

Rolling with the flow: Bumblebees flying in unsteady wakes

Sridhar Ravi^{1*}, James Crall¹, Alex Fisher² and Stacey Combes¹

¹Dept. of Organismic and Evolutionary biology, Harvard University, Cambridge, MA 02138, USA

²Sch. Of Aerospace, Mechanical and Manufacturing Engineering, RMIT University, Melbourne, Vic 3000, Australia

* Author for correspondence (sravi@fas.harvard.edu)

ABSTRACT

Our understanding of how variable wind in natural environments affects flying insects is limited, because most studies of insect flight are conducted in either smooth flow or still air conditions. Here, we investigate the effects of structured, unsteady flow (the von Karman vortex street behind a cylinder) on the flight performance of bumblebees (*Bombus impatiens*). Bumblebees are “all-weather” foragers and thus frequently experience variable aerial conditions, ranging from fully mixed, turbulent flow to unsteady, structured vortices near objects such as branches and stems. We examined how bumblebee flight performance differs in unsteady *versus* smooth flow, as well as how the orientation of unsteady flow structures affects their flight performance, by filming bumblebees flying in a wind tunnel under various flow conditions. The three-dimensional flight trajectories and orientations of bumblebees were quantified in each of three flow conditions: (1) smooth flow, (2) the unsteady wake of a vertical cylinder (inducing strong lateral disturbances) and (3) the unsteady wake of a horizontal cylinder (inducing strong vertical disturbances). In both unsteady conditions, bumblebees attenuated the disturbances induced by the wind quite effectively, but still experienced significant translational and rotational fluctuations as compared to flight in smooth flow. Bees appeared to be most sensitive to disturbance along the lateral axis, displaying large lateral accelerations, translations, and rolling motions in response to both unsteady flow conditions, regardless of orientation. Bees also displayed the greatest agility around the roll axis, initiating voluntary casting maneuvers and correcting for lateral disturbances mainly through roll in all flow conditions. Both unsteady flow conditions reduced the upstream flight speed of bees, suggesting an increased cost of flight in unsteady flow, with potential implications for foraging patterns and colony energetics in natural, variable wind environments.

Key words: Bumblebee flight, flight stability, von Karman street, unsteady flows, turbulence

Short title: Bumblebee flight through vortices

31 INTRODUCTION

32 Volant insects employ a variety of unsteady fluid-mechanic phenomena to remain airborne, including
33 leading edge vortex generation (Ellington et al., 1996), wake capture during hovering (Dickinson et al.,
34 1999), rotational circulation during pronation and supination (Dickinson et al., 1999), and reduction of
35 the Wagner effect via clap and fling (Miller and Peskin, 2009). Over the past two decades, our
36 understanding of these phenomena has been significantly improved by studies exploring the flow field
37 over insect wings in free and/or tethered flight conditions, and through the use of dynamically scaled
38 robotic models (see, Sane, 2003 and Wang, 2005 for reviews). Nearly all experiments on insect flight
39 aerodynamics have been conducted within the confines of laboratories, in the absence of external flow
40 (i.e. still air) or in very smooth flow produced by laminar wind tunnels. However, the vast majority of
41 insects reside in the outdoor environment, within the Atmospheric Boundary Layer (ABL) that extends to
42 a few hundred meters above the Earth's surface, where atmospheric properties (wind, temperature,
43 humidity, etc.) are significantly influenced by the terrain (Stull, 1988). Though migrating insects routinely
44 fly at much higher altitudes (> 1000 m) and are assisted by large-scale meteorological events, these
45 insects too descend to the surface layer for tasks such as feeding, resting, and mating (see Drake and
46 Farrow, 1988 and Chapman et al., 2011).

47 Flight within this region of the atmosphere can be challenging, even in wind-free conditions, because
48 the Earth's surface is seldom flat, and it contains numerous natural and man-made structures that
49 hinder straight, level flight. Wind conditions within the ABL are highly variable, due in part to pressure
50 differences induced by meteorological phenomena and Coriolis forces arising from the Earth's rotation.
51 Excluding extreme weather events, mean wind speeds in the ABL generally vary from 0 m/s (still air) to
52 10 m/s (strong breeze), and wind direction can change rapidly (Stull, 1988). Diurnal insects are further
53 challenged by stronger daytime winds due to convection from the Earth's surface. Some insects may be
54 forced to cease flying in windy weather (Feltwell, 1982 Hendry, 1989 and Combes and Dudley, 2009),
55 but many appear to be capable of contending with the adverse effects of strong, variable environmental
56 airflow through active and/or passive flight control strategies (Crall and Combes, 2013). While some
57 recent studies have investigated the effects of large-scale weather phenomena on insect flight,
58 particularly related to long-distance migration (Chapman et al., 2011), the effects of variable wind
59 patterns on insect flight at shorter time-scales within the ABL remain virtually unexplored.

60 The interaction between airflow and the terrain, which imposes obstacles in the wind's path, can result
61 in highly complex and turbulent flow fields (Watkins et al., 2006). While the flow far away from

62 obstacles is generally well mixed and turbulent, flow in the near wake can be significantly different, with
63 objects such as trees, branches, and flowers producing unsteady but structured flow fields similar to
64 those seen in the wake of bluff bodies. Here, we investigate the effects of unsteady, structured flow in
65 the wake of bluff bodies on the flight performance of bumblebees. Bumblebees are ideal subjects for
66 studying the effects of unsteady wind on insect flight, as they continue to forage even in adverse
67 weather conditions (Heinrich, 2004 and Crall and Combes, 2013) and thus are likely to experience a wide
68 range of environmental flow conditions.

69 We measured instantaneous position and orientation of bees as they flew upstream in a wind tunnel
70 through smooth flow, as well as through the unsteady, von Karman vortex street present in the wake of
71 a circular cylinder. The cylinders used to generate unsteady flows may be considered as abstracts of the
72 tree trunks or branches that bees would routinely fly around while foraging in windy weather. We also
73 investigated the effects of the orientation of the flow disturbance by generating flows behind both a
74 vertical and a horizontal cylinder, which induced strong lateral and vertical disturbances, respectively.

75 Several recent studies have revealed that body orientation and translational motions are tightly coupled
76 in some flying insects (e.g., in both hawkmoths and bumblebees, pitch angle is coupled to
77 longitudinal/forward motion (Dudley and Ellington, 1990 and Willmott and Ellington, 1997
78 respectively)). However, these coupled motions have primarily been examined during voluntary
79 maneuvers such as turning, ascending or accelerating, and therefore reflect active control strategies
80 initiated by the insect. The passive response of flying insects subjected to unexpected aerodynamic
81 disturbances may be very different, and rotational and translational motions may not be coupled in the
82 same way. In addition, the passive responses of insects to external flow disturbances may differ
83 between species, depending on morphology and flight kinematics. For example, honeybees subjected
84 to an isolated gust of wind display large rolling motions, whereas stalk-eye flies subjected to the same
85 disturbance display significant yaw as well as roll (Vance et al., 2013). Identifying the body axes about
86 which insects are least stable to external perturbations, as well as the coupled rotational and
87 translational motions employed during active maneuvering is a critical step in understanding how flying
88 insects negotiate complex, natural aerial environments.

89 We compared the performance of bees flying in smooth and unsteady, structured flow to address three
90 main questions: (1) How does unsteady, structured flow affect the trajectory and flight speed of
91 bumblebees?, (2) How does unsteady flow affect the orientation and stability of bumblebees?, and (3)

92 Do flow disturbances oriented vertically or horizontally produce equivalent responses along the
93 corresponding axes of flying bees?

94 **MATERIALS AND METHODS**

95 ***Study specimens and flight tests***

96 Bumblebees (*Bombus impatiens*) from a commercial breeder (BioBest) were maintained in the lab and
97 given continuous access to a foraging chamber where they could feed freely from an artificial, purple
98 flower containing linalool-scented nectar. Fourteen individuals of similar size (body length = 14 mm \pm 0.5
99 mm, mass = 165 mg \pm 10%) were selected for flight experiments.

100 Each bee was isolated from the hive and cold anesthetized, and a marker (discussed below) was affixed
101 to the dorsal surface of its thorax using cyanoacrylate glue. The marked bee was then placed in a
102 transparent chamber (0.4 x 0.4 x 0.4 m) and allowed to recover and fly freely, without access to food, for
103 approximately two hours prior to the experiment.

104 Once sufficiently starved, each bee was placed in the wind tunnel (with no airflow) where it could feed
105 from an artificial flower resembling the one in the foraging chamber. Once feeding commenced, the bee
106 was allowed to feed for approximately 10 seconds, then separated from the nectar source and released
107 at the downstream end of the wind tunnel. If the bee did not fly towards the artificial flower, it was
108 manually re-introduced to the nectar source and subsequently separated. This cycle was repeated until
109 the bee flew directly to the nectar source. Once consistent behavior was established, wind was
110 introduced and bees were filmed as they flew upstream through smooth flow or an unsteady flow field.
111 Each bee was flown sequentially in each of the three flow conditions, with the order of flow conditions
112 randomized between individuals.

113 Experiments were conducted in a 6 m long suction-type open-return wind tunnel with a 0.9 x 0.5 x 0.5 m
114 working section. The wind-speed was set to \sim 2.55 m/s, which represents an intermediate cruising
115 velocity for bumblebees (Ellington, 1991). To generate structured, unsteady flow, a circular cylinder with
116 a diameter of 25 mm, corresponding to the average wing span of the bumblebees, was placed at the
117 inlet of the test section, extending across the width of the working section. The artificial flower that bees
118 flew towards was positioned within the cylinder in the unsteady trials (Fig. 1A). To maintain behavioral
119 consistency in the smooth flow trials, we attached a small (\sim 5 mm diameter) artificial flower to the
120 upstream mesh of the wind tunnel.

121 This method of unsteady flow generation gives rise to a von Karman vortex street in the wake of the
122 cylinder (Fig. 1A), and has been employed by a number of researchers examining the influence of
123 unsteady flow on swimming and flying animals (Liao et al., 2003; Beal et al., 2006; as well as Hedrick et
124 al. in this issue). At the chosen velocity, the spatial scales of the vortices emanating from the cylinder are
125 on the order of the wing span of the bees. While there exists limited understanding of the influence of
126 various scales of unsteady flow structures on flapping flight performance, we hypothesize that
127 disturbances on the order of the bee's wing span would produce greatest instability; disturbances many
128 orders of magnitude greater would be experienced as quasi-steady changes in oncoming flow, whereas
129 those many orders of magnitude smaller would average out across the body to produce minimal
130 disturbance.

131 We filmed bees and quantified airflow within a specific interrogation volume (a cube with side lengths of
132 100 mm, located 100 mm downstream from the cylinder; Fig. 1A). The downstream distance was chosen
133 to avoid the recirculating region in the near wake of the cylinder and to allow the formation of a full von
134 Karman vortex street. Fluctuations in flow velocity within this volume were quantified in the absence of
135 bees, using a three component hot-wire anemometer sampling at 1kHz, calibrated against a standard
136 pitot-static tube.

137 During flight trials, bees were filmed as they flew through the interrogation volume using two Photron
138 SA3 high-speed cameras sampling at 1000 Hz, placed above the wind tunnel at approximately 30° from
139 the vertical. A static calibration cube that filled the volume of interest was used for spatial calibration via
140 direct linear transformation (Hedrick, 2008).

141 Triangular markers were manually placed on the thorax of bees to enable estimation of bees' position
142 and orientation. The markers consisted of three black points representing the vertices of an isosceles
143 triangle (measuring 2.7 x 2.3 mm) set upon a white background (Fig. 2B). Footage of the bees in flight
144 revealed that the marker was well removed from the wings and did not interfere with wing kinematics.

145 ***Kinematic reconstruction and analysis***

146 The recorded flight sequences were digitized using an open-source MATLAB-based routine, DLTdv5
147 (Hedrick, 2008), utilizing the automated tracking feature to localize the three black points on the
148 triangular marker throughout each sequence. Subsequent analysis of the bee's position and orientation
149 was performed in MATLAB. Reconstructed data were filtered with an 8th-order Butterworth low pass
150 filter with a cutoff frequency of 200 Hz to reduce error due to marker localization (see Error Estimation,

151 below). The software utilizes Direct Linear Transformation (DLT) to calculate the location of an arbitrary
 152 point in 3D space based on the location of the point on each camera’s view. For all flight sequences only
 153 the three black points on the marker (Fig. 2B) were digitized.

154 Mean ground speed of bees was calculated by numerically integrating the absolute flight path of the bee
 155 and dividing it by the total flight time. Mean air speed of bees along their flight path was calculated as
 156 the sum of the mean wind speed in the interrogation volume and the mean ground speed traveled by
 157 the bee:

$$(\text{Mean air speed})_{Tot,x,y,w} = \frac{(\text{Total distance travelled})_{Tot,x,y,w}}{\text{Total time}} + (\text{Mean wind speed})_{Tot,x,y,w}$$

158
 159 In smooth flow conditions, the mean wind speed was uniform within the interrogation volume;
 160 however, in the wake of the cylinder, mean streamwise velocity varied slightly across the control volume
 161 (Fig. 1B). Because simultaneous measurement of the bee’s position and instantaneous wind speed at
 162 that particular position is impractical, we used the mean wind speed across the interrogation volume
 163 combined with the bee’s ground speed to estimate mean air speed in unsteady flow trials. This method
 164 of air speed estimation was considered reasonable because variation in mean wind speed across the
 165 interrogation volume was relatively limited, and the flight time of the bees was much greater than the
 166 advective time scales of the von Karman vortices.

167 To further elucidate the influence of unsteady flows on the bees’ flight trajectories, ground speeds of
 168 bees in the longitudinal, lateral and vertical directions (in a global coordinate system; Fig. 2B) were
 169 calculated separately and compared between flow conditions. For all flow conditions there was no mean
 170 wind in either the lateral or vertical direction, hence the lateral and vertical airspeeds were equal to
 171 their respective ground-speeds. Standard deviations of velocity along each axis in each trial were
 172 calculated to compare the relative strength of velocity fluctuations along each axis. Power spectra of
 173 bee velocity along each axis were calculated using the Welch method of spectral estimation in MATLAB,
 174 to identify dominant frequencies of motion. Because bumblebees typically adopt a “casting” flight path,
 175 flying slowly from side to side as they move upstream, we also examined the standard deviations of
 176 velocities subjected to a 3 Hz high-pass filter, to separate the higher frequency components of the bees’
 177 velocity fluctuations from the low-frequency casting behavior. The cutoff frequency of 3 Hz was chosen
 178 arbitrarily, based on the power spectra of bee velocity; however, sensitivity to cutoff frequency was

179 evaluated, and the filtered results were found to be relatively insensitive to cutoff frequency over a
180 range of ~ 3-10 Hz.

181 Instantaneous acceleration was calculated by numerically differentiating bee velocity. Power spectra of
182 accelerations along the longitudinal, lateral, and vertical axes were calculated to assess dominant
183 frequencies of acceleration fluctuations and standard deviations of accelerations were calculated to
184 compare the magnitude of fluctuations along the three axes.

185 The influence of flow conditions on the body orientation and rotation rates of bees was assessed by
186 evaluating variation in roll, pitch and yaw angles of the triangular markers, using a rigid body
187 assumption. As abdomen position was not tracked in the flight sequences, pitch angle estimation
188 through the conventional method (angle between head-abdomen vector and horizon) could not be
189 made; however, because most aerodynamic force is produced in the thorax and many insects are known
190 to actuate their abdomens independently during flight, we chose to use the orientation of the thorax
191 itself for pitch angle estimation. To calculate instantaneous orientation of the thorax, a local plane was
192 constructed based on the three points on the triangular marker. The origin of the right-handed local
193 coordinate system of the plane was placed on the posterior-most point on the marker and translational
194 components between the local and global coordinate systems were removed (see Fig. 2B). Subsequently
195 the directional cosine matrix (DCM; i.e., the rotation matrix between the local and global coordinate
196 systems) was calculated. From the DCM, the Euler angles based on the Roll-Pitch-Yaw (RPY) sequence of
197 intrinsic rotations was obtained (Diebel, 2006). Conceptually, the RPY angles derived from this method
198 imply that the instantaneous orientation of the marker (bee) with respect to the neutral position (where
199 the local and global coordinate systems are coincident), can be described by initially performing a
200 rotation about the local coordinate x-axis (roll), subsequently a rotation about the local coordinate y-
201 axis (pitch) and finally a rotation about the local coordinate z-axis (yaw). A similar method was used by
202 (Walker et al., 2012) and (Nicholas, 2012) to estimate the orientation of freely flying hoverflies and
203 houseflies, respectively.

204 Power spectra of orientation angles were calculated to identify dominant frequencies of fluctuations in
205 body rotation around the roll, pitch and yaw axes. To obtain instantaneous rotation rates of bees in the
206 local coordinate system, the time derivative of the RPY angles was multiplied by the rotation rate matrix
207 (Diebel, 2006). Mean absolute rotation rates were calculated from the instantaneous angular velocity
208 data. The rotation data was also treated with a 3 Hz high-pass filter to remove low-frequency casting
209 motions, as in the translational analyses described above.

210 To understand how body rotations (either voluntary or involuntary) are related to translational motions
211 of bees, we performed normalized cross-correlation analysis between instantaneous roll/yaw angles and
212 lateral acceleration, as well as between pitch angle and vertical/longitudinal accelerations.

213 Statistical significance of results was analyzed by performing paired *t*-tests ($n = 14$ individuals in all
214 cases) between experimental conditions (smooth flow [S], unsteady wake of horizontal cylinder [U_{horiz}],
215 and unsteady wake of vertical cylinder [U_{vert}]) in MATLAB.

216

217 ***Error estimation***

218 Digitization error in localizing the centroids of marker points is expected to be of the order of 1-2 pixels,
219 which is much smaller than the mean number of pixels separating the markers (~ 30). This error is
220 expected to manifest only at higher frequencies, on the order of the Nyquist frequency. The digitized
221 data were passed through an 8th order Butterworth low-pass filter to remove any higher frequency
222 errors due to the digitization process, with a cutoff frequency of 200 Hz, which is lower than the Nyquist
223 frequency (500 Hz) but higher than the flapping frequency of the bees (~ 180 Hz).

224 Error due to the 3D reconstruction process was analyzed using the DLTdv5 MATLAB routine, which
225 provides residuals (in pixels) from the direct linear transformation performed for each time instant
226 (Hedrick, 2008). These residuals are the root-mean-square error in the 3D reconstruction of the points
227 from the camera views, and may be considered a metric for the accuracy of the digitization process. A
228 low residual is indicative of accurate triangulation of the points in 3D space. To avoid errors in
229 estimation of orientation angles due to the relatively close proximity of points on the marker, only
230 sections of flight sequences with DLT residuals < 2 pixels were chosen for further analysis. To further
231 assess the accuracy of the reconstruction process, the reconstructed distances between marker points
232 were compared to the actual physical distances between them for each time instant analyzed. For the
233 flight sequences analyzed (those with DLT residuals < 2), the root mean square difference between
234 reconstructed and actual marker distances was < 0.05 mm, corresponding to an uncertainty of $< 2\%$.

235 Markers were affixed to each bee's thorax manually, and thus may have been offset from the bee's
236 neutral axes by different amounts in the 14 individuals tested. These offsets in marker positioning could
237 introduce error into the estimation of instantaneous body orientation angles. However, the output
238 variables used for statistical analysis (standard deviation of rotation angles, mean absolute rotation

239 rates, standard deviation of rotation rates, etc.) were based on changes in orientation angle, and thus
240 are not affected by slight errors in estimation of actual body orientation angles.

241

242 **RESULTS**

243 ***Flow conditions***

244 With unimpeded (smooth) flow, a flat velocity profile was present across the interrogation volume (< 2%
245 variation in mean flow speed, Fig. 1B) and turbulence intensity (standard deviation/mean wind speed)
246 was less than 1.2%. There were no dominant velocity fluctuations at any particular frequency (Fig. 1C-D),
247 indicating that the flow disturbance created by the small flower embedded in the upstream mesh was
248 minimal.

249 When either a horizontal or vertical cylinder was introduced to generate unsteady flow, a deficit in
250 mean longitudinal velocity could be seen in the wake of the cylinder (as compared to the smooth flow),
251 and the mean velocity profile varied slightly throughout the interrogation volume (Fig. 1B). Vortex
252 shedding occurred at 23 Hz (Fig. 1C-D), in agreement with the predicted vortex shedding Strouhal
253 number of 0.19 (Roshko, 1961; Vickery, 1966). When the cylinder was aligned vertically, strong lateral
254 velocity fluctuations were induced at the shedding rate (Figs. 1C), and when the cylinder was aligned
255 horizontally, strong vertical velocity fluctuations were induced (Fig. 1D). Due to the influence of the
256 counter-rotating vortices, velocity along the dominant axis of disturbance (i.e. lateral flow with the
257 vertical cylinder, vertical flow with the horizontal cylinder) varied approximately as a square wave.
258 Smaller velocity fluctuations in the non-dominant directions at 23 Hz can also be seen in the spectra
259 (Figs. 1C-D), indicating that some 3D effects were present; these may be attributed to ambient
260 freestream turbulence within the tunnel and small surface non-uniformities of the cylinder.

261

262 ***Flight speed and trajectory***

263 Mean air speed of bees along their flight trajectory was lower in unsteady flow as compared to smooth
264 flow conditions (Fig. 3; paired *t*-tests: $S-U_{\text{horiz}}$ & $S-U_{\text{vert}}$, $p \ll 0.0001$, where *S* is smooth flow, and U_{horiz} and
265 U_{vert} are unsteady flow behind the horizontal and vertical cylinder, respectively), but did not differ with
266 orientation of the cylinder ($U_{\text{horiz}}-U_{\text{vert}}$, $p = 0.55$). Similarly, longitudinal (upstream) air speed was lower in
267 unsteady flow than in smooth flow, but did not differ with flow orientation ($S-U_{\text{horiz}}$ & $S-U_{\text{vert}}$, $p \ll$

268 0.0001; $U_{\text{horiz}}-U_{\text{vert}}$, $p = 0.6533$). There were no significant differences in mean longitudinal and lateral
269 ground speed among flow conditions (Fig. 4A-B), but mean vertical ground speed was higher in the wake
270 of the horizontal cylinder as compared to the other two flow conditions (Fig. 4C; $S-U_{\text{horiz}}$, $p = 0.035$; $U_{\text{horiz}}-$
271 U_{vert} , $p = 0.04$; $S-U_{\text{vert}}$, $p = 0.75$).

272 Standard deviations of longitudinal, lateral and vertical velocity were similar across all three flow
273 conditions (Figs. 4G-I, solid boxes; $S-U_{\text{horiz}}$, $p = 0.5, 0.4$ & 0.4 for longitudinal, lateral and vertical
274 directions, respectively; $S-U_{\text{vert}}$, $p = 0.2, 0.8$ & 0.3 ; $U_{\text{horiz}}-U_{\text{vert}}$, $p = 0.8, 0.5$ & 0.9). However, the flight
275 trajectories of bees flying upstream in the wind tunnel consisted of motions over a range of frequencies.
276 Bees typically displayed high-amplitude, low-frequency casting movements while flying upstream; these
277 smooth, low-frequency motions were less pronounced in unsteady flows, where higher frequency
278 movements around the flight path were more common (Fig. 5). When the low-frequency casting
279 maneuvers were removed by a 3 Hz high-pass filter, the standard deviation of lateral velocity differed
280 significantly between flow conditions, with larger lateral velocity fluctuations in both unsteady flow
281 conditions as compared to smooth flow (Fig. 4H, open boxes; $S-U_{\text{horiz}}$, $p = 0.02$; $S-U_{\text{vert}}$, $p < 0.001$; $U_{\text{horiz}}-$
282 U_{vert} , $p = 0.002$), and the highest lateral fluctuations generated by the vertical cylinder. Standard
283 deviations of filtered longitudinal and vertical velocity data remained similar across flow conditions.

284 These large fluctuations in lateral velocity at higher frequencies were also manifested as large
285 fluctuations in lateral acceleration under unsteady flow conditions, with the standard deviation of lateral
286 accelerations being highest in the wake of the vertical cylinder (Fig. 6B; $S-U_{\text{horiz}}$, $p < 0.001$; $S-U_{\text{vert}}$, $p <$
287 0.001 ; $U_{\text{horiz}}-U_{\text{vert}}$, $p < 0.001$). Vertical acceleration fluctuations were generally lower than lateral ones,
288 but the standard deviation of vertical accelerations was significantly higher in unsteady flow generated
289 by the horizontal cylinder than in the other two flow conditions (Fig. 6C; $S-U_{\text{horiz}}$, $p = 0.006$; $S-U_{\text{vert}}$, $p =$
290 0.20 ; $U_{\text{horiz}}-U_{\text{vert}}$, $p = 0.03$). Acceleration fluctuations in the longitudinal direction were relatively low,
291 with significantly higher fluctuations in the wake of the vertical cylinder as compared to smooth flow
292 (Fig. 6A; $S-U_{\text{horiz}}$, $p = 0.36$; $S-U_{\text{vert}}$, $p = 0.01$; $U_{\text{horiz}}-U_{\text{vert}}$, $p = 0.09$)

293 Spectral analysis revealed peaks in body acceleration near the vortex shedding frequency in both
294 unsteady flow conditions (Figs. 6D-F), similar to the velocity spectra (Figs. 4D-F). However, whereas
295 velocity fluctuations occurred primarily along either the lateral or vertical axis, depending on the
296 orientation of unsteady flow (Figs. 4D-F), acceleration fluctuations near the shedding frequency
297 occurred along all three axes in both unsteady flow conditions (Figs. 6D-F).

298

299 **Body Orientation**

300 As seen previously in standard deviations of bees' velocities (Figs. 4G-I), the standard deviations of bees'
301 orientation angles were also affected by the low frequency casting maneuvers that bees performed
302 while flying upwind (Fig. 5), leading to similar magnitude of roll and yaw fluctuations in the three flow
303 conditions (Fig. 7A-C, solid boxes; $S-U_{\text{horiz}}$, $p = 0.2$ & 0.4 for roll and yaw, respectively; $S-U_{\text{vert}}$, $p = 0.8$ &
304 0.8 ; $U_{\text{horiz}}-U_{\text{vert}}$, $p = 0.2$ & 0.4). The pitch angle fluctuations were higher in both unsteady flow conditions
305 as compared to smooth flow (Fig. 7B, solid boxes (significance bars not shown); $S-U_{\text{horiz}}$, $p = 0.04$ $S-U_{\text{vert}}$, p
306 $= 0.01$ $U_{\text{horiz}}-U_{\text{vert}}$, $p = 0.5$). However, when low frequency casting motions are removed with a 3 Hz high-
307 pass filter, it becomes clear that bees experience significantly more high-frequency roll fluctuations in
308 both unsteady flow conditions, as compared to smooth flow (Fig. 7A, open boxes; $S-U_{\text{horiz}}$, $p \ll 0.0001$; $S-$
309 U_{vert} , $p \ll 0.0001$; $U_{\text{horiz}}-U_{\text{vert}}$, $p = 0.1$). Differences in pitch and yaw fluctuations were also significant
310 between unsteady and smooth flow conditions (Figs. 7B-C; $S-U_{\text{horiz}}$, $p = 0.001$ & 0.002 ; $S-U_{\text{vert}}$, $p = 0.007$ &
311 0.02), but not among unsteady flow conditions (Figs 7B-C; $U_{\text{horiz}}-U_{\text{vert}}$, $p = 0.4$ & 0.5).

312 Distinct peaks in roll fluctuations (as well as lesser peaks in yaw and pitch) near the vortex shedding
313 frequency were present in the wake of the vertical cylinder (Fig. 7D-F), demonstrating that this unsteady
314 flow pattern destabilized bees, particularly around the roll axis. Surprisingly, no clear peaks in pitching or
315 other body rotations were present in the wake of the horizontal cylinder (Fig. 7D-F), despite the
316 presence of peaks in the vertical air speed of bees (Fig. 4D-F). Spectra of rotation rates (not shown) were
317 similar to those of the orientation angles themselves.

318 Variations in mean (absolute) rotation rates indicated that much higher rotation rates occurred around
319 the rolling axis as compared to pitch or yaw in all three flow conditions (Fig. 8A-C). Mean rolling rates in
320 excess of 500 degrees/sec were commonly experienced by the bees in unsteady conditions. Rolling rates
321 were significantly higher in both unsteady flow conditions as compared to smooth flow, and were higher
322 behind the vertical cylinder as compared to the horizontal one (Fig. 8A; $S-U_{\text{horiz}}$, $p \ll 0.0001$, $S-U_{\text{vert}}$, $p \ll$
323 0.0001 ; $U_{\text{horiz}}-U_{\text{vert}}$, $p = 0.003$). Pitching rates were much lower than rolling rates, but bees pitched more
324 quickly in unsteady as compared to smooth flow (Fig. 8B; $S-U_{\text{horiz}}$, $p = 0.001$, $S-U_{\text{vert}}$, $p = 0.0001$, $U_{\text{horiz}}-$
325 U_{vert} , $p = 0.7$), and yawing rates were the lowest, but still significantly higher in unsteady flow ($S-U_{\text{horiz}}$, p
326 $= 0.004$, $S-U_{\text{vert}}$, $p = 0.0002$, $U_{\text{horiz}}-U_{\text{vert}}$, $p = 0.2$). The standard deviation of rotation rates (Fig. 8D-F) was
327 generally higher than the absolute mean, but variations between smooth and unsteady conditions were

328 similar, with all flow conditions producing the largest fluctuations around the roll axis, followed by pitch
329 and yaw.

330

331 ***Relationships between body orientation and translational acceleration***

332 The kinematic analyses revealed a strong cross-correlation (with zero phase lag) between roll angle and
333 acceleration along the lateral axis of the wind tunnel for bees in smooth flow ($r = 0.7 \pm 0.2$, $n = 14$ bees;
334 Fig. 9A-B), whereas there was no clear correlation between yaw angle and lateral acceleration ($r = 0.3 \pm$
335 0.3). As expected for voluntary maneuvers (in which a body rotation redirects the axis of force
336 production, leading to translation), the correlation between roll angle and lateral acceleration in smooth
337 flow was positive, with the largest lateral accelerations coinciding with the largest roll angles (Fig. 9A).

338 In contrast, there was no substantial correlation between roll angle and lateral acceleration during trials
339 conducted in unsteady flow generated by the vertical cylinder (Fig. 9B). However, when the data was
340 filtered with a 3 Hz low-pass filter to remove higher frequency motions (in contrast to previous filtering
341 that excluded low frequency motions), the correlation between roll angle and lateral acceleration again
342 became positive and significant (Fig. 9C; $r = 0.7 \pm 0.15$). The same pattern was generally true for flight in
343 unsteady flow generated by the horizontal cylinder (unfiltered: $r = 0.2 \pm 0.3$; filtered: $r = 0.6 \pm 0.2$).

344 The correlation between pitch angle and vertical acceleration was relatively low but positive in smooth
345 flow ($r = 0.2 \pm 0.2$). In unsteady flow, there was no clear correlation between pitch angle and vertical
346 acceleration (horizontal cylinder: $r = 0.1 \pm 0.5$; vertical cylinder: $r = 0.0 \pm 0.2$), and filtering with a 3 Hz
347 low-pass filter did not significantly alter this relationship (horizontal cylinder: $r = 0.0 \pm 0.3$; vertical
348 cylinder: $r = 0.3 \pm 0.4$).

349

350 **DISCUSSION**

351 ***Effects of unsteady flow on flight trajectory and stability***

352 In the broader context of insect flight in natural environments, one of the key questions is how well
353 bumblebees are able to contend with unsteady airflow; ultimately, we would like to know how bees'
354 capabilities compare both to other flying insects, as well as to the magnitude of unsteady flows that
355 bees experience in the real world. As compared to the null hypothesis that bees would display

356 translational and rotational fluctuations equal to those present in the external flow (i.e. if they were
357 massless and had no active or passive control of their position or orientation), it is clear that bees are
358 quite successful overall at attenuating external flow perturbations (Table 1; note that for the unsteady
359 flow conditions, only fluctuations at frequencies > 3 Hz were considered, in order to remove the effects
360 of voluntary casting behavior). Bees typically displayed fluctuations (i.e., standard deviations) in
361 translational velocity and acceleration that were at least an order of magnitude less than those present
362 in the external flow, and showed similar levels of attenuation in pitch and yaw angles.

363 Some attenuation of the fluctuations induced by the flow is expected because the bee's mass (inertia)
364 will passively reduce the magnitude of fluctuations experienced by the bee. However, bees are
365 undoubtedly also responding actively to minimize and correct for external perturbations through
366 changes in wing kinematics, as has been shown in honeybees and other flying insects responding to
367 isolated external perturbations (Vance et al., 2013; Ristroph et al., 2010). Active responses of the bees
368 could not be determined in this study due to the lack of information on wing kinematics. Even with this
369 information, it would be difficult to conclusively identify the extent of active response, due to the tight
370 coupling between disturbance and response, as well as the complex spatial and temporal variation in
371 external flows. The rapid drop-off in energy of acceleration fluctuations at frequencies higher than the
372 vortex shedding rate (Fig. 6) suggests that the bees did not respond to disturbances induced by the
373 vortices with rapid corrective accelerations, but rather responded at rates commensurate with the
374 disturbances.

375 While bees can clearly attenuate external perturbations along all axes (Table 1), they appear to be less
376 sensitive (i.e., more stable) to perturbations along the vertical axis, as opposed to the lateral axis.
377 Fluctuations in vertical acceleration in response to the horizontal cylinder were approximately half the
378 magnitude of fluctuations in lateral acceleration in response to the vertical cylinder (Fig. 6), and the
379 energy present at the vortex shedding frequency in the spectra is significantly higher in the latter. This
380 could imply that bees are more aerodynamically stable along the vertical axis and/or that they are more
381 adept at actively responding to translational disturbances along this axis. However, the lower magnitude
382 of fluctuations in pitch as compared to roll under all flow conditions (Fig. 8) suggests that bees may be
383 "passively" more immune to disturbances along the vertical/pitching axis. In addition, the presence of a
384 peak in vertical ground speed fluctuations near the vortex shedding frequency in the wake of a
385 horizontal cylinder, but the absence of a peak in pitching, suggests that the von Karman street arising
386 from the horizontal cylinder resulted only in translational perturbations along the vertical axis, and did

387 not cause any rotational disturbances or elicit rotational responses in bees at the vortex shedding
388 frequency.

389 Apart from the passive attenuation of disturbances by virtue of body mass (inertia) and other damping
390 phenomena (e.g. translational damping by virtue of flapping kinematics, and rotational damping due to
391 flapping counter torque; Hedrick, 2011), as well as active responses in the form of wing kinematic
392 modulation, bumblebees likely employ a variety of other active and passive means to resist
393 perturbations and maintain stability in unsteady flows. Active deflection of various body parts has been
394 shown to influence stability, such as in orchid bees that extend their limbs when flying in turbulent air to
395 increase their rolling moment of inertia (Combes and Dudley, 2009). Other studies have shown that
396 abdominal deflection may augment not only pitching stability, but also translational stability along the
397 vertical axis (Dyhr et al., 2013). Though no obvious leg extension occurred in the flight sequences
398 collected for this study, some abdominal deflection was noted qualitatively, which could contribute to
399 the bees' stability along the vertical/pitching axis.

400 The relatively limited sensitivity to disturbances along both the vertical and longitudinal axes in
401 comparison to the lateral axis could also arise from the fact that forces are actively produced by the bee
402 along these axes (lift and thrust, respectively). In steady level flight, as the bee counteracts its drag by
403 generating thrust (longitudinal axis) and counteracts its weight by generating lift (vertical axis), a
404 disturbance along these axes will only require a slight modulation of the existing forces to correct for the
405 influence of the disturbance. However, a disturbance along the lateral axis would be expected to have a
406 greater influence, since no (or very limited) forces are being produced along this axis, unless the bee is
407 performing a turning maneuver. Hence, in the case of a lateral disturbance, the bee would need to
408 correct for the disturbance through inertial reorientation (roll) of its primary force vector.

409 In addition to inherent differences in force production, the rotational moment of inertia of the bee also
410 varies about its three axes. The rotational moment of inertia is generally lowest around the roll axis,
411 followed by the pitch and yaw axes (Dudley, 2002), and the differences in rotational fluctuations that
412 bees experienced around these axes in unsteady flow follow this trend. Bees rolled far more than they
413 pitched or yawed in all flow conditions, and unsteady flow amplified these trends (Fig. 7-8). Bees also
414 experienced significantly greater fluctuations in velocity and acceleration along the lateral axis (Figs 4, 6)
415 with external flow perturbations generated by the vertical cylinder imposing lateral forces of over half
416 the bees' body weight (Fig. 6B). Intriguingly, our results vary substantially from parallel experiments on
417 the flight stability of hawkmoths (*Manduca sexta*) (Ortega-Jimenez *et al* in review), which experienced

418 greater fluctuations in yaw than in roll when flying in the wake of a vertical cylinder. It is possible that
419 the differences in observations are due to experimental conditions; bees in our experiment were
420 actively flying upsteam to a food source, whereas hawkmoths were maintaining stationary position at a
421 flower in an oncoming flow. The observed differences may also reflect differences in passive stability or
422 flight control strategy, since these species vary significantly in morphology, wing loading and flapping
423 frequency (Ellington, 1984).

424 The spectral and temporal analysis of the flight trajectories allowed us to discern that bees typically
425 perform voluntary, lateral casting motions at low frequencies (Fig. 5), and that they primarily utilize the
426 roll axis to perform these lateral maneuvers. Thus, although bees may be more sensitive to disturbances
427 along the lateral/roll axis, they also appear to be most agile around this axis. Bees may make use of the
428 relative ease of perturbing stable flight (i.e., for a given amount of torque, a larger roll can be produced
429 as compared to pitch or yaw) to effect voluntary maneuvers. Similarly, in unsteady flow we would
430 expect that, although bees experience the largest translational perturbations around the lateral axis,
431 they would also be capable of responding most quickly and easily by producing a corrective roll in the
432 opposite direction. This may help explain the relatively low, negative correlation observed between roll
433 and lateral acceleration over the entire frequency range (Fig. 9C); this likely reflects a combination of
434 low frequency, voluntary casting maneuvers (with positive correlation; Fig. 9C), external perturbations
435 producing lateral acceleration and roll in the same direction (positive correlation), and corrective
436 maneuvers consisting of rolls in the opposite direction (negative correlation).

437 The lack of a strong correlation between yaw angle and lateral acceleration further reinforces the idea
438 that bees primarily utilize the roll axis for lateral maneuvers (voluntary or corrective). In terms of
439 vertical maneuvers, the low, positive correlation between pitch and vertical acceleration suggest that
440 bees only partially utilize inertial reorientation (i.e. pitch) to regulate vertical motion, and likely also
441 employ other mechanisms, such as altering the magnitude of mean force production through changes in
442 wing kinematics.

443

444 ***Effects of unsteady flow on energetics and cost of flight***

445 One strategy that fish have been shown to adopt for maintaining position and conserving energy in
446 unsteady flows is known as Karman gaiting (Liao et al., 2003). The passive and active compliance of the
447 body to oncoming vortices results in a swaying-undulating motion that enables fish to maintain stable

448 position with minimal energetic cost in highly unsteady flow conditions (Liao, 2007). The large
449 differences in morphology and force production mechanisms between laterally undulating fish and
450 flying bees suggests that the interaction of these animals with the oncoming vortices would be
451 considerably different; hence strategies employed by fish may not be suitable (or even feasible) for
452 bees. There is however a possibility that bees could actively slalom around oncoming vortices, thereby
453 reducing their energy expenditure. However, this cannot be ascertained in the absence of information
454 regarding the instantaneous position of the vortex with respect to the bee, for which additional
455 experiments combining simultaneous quantitative flow visualization and bee flight path measurements
456 would be required.

457 Assuming nominally similar mean power output in smooth and unsteady flow, the differences in the
458 bees' mean air speed along their flight paths suggests that it would take longer to travel a given distance
459 in unsteady flows (increasing the cost of transport). Though the reduction in mean air speed between
460 smooth and unsteady flow was only ~8%, this difference was consistent between individuals and
461 statistically significant. However, further experiments assessing the flight speeds and metabolic power
462 of bees flying through various intensities and scales of unsteady flow are needed to elucidate the
463 energetic implications of flying in complex aerial environments. If unsteady air flow in the ABL increases
464 energetic costs and/or reduces the mean flight speed of bees, this could have direct implications for the
465 foraging efficiency of bees in natural environments, particularly in windy weather - with potentially
466 adverse effects on colony energetics, growth and pollination efficiency.

467 Previous work has shown that that fully mixed, turbulent flows have a significant and adverse effect on
468 the flight of orchid bees (Combes and Dudley, 2009). Here, we show that insect flight is also adversely
469 affected by structured, unsteady flows (von Karman vortex streets) emanating from objects. Most
470 interestingly, our results indicate that the orientation of flow structures (vertically *versus* horizontally
471 aligned vortices) has relatively little effect on how instabilities are manifest in flying bees. Our
472 expectation was that a horizontally oriented cylinder (creating a vertical perturbation) would induce
473 variation in pitch angle, whereas a vertically oriented cylinder (creating a lateral perturbation) would
474 induce variation in yaw angle. However, our results clearly demonstrate that in both unsteady flow
475 conditions, bees are most unstable about the lateral/roll axis, and that bees make use of this instability
476 to effect voluntary and corrective maneuvers about this axis as well.

477

478 **REFERENCES**

- 479 **Beal, D. N., Hover, F. S., Triantafyllou, M. S., Liao, J. C. and Lauder, G. V** (2006). Passive propulsion in
480 vortex wakes. *Journal of Fluid Mechanics* **549**, 385–402.
- 481 **Chapman, J. W., Drake, V. A. and Reynolds, D. R.** (2011). Recent insights from radar studies of insect
482 flight. *Annual review of entomology* **56**, 337–56.
- 483 **Crall, J. and Combes, S.** (2013). Blown in the wind: Bumblebee temporal foraging patterns in naturally
484 varying wind conditions. In *Integrative and Comparative Biology*, p. E270. OXFORD UNIV. PRESS
485 INC.
- 486 **Dickinson, M. H., Lehmann, F. O. and Sane, S. P.** (1999). Wing Rotation and the Aerodynamic Basis of
487 Insect Flight. *Science* **284**, 1954–1960.
- 488 **Diebel, J.** (2006). *Representing attitude: Euler angles, unit quaternions, and rotation vectors*. Stanford,
489 California 94301-9010.
- 490 **Drake, V. A. and Farrow, R. A.** (1988). The Influence of Atmospheric Structure and Motions on Insect
491 Migration. *Annual Review of Entomology* **33**, 183–210.
- 492 **Dudley, R.** (2002). *The Biomechanics of Insect Flight: Form, Function, Evolution*. Princeton University
493 Press.
- 494 **Dudley, R. and Ellington, C. P.** (1990). Mechanics of forward flight in bumblebees: I. Kinematics and
495 morphology. *Journal of Experimental Biology* **148**, 19–52.
- 496 **Dyhr, J. P., Morgansen, K. A., Daniel, T. L. and Cowan, N. J.** (2013). Flexible strategies for flight control:
497 an active role for the abdomen. *Journal of Experimental Biology* **216**, 1523–1536.
- 498 **Ellington, C. P.** (1984). The Aerodynamics of Hovering Insect Flight. II. Morphological Parameters.
499 *Philosophical Transactions of the Royal Society B: Biological Sciences* **305**, 17–40.
- 500 **Ellington, C. P.** (1991). Limitations on animal flight performance. *Journal of Experimental Biology* **160**,
501 71–91.
- 502 **Ellington, C. P., Van den Berg, C., Willmott, A. P. and Thomas, A. L. R.** (1996). Leading-edge vortices in
503 insect flight. *Nature* **384**, 626–630.
- 504 **Feltwell, J.** (1982). *Large White Butterfly: The Biology, Biochemistry, and Physiology of Pieris Brassicae*
505 (*Linnaeus*). Dr. W. Junk Publishers.
- 506 **Heinrich, B.** (2004). *Bumblebee economics*. Harvard University Press.
- 507 **Hendry, G.** (1989). *Midges in Scotland*. Mercat Press.

- 508 **Liao, J. C.** (2007). A review of fish swimming mechanics and behaviour in altered flows. *Philosophical*
509 *transactions of the Royal Society of London. Series B, Biological sciences* **362**, 1973–93.
- 510 **Liao, J. C., Beal, D. N., Lauder, G. V and Triantafyllou, M. S.** (2003). Fish exploiting vortices decrease
511 muscle activity. *Science (New York, N.Y.)* **302**, 1566–9.
- 512 **Miller, L. A. and Peskin, C. S.** (2009). Flexible clap and fling in tiny insect flight. *The Journal of*
513 *experimental biology* **212**, 3076–90.
- 514 **Nicholas, I. K.** (2012). Automated Kinematic Extraction of Wing and Body Motions of Free Flying Diptera.
- 515 **Roshko, A.** (1961). Experiments on the flow past a circular cylinder at very high Reynolds number.
516 *Journal of Fluid Mechanics* **10**, 345.
- 517 **Sane, S. P.** (2003). The aerodynamics of insect flight. *Journal of Experimental Biology* **206**, 4191–4208.
- 518 **Stull, R. B.** (1988). *An Introduction to Boundary Layer Meteorology*. Springer.
- 519 **Vickery, B. J.** (1966). Fluctuating lift and drag on a long cylinder of square cross-section in a smooth and
520 in a turbulent stream. *Journal of Fluid Mechanics* **25**, 481.
- 521 **Walker, S. M., Thomas, A. L. R. and Taylor, G. K.** (2012). Operation of the alula as an indicator of gear
522 change in hoverflies. *Journal of the Royal Society, Interface / the Royal Society* **9**, 1194–207.
- 523 **Wang, Z. ~J.** (2005). Dissecting Insect Flight. *Annual Review of Fluid Mechanics* **37**, 183–210.
- 524 **Watkins, S., Milbank, J., Loxton, B. J. and Melbourne, W. H.** (2006). Atmospheric Winds and Their
525 Implications for Microair Vehicles. *AIAA Journal* **44**, 2591–2600.
- 526 **Willmott, A. P. and Ellington, C. P.** (1997). The mechanics of flight in the hawkmoth *Manduca sexta*. I.
527 Kinematics of hovering and forward flight. *Journal of Experimental Biology* **200**, 2705–2722.

528

529 **Author contributions**

530 The experiments were performed by S.R. & J.C. Analysis of results and writing of the
531 manuscript was performed by all authors.

532 **Author competing interests**

533 The authors declare no competing financial interests.

534

535 **Acknowledgements**

536 This work was supported by an NSF Expeditions in Computing grant to S.C. (CCF-0926158).
537

538

539

540

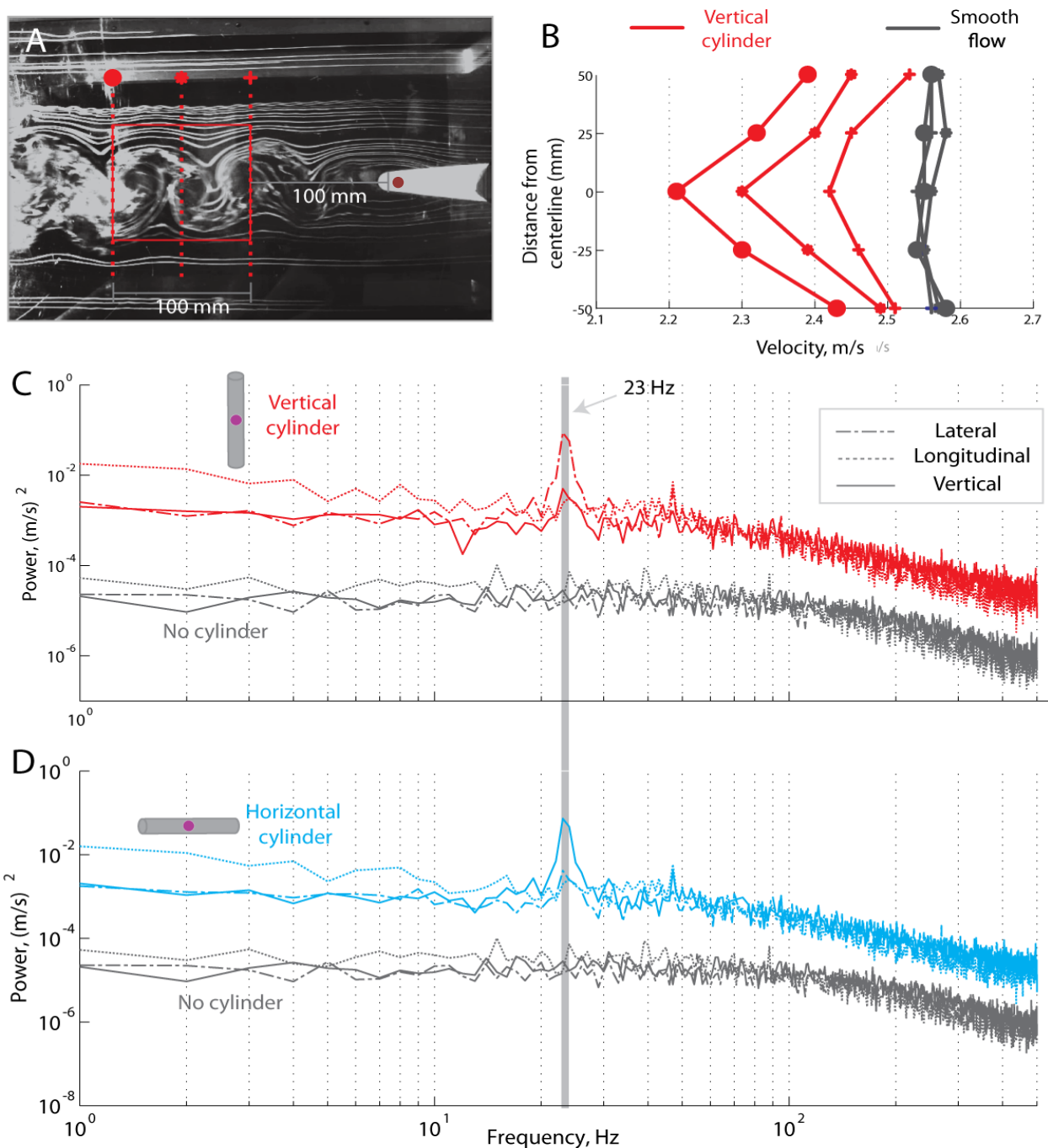
541

542

543

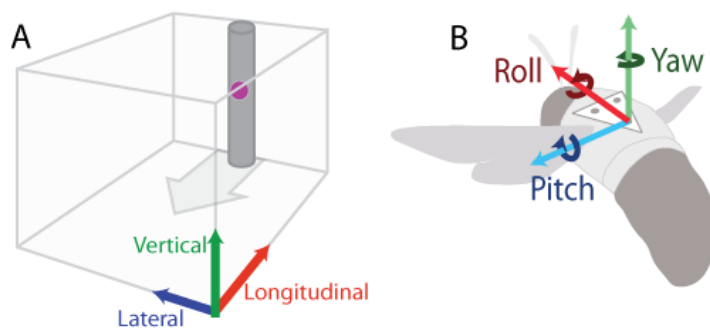
544

545 **Figures**

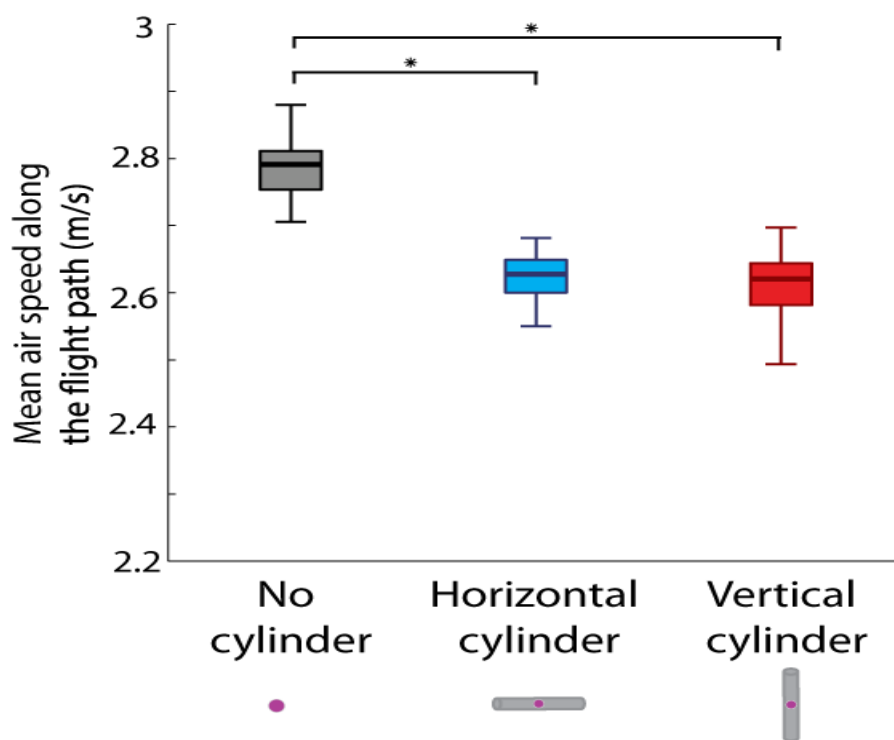


546

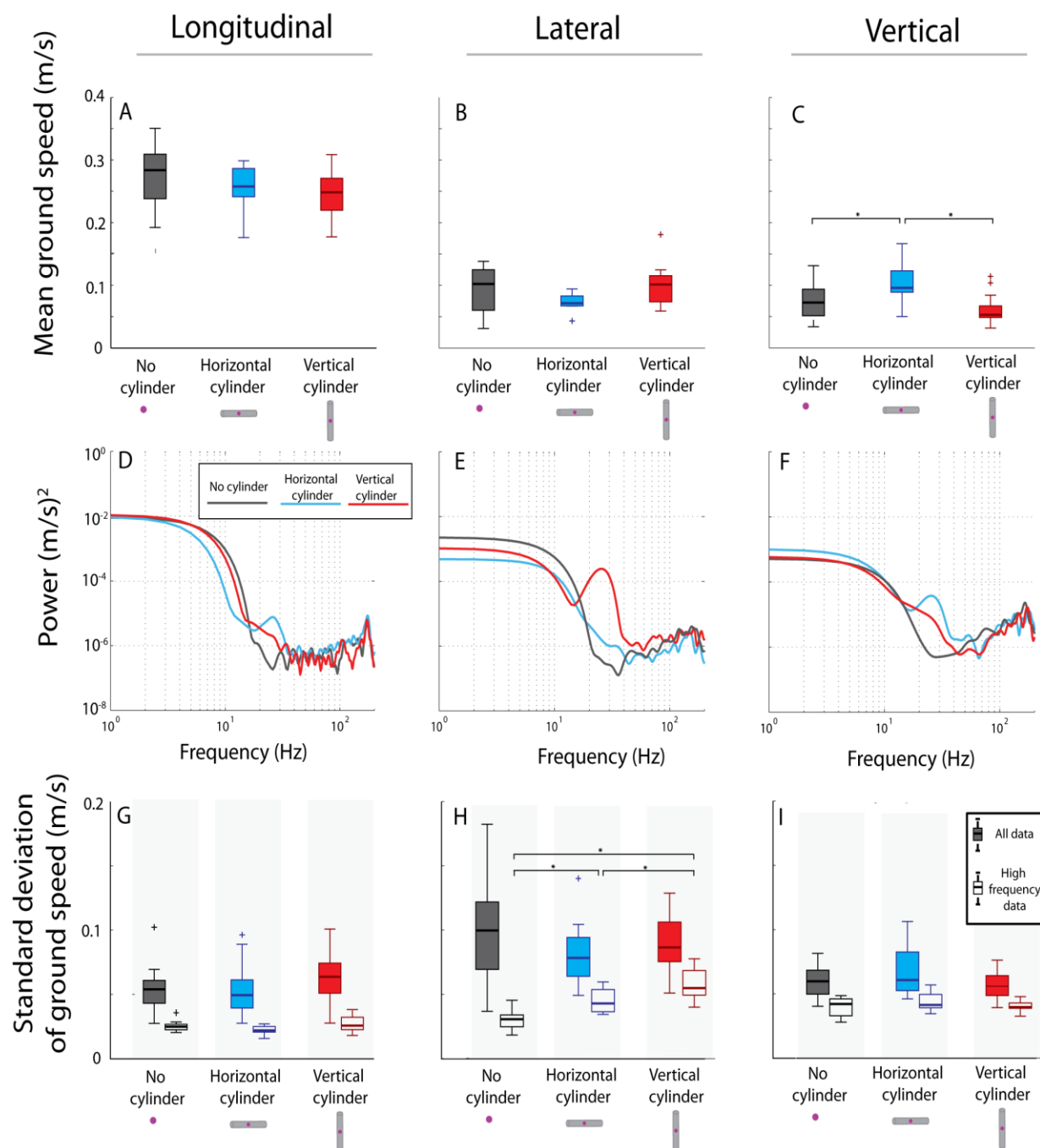
547 Figure 1: (A) Smoke flow visualization showing the von Karman vortex street in the wake of the vertical
 548 cylinder. Position and orientation of bees was measured within a cube of 100 mm side length, the
 549 location of which is depicted by the red square. The purple marker seen in the center of the cylinder
 550 represents the artificial flower. (B) Mean wind velocity measured at different locations within the 100
 551 mm cube (locations shown by symbols in A). (C & D) Spectra of velocity fluctuations measured along the
 552 three axes in the wake of the vertical and horizontal cylinder, respectively, as well as with no cylinder
 553 present.



554
 555 Figure 2: (A) Global coordinate system used for measurements of the position of bees. (B) Local
 556 coordinate system used for measurements of body orientation of bees.
 557



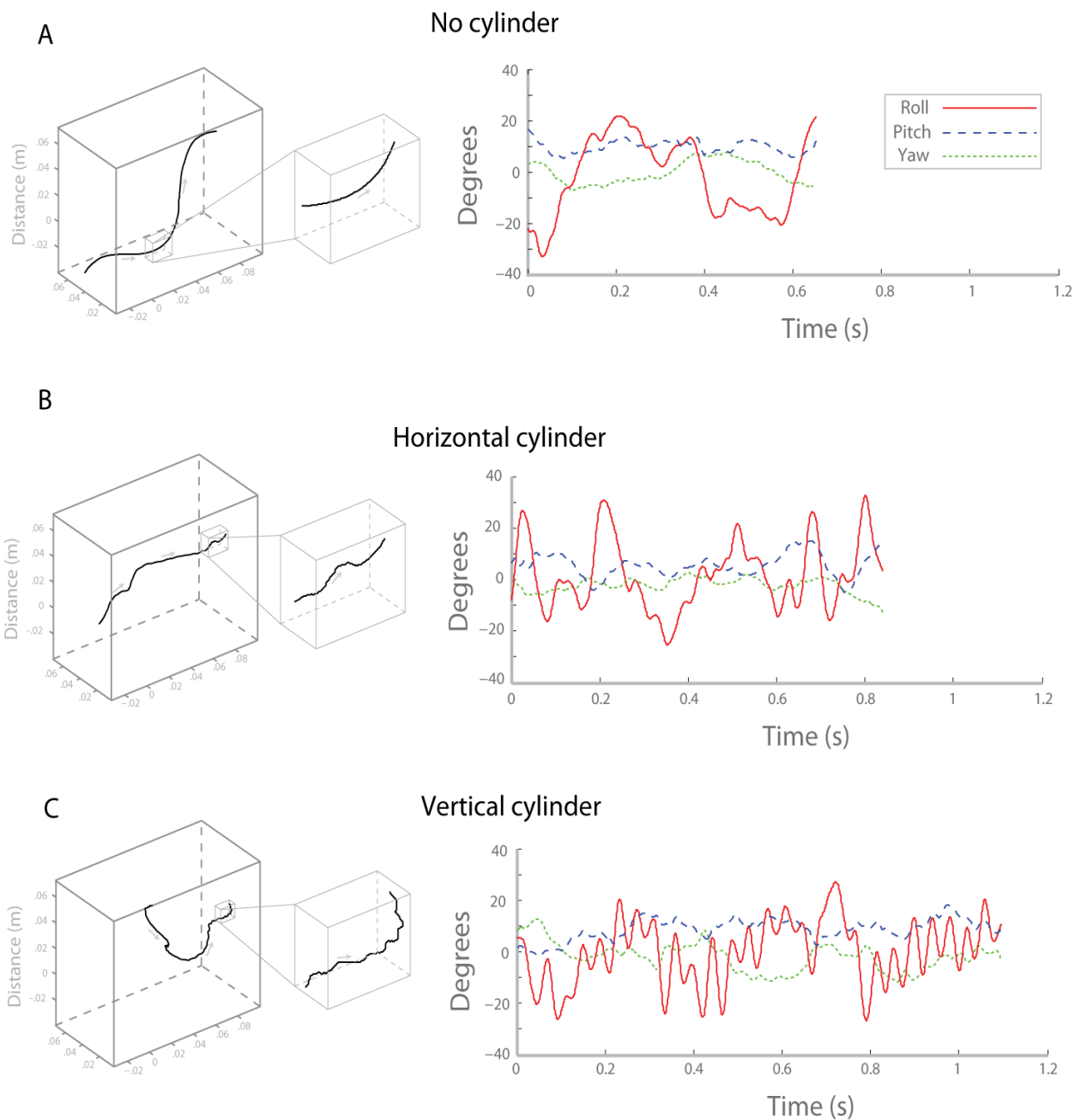
558
 559 Figure 3: Mean air speed of bees ($n = 14$) along their flight trajectories in the three flow conditions



560

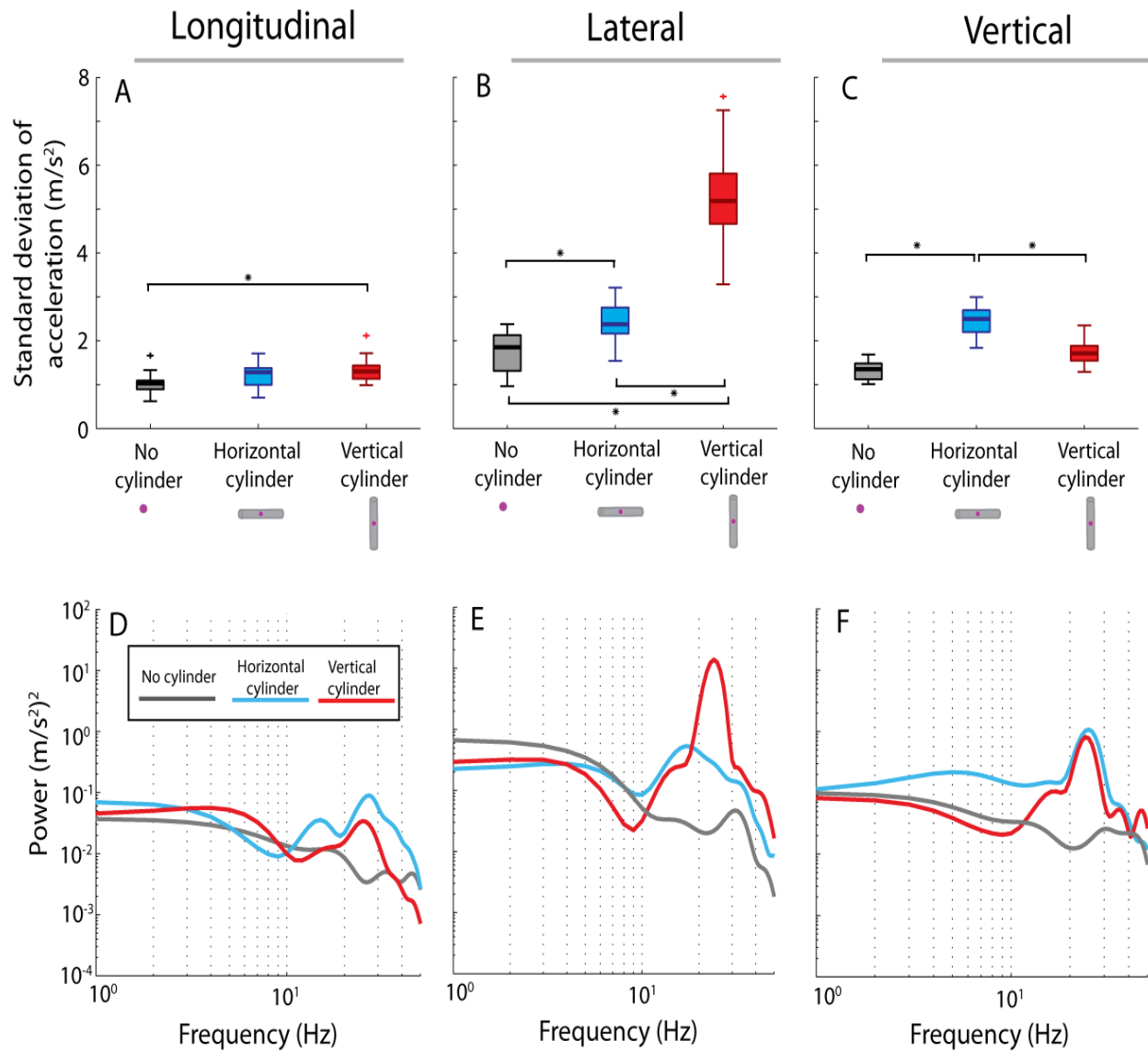
561 Figure 4: (A-C) Mean ground speed of bees ($n = 14$) along the longitudinal, lateral and vertical axes of the
 562 wind tunnel in the three flow conditions. For (B & C), mean lateral and vertical ground speed was equal
 563 to the mean air speed along those axes. (D-F) Power spectral density of an individual bee's velocity along
 564 each axis in the different flow conditions. (G-I) Standard deviation of the bees' velocities along each axis;
 565 data for full flight trajectories are shown by solid boxes, and those derived from only higher frequency
 566 motions (3 Hz high-pass filtered data) by open boxes.

567



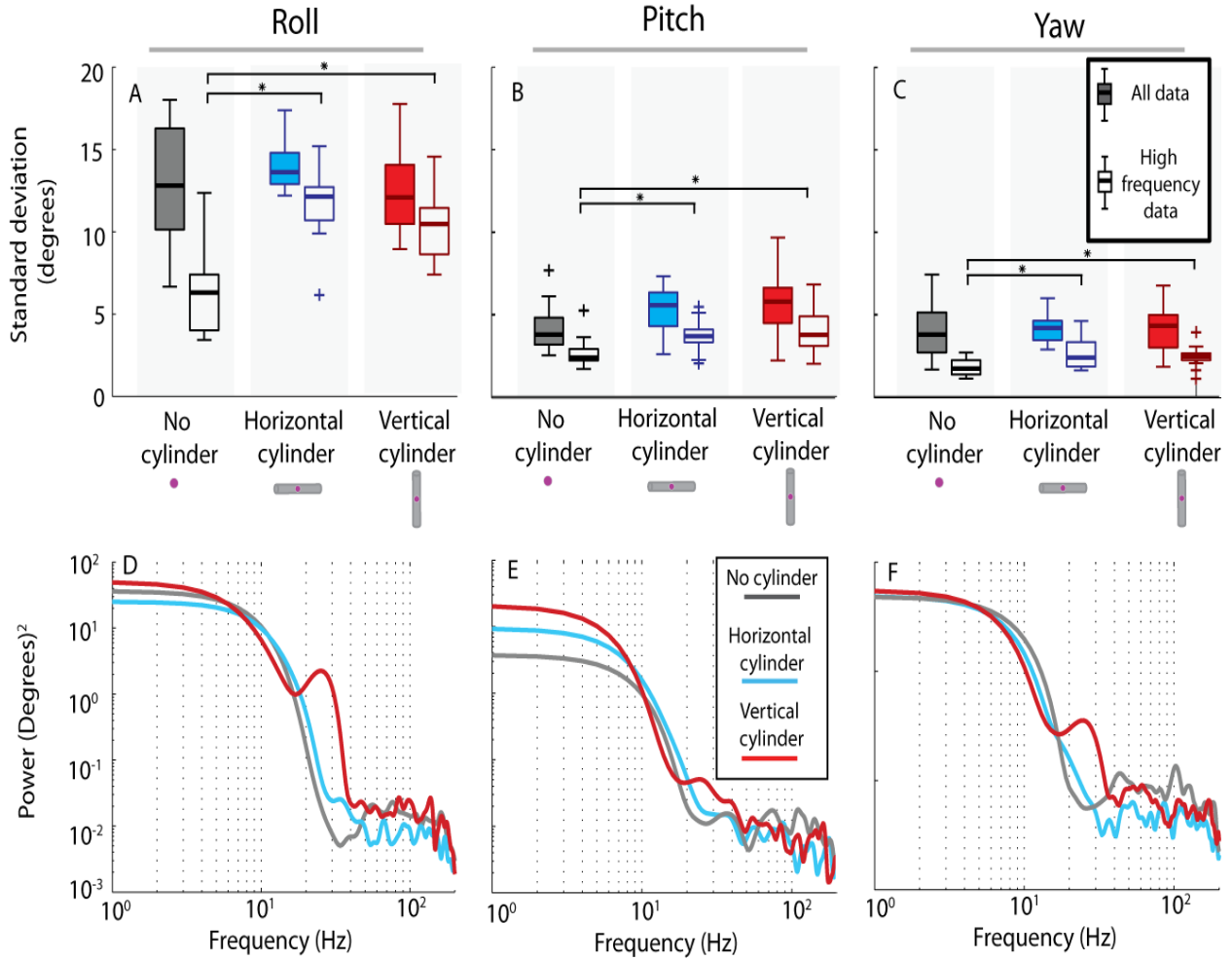
568

569 Figure 5: (A-C) Typical flight trajectories and body orientations of a bee in each flow condition. 3-d
 570 trajectory (in cm) within the wind tunnel is shown on the left, with movements within the interrogation
 571 volume shown by the inset. Instantaneous roll, pitch and yaw while flying through the interrogation
 572 volume is shown on the right.



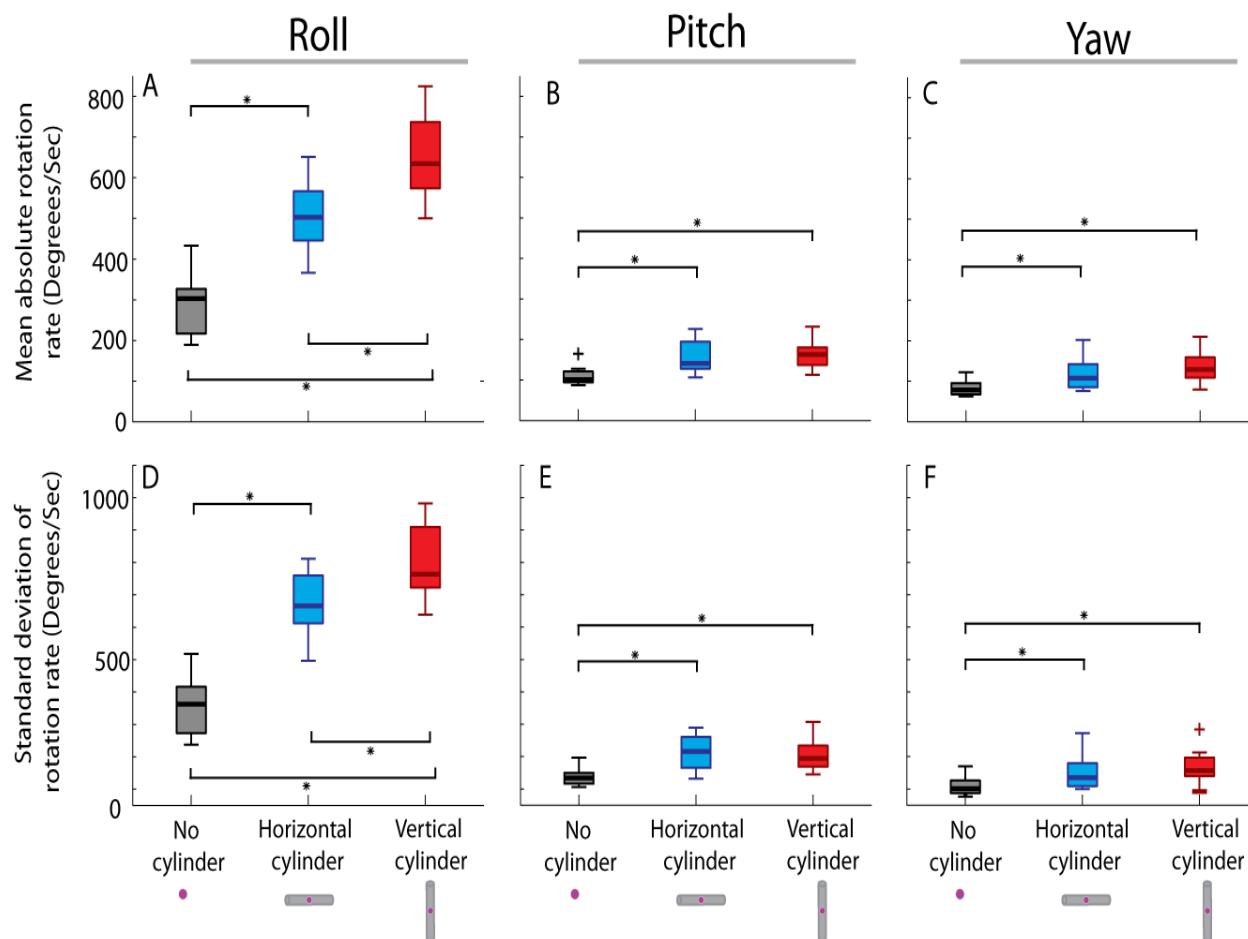
573

574 Figure 6: (A-C) Standard deviation of bees' accelerations along the longitudinal, lateral and vertical axes
 575 of the wind tunnel in the three flow conditions. (D-F) Power spectral density of an individual bee's
 576 acceleration along each axis in the different flow conditions. For analysis of accelerations, data was
 577 passed through a 50Hz low-pass filter.



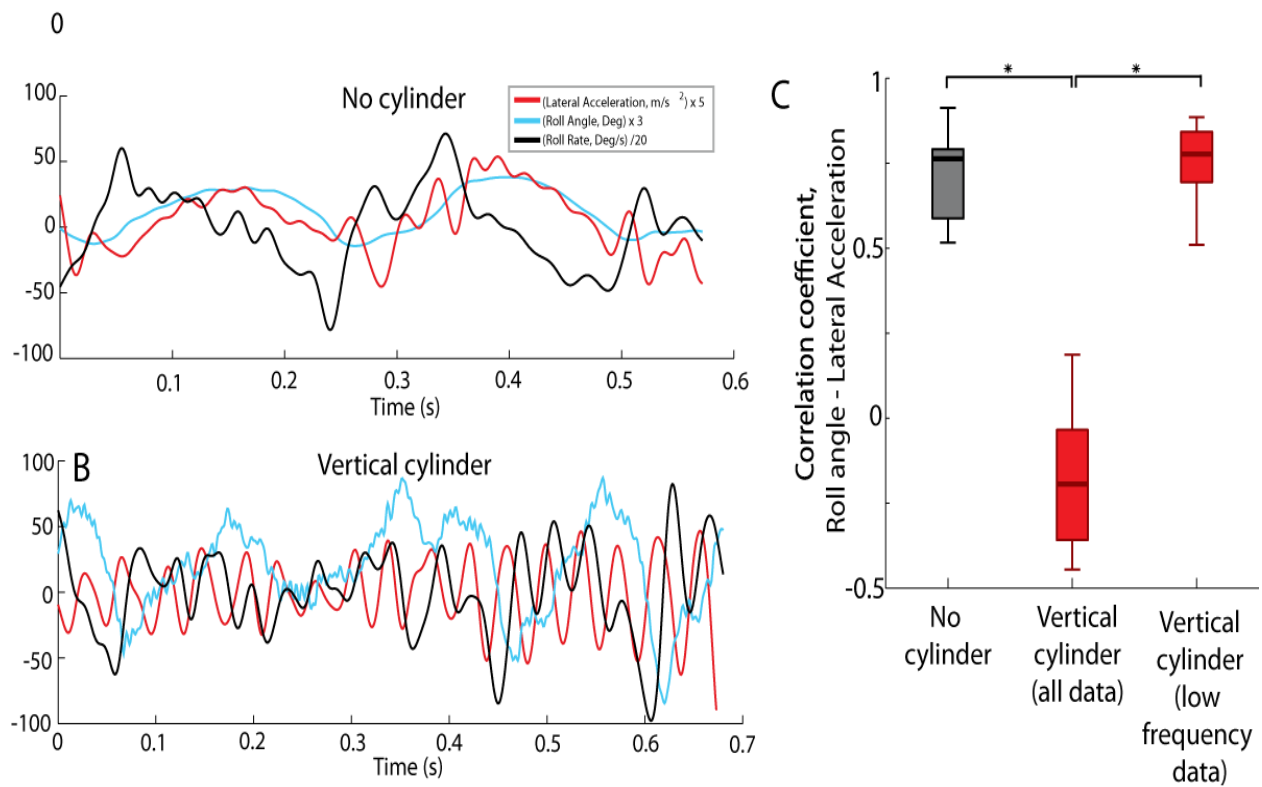
578

579 Figure 7: (A-C) Standard deviation of bees' orientation angles along each body axis (full dataset shown
 580 by solid boxes and higher frequency/3Hz high-pass filtered data by open ones). (D-F) Power spectral
 581 density of the roll, pitch and yaw angles of an individual bee in the three flow conditions.



582

583 Figure 8: (A-C) Mean absolute rotation rates of bees, and (D-F) standard deviation of rotation rates in
 584 each flow condition.



585

586 Figure 9: Time series of the lateral acceleration, roll angle and rolling rate of an individual bee in the no
 587 cylinder (A) and vertical cylinder (B) conditions. Note that ordinate scales are different in A and B. (C)
 588 The zero-time-shift correlation between roll angle and lateral acceleration of bees ($n = 14$) in smooth
 589 flow (left), in the wake of the vertical cylinder (center), and in the same wake with higher frequency
 590 motions removed through filtering (right).

591

592

593

594

595

596

597

598

599

600

	Smooth Flow (No Cylinder)		Horizontal Cylinder		Vertical Cylinder	
	Flow	Bees	Flow	Bees	Flow	Bees
Longitudinal Velocity	0.065	0.02±0.005	0.31	0.02±0.005	0.32	0.03±0.007
Lateral Velocity	0.056	0.03±0.01	0.3	0.043±0.01	0.69	0.056±0.01
Vertical Velocity	0.061	0.04±0.007	0.71	0.046±0.005	0.29	0.042±0.005
Longitudinal Acceleration	7.1	1.2±0.02	51.6	1.6±0.05	50.5	1.7±0.05
Lateral Acceleration	4.9	1.6±0.4	102.2	2.7±0.5	49.5	5.2±0.7
Vertical Acceleration	5.3	1.1±0.1	47.9	2.5±0.2	106.5	2±0.1
Roll	-	6°±3°	-	11°±2°	-	10°±3°
Pitch	1.5°	3°±1°	20.6°	4°±2°	12.3°	4°±2°
Yaw	1.3°	2°±1°	11.1°	3°±2°	19.2°	4°±1°

601 Table 1: Summary of the standard deviations of velocity, acceleration, and rotation along each axis, in
602 the oncoming flow as compared to in bees (averaged across all bees ± standard deviation, $n = 14$). For all
603 flight trajectories, only fluctuations above 3Hz (excluding voluntary, low frequency motions) are shown.
604 Longitudinal, lateral and vertical velocity was measured in m/s, acceleration in m/s^2 , and angles in
605 degrees.