result in no change in
594 liver size (and no changes in surface area), but would dampen the increase in negative
595 buoyancy with decreasing water density. We consider a liver density of 920 kg m^{-3} to be a
596 lower bound of liver density. Livers of this density are encountered in neutrally buoyant
597 sharks such as *Cetorhinus maximus* (Bone and Roberts, 1969).

598

599 *Scenario 3 – Increasing Liver Size*

600 Increasing the size of the liver is another mechanism by which more upthrust can be
601 generated and the impact of decreasing water density can be mitigated. We consider that 30%
602 of the body volume to comprise of liver tissue to be the upper ceiling of hypothetical livers.
603 This represents a realistic upper bound. Similar liver sizes are encountered in sharks that are
604 close to neutral buoyancy and these species face a similar constraint in minimising negative
605 buoyancy. Increasing liver volume while maintaining the volume of lean tissue is expected to
606 increase surface area and decrease fineness ratio, affecting parasite drag.

607

608 *Scenario 4 – Increasing Liver Size and reduction of Liver Density*

609 This scenario represents a combination of scenarios 2 and 4. The two distinct processes can
610 act synergistically in providing more buoyancy. We modelled the energetic consequences of

611 these four scenarios, using the observed body composition of bull sharks (*Carcharhinus*
612 *leucas*) captured in Florida by Baldrige (1970). Namely, we consider that the lean tissue
613 density is 1075 kg m^{-3} , the nominal liver density is 964 kg m^{-3} and liver volume represents
614 11% of whole body volume. We parameterised this model with a shark of 1m pre-caudal
615 length and an associated mass of 15 kg (Thorburn, 2006).

616

617 **Field Methods**

618 *Capturing of animals*

619 Largetooth sawfish (*Pristis pristis*) and bull sharks were captured between September and
620 October 2011 and 2012 in the Fitzroy River, Western Australia. Animals were captured using
621 bottom-set gill-nets (15 and 20 cm stretched mesh-size) set at night. Nets were checked at
622 regular intervals of 1.5 hours.

623

624 **Measurement and calculation of body density**

625 Captured sawfish and bull sharks were initially sexed and measured. Animals were weighed
626 to the nearest 5 g using a sling and digital hanging-scale (UWE HS 7500 series, Capacity:
627 7500g, Resolution: 5g). To determine the submerged weight (W_{sub}) of the animals, a sling
628 was suspended from a tripod (Daiwa infinity weigh tripod) in water of approximately 1.2 m
629 depth. Before animals were placed into the sling, the weight of the sling was zeroed. Animals
630 remained motionless in the sling and a weight was read after the scale stabilised. While
631 weighing, it was ensured that no part of the sling touched the river-bed or the tripod. After
632 submerged weight was determined, we measured the mass of animals using the same sling
633 and scale, without submergence. Care was taken that no water remained in the sling when the
634 mass was determined. Following these measurements, whole body density (ρ_{Shark}) was
635 calculated based on the density of freshwater at $28 \text{ }^{\circ}\text{C}$, the common water temperature during

636 night time (Gleiss & Morgan, unpubl. data) with a corresponding water density of 996 kg m^{-3} ,
637 as determined by the relation $\rho_{\text{shark}} = (W_{\text{air}} \rho_{\text{water}}) / (W_{\text{air}} - W_{\text{sub}})$.

638

639 **Determination of Liver density and liver-free body density**

640 All individuals that perished in gill-nets were used for further analysis of buoyancy
641 regulation. After determining whole body density, fish were dissected and liver density and
642 volume was determined by displacing livers in a graded water cylinder. Livers were
643 forcefully submerged with a long toothpick, to overcome positive buoyancy. The volume of
644 the toothpick was negligible in relation to liver volume. Liver density (ρ_{liver}) was simply
645 calculated from mass and displaced volume. Density of the liver-free body (ρ_{lean}) was
646 determined in the same fashion as prior to dissection of the liver, by determination of mass
647 and submerged weight using the described sling.

648

649 **Meta-analysis of densities in marine and freshwater elasmobranchs**

650 In order to compare buoyancy between marine and freshwater forms, we collated all such
651 measurements from the literature, primarily based on two publications (Baldrige Jr, 1970;
652 Bone and Roberts, 1969). Some parameters were not reported in these original papers (e.g.
653 liver-free density), but could be calculated based on the data provided. We excluded any
654 deep-sea individuals from the analysis due to significantly different densities (near neutral) as
655 a result of the different lifestyle, as well as the basking shark for the same reason, resulting in
656 113 Individuals of 27 marine species being included in the analysis. In order to compare our
657 data from freshwater elasmobranchs to the marine forms, we analysed the data using Mixed
658 Models, due to unbalanced sample size for the different species (Zuur et al., 2007). To
659 account for these repeated measures on a single species, we used the species ID as a random
660 effect in our model. Models also included lifestyle as a covariate, which was determined

661 based on the species description in Compagno (2001), separating species into two groups
 662 considered to exclusively associate with the sea-bed (demersal), and those that swim in the
 663 water-column (pelagic & benthopelagic, see Supplementary Table ES1), as previous papers
 664 have shown the impact of lifestyle on buoyancy in elasmobranchs (Bone and Roberts, 1969).
 665 Mixed Models were fitted using the "lme4" package implemented in the R statistical package
 666 (R Development Core Team, 2010) and model selection was based on small sample corrected
 667 Akaike's Information Criterion (AIC_c) computed in the model selection package "MuMin".
 668

669 **Appendix. The parasite drag of fins**

670
 671 An aircraft wing's drag is calculated with computer programs that, from an airfoil's known
 672 shape and dimension data, yield the parasite and induced drag, the lift force and aerodynamic
 673 moments. Having no information about the airfoil profiles of shark fins, we resort to an
 674 approach similar to that of eqn. 3. Here again the parasite drag of airfoils and fins generate
 675 both friction and pressure drag, with the latter being generally much smaller than the former.
 676 The effects of both on each fin is represented by another equation developed by Hoerner, but
 677 applied to symmetrical airfoils ((Blevins, 1992); p. 352):

$$678 \quad C_{D \text{ parasite}} \Big|_{fin} = C_{friction}^{fin} \left[1 + 2.0 \left(\left\langle \frac{t_{fin}}{FC} \right\rangle \right) + 60.0 \left(\left\langle \frac{t_{fin}}{FC} \right\rangle \right)^4 \right] \quad \text{eqn. A.1}$$

679 The pressure drag terms in $\langle t_{fin}/FC \rangle$ represent the mean *fin maximum thickness over fin*
 680 *chord*, as averaged over chord span. Herein $\langle t_{fin}/FC \rangle = 0.2$ for all caudal and non-caudal
 681 fins. The factor $C_{friction}^{fin}$ is, on the other hand, the shear stress friction created on each side of
 682 a fin. The detailed derivation of this coefficient appears in the Electronic Supplement (ES 1).
 683 Unlike the body which was likened to a thin, flat rectangular surface of same area for the
 684 purpose of friction coefficient calculation (i.e., the K/Re^a factor in eqn.3), a non-caudal fin is
 685 regarded instead as a thin and two-sided right triangle of base (or "root chord") FC and height

686 (or “span”) FS. The distinction is necessary since the shear stress exerted on a rectangle in the
 687 direction of the flow is the same over its width, in contrast to that of a triangle in which both
 688 chord and shear stress decreases span-wise from (fin) root to tip. Covering each side of a fin
 689 with long (chordwise) and narrow (spanwise) rectangular strips of known shear stress (Fig.
 690 ES.1), the friction factor comes out as follows for *each non-caudal fin*

$$691 \quad C_{friction}^{non-caudal-fin} = \left(\frac{(FS)^{2-\alpha}}{SA} \right) \cdot 2 \cdot \frac{K}{(u/\nu)^\alpha} \left(\frac{FC}{FS} \right)^{1-\alpha} \left(\frac{1}{2-\alpha} \right) \quad \text{eqn. A.2}$$

692 As with the body, the friction drag coefficient of each strip is parameterized by our proxy
 693 $C_{friction} = K/Re^\alpha$. On the other hand, and being highly swept, caudal fins are instead
 694 approximated by two right triangles of differing root chords (FCA and FCB) but of same
 695 span (FS), with one triangle inserted into the other in a manner to superpose their span
 696 (Figure ES.2). Here FCA is the root chord of the actual swept fin and $FCA < FCB$ by
 697 construction. Using strips again to calculate the friction coefficient yields the same equation
 698 as A.2, but with the factor $(FC/FS)^{1-\alpha}$ replaced by $(FCA/FS)^{1-\alpha}$.

699

700 The parasite drag force of a fin (caudal and non-caudal) is then calculated by multiplying the
 701 friction drag coefficient above by the factor $1/2 \rho_{water} u^2 SA$, per eqn. 2 (u being the shark’s
 702 speed). Note that eqn. A.2 assumes strictly chord-wise flows, thus neglecting cross-flow
 703 effects. Note also that with shark bodies and fins being slender, the *parasite* drag formulae
 704 discussed in this paper are generally insensitive to angles of attack (AOA), i.e., *when away*
 705 *from stall*. *Induced* drag, on the other hand, *is* sensitive to AOA and specific airfoil profile,
 706 but the constraint $W = F_{lift}$ used here allows us to ignore such details as W is known.

707

708

709

710

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720

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850 **Table 1 Hypothetical morphological scenarios that were modelled in response to**
 851 **changing salinity.** Scenario 0 represents the Null Model of the morphological characters for
 852 a 1.25 m bull shark in marine waters.
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	Scenario 0	Scenario 1	Scenario 2	Scenario 3	Scenario 4
	Marine	No compensation	Increasing Liver Size	Decreasing Liver Density	Increasing Liver Size + Decreasing Liver Density
Mass (kg)	14.5	14.5	18.3	14.5	18.3
Water Density (kg m ⁻³)	1026	996	996	996	996
Lean Tissue Density (kg m ⁻³)	1076	1076	1076	1076	1076
Liver Tissue Density (kg m ⁻³)	964	964	964	920	920
Lean Tissue Volume (m ³)	0.0118	0.0118	0.0118	0.0118	0.0118
Liver Tissue Volume (m ³)	0.0020	0.0020	0.0045	0.0021	0.0045
Surface Area of body (m ²)	0.59	0.59	0.66	0.59	0.66
Fineness ($\frac{t}{SL}$)	0.212	0.212	0.234	0.211	0.234
Projected Frontal Area (m ²)	0.035	0.035	0.045	0.035	0.045
Submerged Weight (N)	4.40	8.44	7.26	7.47	4.44

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883 **Table 2 Details of all sawfish and bull sharks that were weighed in air and while**
 884 **submerged.**
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	TL (mm)	Mass (g)	W_{sub} (N)	Buoyancy Ratio (%)	V (ml)	P_{Shark} (kg m⁻³)
<i>C. leucas</i>	862	4175	2.50	6.11	3936	1060.8
<i>C. leucas</i>	824	3390	2.35	7.08	3163	1071.9
<i>C. leucas</i>	851	4145	2.60	6.39	3896	1064.0
<i>C. leucas</i>	950	4815	2.89	6.13	4538	1061.0
<i>C. leucas</i>	840	3765	2.40	6.51	3534	1065.3
<i>P. pristis</i>	1224	4600	2.74	6.07	4338	1060.3
<i>P. pristis</i>	1018	2365	1.47	6.34	2224	1063.4
<i>P. pristis</i>	1140	3780	2.48	6.69	3541	1067.4
<i>P. pristis</i>	1151	3660	2.26	6.28	3444	1062.8
<i>P. pristis</i>	1090	3130	1.91	6.23	2947	1062.2
<i>P. pristis</i>	1082	2890	1.81	6.40	2716	1064.1
<i>P. pristis</i>	1025	3015	1.81	6.14	2841	1061.1
<i>P. pristis</i>	1119	3060	2.01	6.70	2866	1067.5
<i>P. pristis</i>	1021	2170	1.32	6.22	2043	1062.1
<i>P. pristis</i>	1207	4230	2.75	6.62	3966	1066.6
<i>P. pristis</i>	1079	2765	1.77	6.51	2595	1065.4
<i>P. pristis</i>	1040	2760	1.96	7.25	2570	1073.8
<i>P. pristis</i>	1104	2895	1.91	6.74	2711	1067.9
<i>P. pristis</i>	1025	2215	1.47	6.77	2073	1068.3
<i>P. pristis</i>	912	1530	1.03	6.86	1431	1069.4
<i>P. pristis</i>	1172	4000	2.50	6.38	3760	1063.8
<i>P. pristis</i>	1120	3600	2.11	5.97	3399	1059.3

Table 3 Details of the sawfish (n=2) and bull sharks (n=3) that were available for full necropsies.

	<i>Carcharhinus leucas</i>				<i>Pristis pristis</i>		
	<i>1</i>	<i>2</i>	<i>3</i>	Mean	<i>1</i>	<i>2</i>	Mean
Total length (mm)	862	824	851	846 ± 20	1146	1130	1138 ± 11
Mass (g)	4175	3390	4145	3903 ± 445	4000	3600	3800 ± 283
W_{sub} (N)	2.50	2.35	2.60	253 ± 13	2.50	2.07	235 ± 28
Body Volume (ml)	4429	3634	4410	4158 ± 454	4255	3813	4034 ± 312
% Mass / Submerged Weight	6.11	7.08	6.39	6.53 ± 0.50	6.38	5.97	6.17 ± 0.28
Mass excluding liver (g)	3860	3150	3750	3587 ± 382	3770	3360	3565 ± 290
Submerged Weight excluding liver (g)	280	225	260	255 ± 28	255	215	235 ± 28
Liver Mass (g)	410	226	289	308 ± 93	230	240	235 ± 7
Liver Volume (ml)	450	235	320	335 ± 108	234	245	240 ± 8
Body Volume excluding Liver (ml)	3594	2937	3504	3345 ± 356	4021	3579	3800 ± 312
Body Density (kg m⁻³)	1061	1072	1064	1066 ± 6	1064	1059	1060 ± 3
Body Density excluding liver (kg m⁻³)	1074	1073	1070	1072 ± 2	1068	1064	1066 ± 3
% Liver Volume	7.71	6.22	8.88	7.60 ± 1.33	5.51	6.15	5.83 ± 0.45
% Liver Mass	9.81	6.65	6.98	7.82 ± 1.74	5.75	6.67	6.21 ± 0.65
Liver Density (kg m⁻³)	910	960	904	920 ± 31	982	980	981 ± 2

Table 4 Model selection criteria for 3 analysis (Fig. 2) comparing morphological data from freshwater elasmobranchs sampled as part of this study and marine forms published in previous papers (Baldrige Jr, 1970; Bone and Roberts, 1969).

	Model	df	logLik	AICc	delta	weight
Mass vs Liver Mass	logLiverMass ~ logMass	4	45.88	-83.4	0	0.433
	logLiverMass ~ logMass + Lifestyle	6	47.21	-82.3	1.14	0.245
	logLiverMass ~ logMass + Lifestyle + Habitat	5	46.179	-81.8	1.6	0.194
	logLiverMass ~ logMass + Habitat	7	48.002	-81	2.44	0.128
Mass vs Wsub	logWsub ~ logMass + Habitat	5	122.817	-233.9	0	0.5
	logWsub ~ logMass + Lifestyle + Habitat + logMass * Lifestyle	6	122.92	-231.7	2.18	0.168
	logWsub ~ logMass + Lifestyle	4	123.057	231.2	2.67	0.131
	logWsub ~ logMass + Habitat*Lifestyle	7	119.679	231.1	2.86	0.12
Liver Density	P _{Liver} ~ Lifestyle + Habitat	6	254.169	-495.6	0	0.865
	P _{Liver} ~ Lifestyle	5	251.078	-491.6	3.96	0.120
	P _{Liver} ~ Habitat	4	247.401	-486.4	9.13	0.009
	P _{Liver} ~ 1	1	245.926	-485.6	9.94	0.006
Lean Tissue Density	P _{Lean Tissue Density} ~ 1	1	77.389	-148.6	0	0.605
	P _{Lean Tissue Density} ~ Habitat	4	77.415	-146.5	2.08	0.214
	P _{Lean Tissue Density} ~ Lifestyle	5	78.033	145.6	3.01	0.135
	P _{Lean Tissue Density} ~ Lifestyle + Habitat	6	78.059	-143.4	5.16	0.046

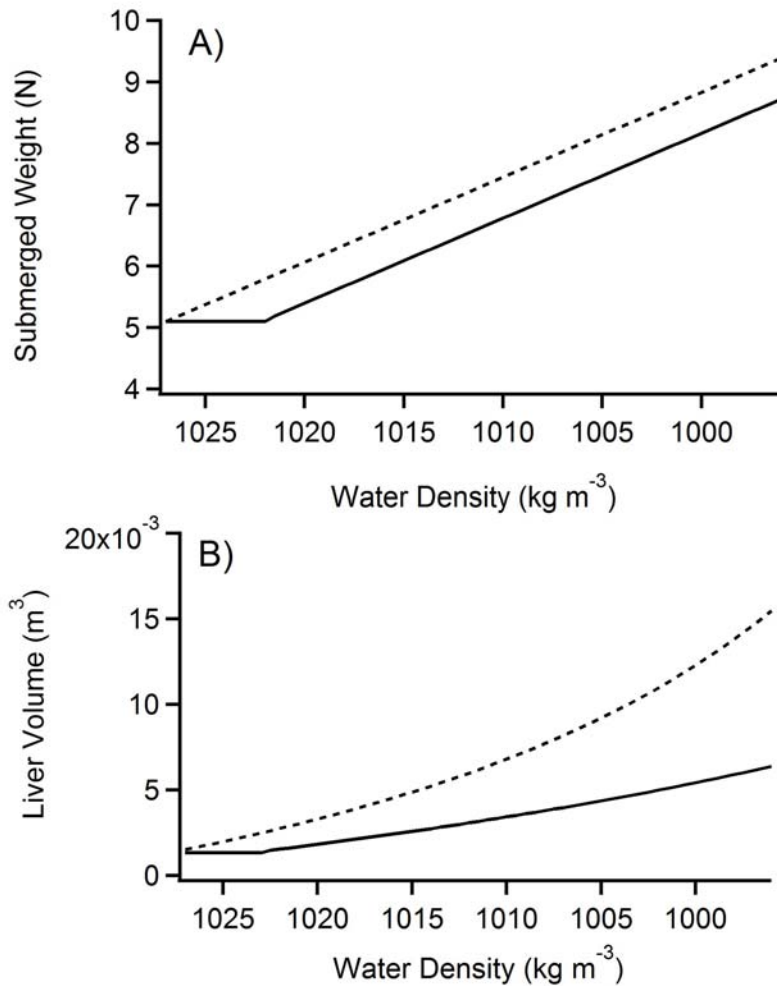


Figure 1 Modelled implications of water density for the buoyancy control of elasmobranchs. Data were modelled based on the equation 1 and parameterised with a hypothetical shark of 15 kg with the same body composition and tissue densities as those observed in Baldrige (Baldrige Jr, 1970). The stippled line indicates the response to changing environmental density if no compensation in liver density occurs. The solid lines represents the same model, assuming that the animal has the ability to reduce its liver density to those encountered in neutrally buoyant deep-sea sharks ($\sim 920 \text{ kg m}^{-3}$) representing the lowest liver densities encountered in elasmobranchs. A) Assuming no morphological changes (i.e. constant tissue volumes and densities), submerged weight would increase by $\sim 120\%$ for a shark moving into freshwater. A reduction in liver density to 920 kg m^{-3} would be able to compensate any changes in water density up to $\sim 1025 \text{ kg m}^{-3}$, yet still resulting in submerged weight doubling. B) Negative buoyancy may also be compensated by changes in liver size; in order to maintain the same submerged weight (4.5 N) as in marine waters, our hypothetical shark's liver would have to increase 8-fold in volume (stippled line) and even if liver density would be reduced, liver volume would have to increase 3-4 fold to maintain similar buoyancy as in marine waters. These cases would result in liver size comprising 70% or 35% of whole body volume respectively compared to 11% in marine waters. In all scenarios described, lean tissue density and volume are unchanged.

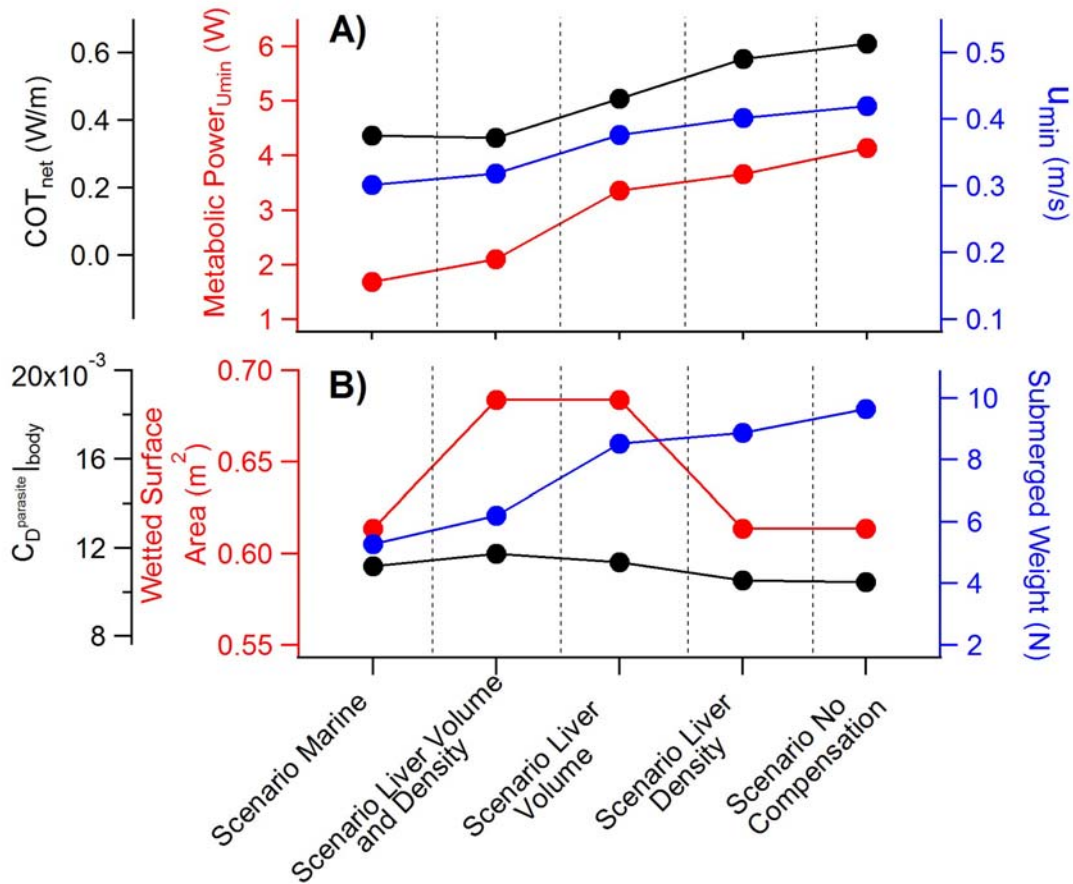


Figure 2 Parameters and results of our modelling exercise (bull shark, 1.2m standard length). A) All scenarios result in increasing costs of locomotion, as a result of increasing u_{min} which increases drag. All hypothetical scenarios also result in increasing cost of transport, with the exception of the scenario where liver size increases and liver density decreases. B) This pattern is a result of all scenarios being characteristic of increased negative buoyancy, with the lowest increase where both density and size have been altered. Based on our considerations of u_{min} , all potential compensatory strategies result in increased costs. Based on u_{min} , increases in liver size and liver density should be the optimal strategy for compensation. This however, ignores the cost of swimming at faster speeds, which are discussed in Figure 4.

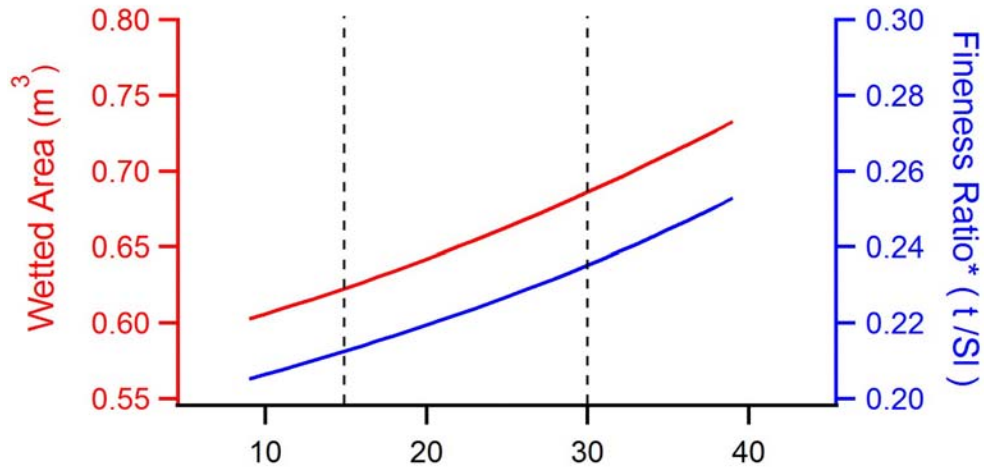


Figure 3 Hydrodynamics of increasing liver size. To gauge the costs associated with faster speeds that may be employed during foraging, here we model the implications of increasing liver sizes on drag. As induced drag responds $1/u^2$, its contribution to total drag at greater speeds will diminish, while parasitedrag will increase u^2 . Here we show that increasing liver size results in an increase of two of the primary parameters that contribute to parasite drag. All things being equal, drag is proportional to wetted area (eqn. 3) and our approximation suggests that this parameter will increase by $>10\%$ from liver volume of 15% - 30% (dashed vertical lines). The Fineness Ratio is the dominant factor in the calculation of $C_D^{parasite}|_{body}$ (eqn. 3). Increasing the fineness ratio by 10% subsequently results in a less streamlined body and a higher drag coefficient proportional to that increase. These data therefore suggest that compensatory mechanisms involving increasing liver size may reduce the costs at low swimming speeds, but will result in significantly increased costs at faster speeds. *Please note that our definition of fineness ratio is the inverse of its typical use. We have chosen to adhere to this format as a result of the formulation in eqn. 3.

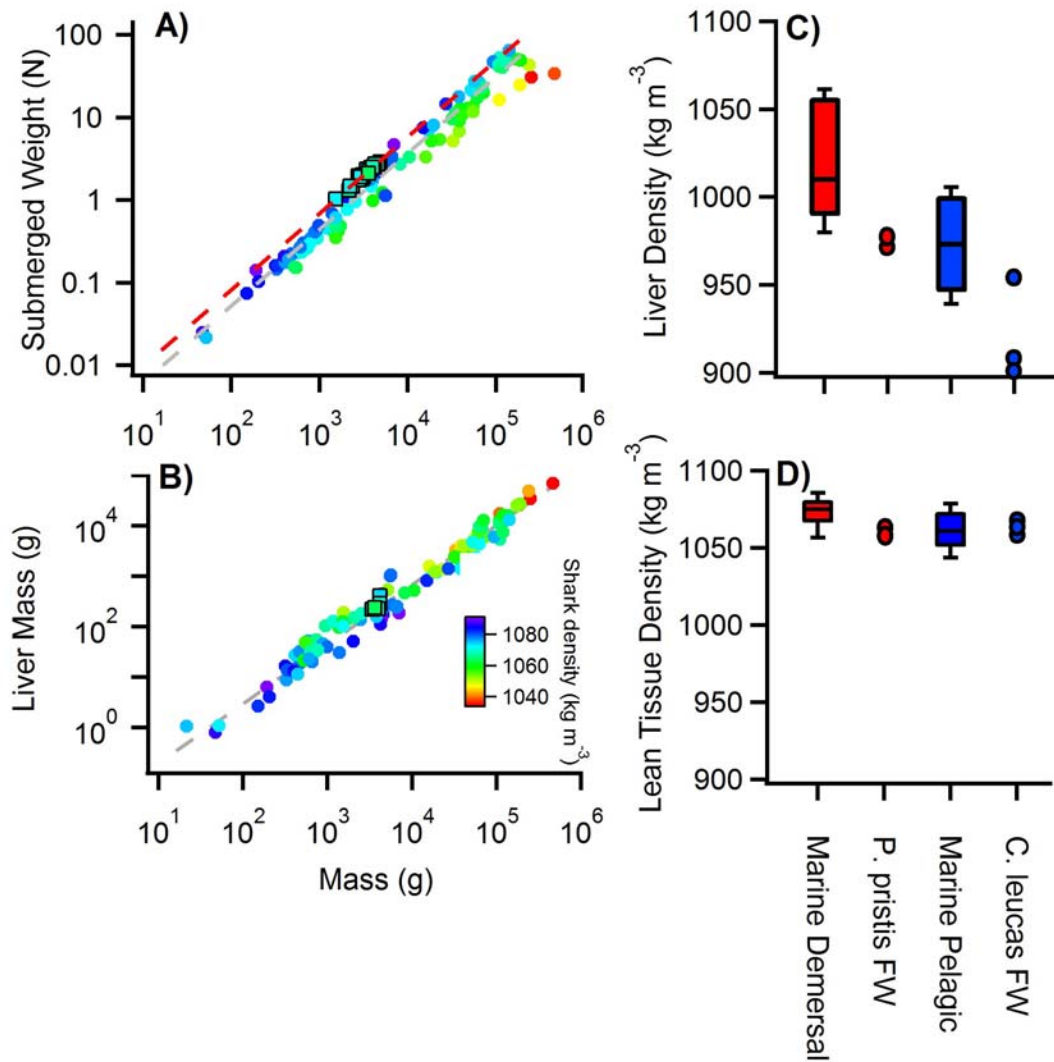


Figure 4 Morphological differences in marine and freshwater elasmobranchs. A) Significant differences were found in the submerged weight between all individuals sampled by Bone and Roberts (1970) and Baldrige Jr (1970) in marine waters (grey stippled line, excluding species that are neutrally buoyant, such as deep-sea sharks and the basking shark, *Cetorhinus maximus*) and *Carcharhinus leucas* (n=5) and *Pristis pristis* (n=20) sampled in freshwater as part of this study (red stippled line). B) No differences in liver size between individuals sampled in marine environments and the 2 sawfish and 3 bull sharks that were available for full necropsy. C) Comparison of liver density in the sharks sampled from marine waters and those from freshwater. The lifestyle of the species has a significant effect on liver density, with demersal individuals having denser livers than those that are pelagic. The two species we sampled in freshwater were close or below the lower 90th percentile for all marine individuals sampled previously suggesting that individuals occupying freshwater may have lower liver densities. D) No major differences in lean tissue density could be detected between either lifestyles or habitat. See Table 4 for the model selection for all three analyses.