# A COMPUTATIONAL FLUID DYNAMIC STUDY OF HAWKMOTH HOVERING 

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## Summary

A computational fluid dynamic (CFD) modelling approach is used to study the unsteady aerodynamics of the flapping wing of a hovering hawkmoth. We use the geometry of a Manduca sexta-based robotic wing to define the shape of a three-dimensional 'virtual' wing model and 'hover' this wing, mimicking accurately the threedimensional movements of the wing of a hovering hawkmoth. Our CFD analysis has established an overall understanding of the viscous and unsteady flow around the flapping wing and of the time course of instantaneous force production, which reveals that hovering flight is dominated by the unsteady aerodynamics of both the instantaneous dynamics and also the past history of the wing.

A coherent leading-edge vortex with axial flow was detected during translational motions of both the up- and downstrokes. The attached leading-edge vortex causes a negative pressure region and, hence, is responsible for enhancing lift production. The axial flow, which is derived from the spanwise pressure gradient, stabilises the vortex and gives it a characteristic spiral conical shape.

The leading-edge vortex created during previous translational motion remains attached during the rotational motions of pronation and supination. This vortex, however, is substantially deformed due to coupling between the translational and rotational motions, develops into a complex structure, and is eventually shed before the subsequent translational motion.

Estimation of the forces during one complete flapping cycle shows that lift is produced mainly during the downstroke and the latter half of the upstroke, with little force generated during pronation and supination. The stroke plane angle that satisfies the horizontal force balance of hovering is $23.6^{\circ}$, which shows excellent agreement with observed angles of approximately $20-25^{\circ}$. The time-averaged vertical force is $40 \%$ greater than that needed to support the weight of the hawkmoth.

Key words: CFD, computational fluid dynamics, leading-edge vortex, dynamic stall, insect flight, hovering, hawkmoth, Manduca sexta.

## Introduction

Flapping flight is employed by most flying insects (approximately 750000 species), birds and bats (nearly 8000 species). Animal flight covers a wide range of Reynolds numbers, from approximately 10 for the smallest insects with fringed wings to approximately $10^{4}$ for large insects such as certain beetles, moths and butterflies, and up to approximately $10^{5}$ for most birds and bats.

The question of how flapping animals fly can be translated from the aerodynamic point of view to the basic problem of the interaction between the wings and the surrounding air. The way the wings are put in motion, the characteristics of this motion and the main features of the wing-airflow interaction form the essence of the flight mechanism. Flying animals, in general, differ from conventional aircraft in beating their wings rapidly to hover and dart, in performing manoeuvres with rapid
accelerations and decelerations, and in quick plunging and pitching motions. Therefore, we need to understand the aerodynamics of the flapping wings undergoing such highly three-dimensional and unsteady flapping motions, i.e. of the complicated three-dimensional, unsteady and viscous flow around wings with a variable geometry.

The goal of understanding the production of aerodynamic forces can be approached from either of two directions: by characterising the structure of the resultant wake and/or the near-field flow or by studying the time course of force generation by the flapping wings. The approach that visualises the resultant wake, combined with energy conservation assumptions, allows the force production of the wings to be calculated from the flows past them. The key point here is how accurately to characterise and model the unsteady wake pattern
behind the flapping wings, which affects the advance ratio, the strength and the location of the wake and, hence, the forces on the body. Rayner (1979) proposed a vortex theory of animal flight based on the wake being modelled as a series of vortex rings periodically shed into the wake. However, flow visualisation of the wake behind a jackdaw Corvus monedula (Spedding, 1986) shows that this model is not quite realistic; the momentum of the vortex rings produced less than $35 \%$ of the momentum necessary to support the weight of the bird. Maxworthy (1979) succeeded in his pioneering experimental study in visualising the near-field flow around a rigid threedimensional model of the 'fling' motion (Weis-Fogh, 1972) and found a leading-edge vortex with spanwise flow. Using smoke-visualisation of Manduca sexta (Willmott and Ellington, 1997) and of a hawkmoth-based robotic wing (Van den Berg and Ellington, 1997), this leading-edge vortex and the axial (spanwise) flow at the core of the vortex were clearly observed and confirmed to be essential for enhancing lift in insect flight.

The second approach, obtaining the time course of force generation by flapping wings, has also been followed both experimentally and numerically. There are relatively few measurements of the instantaneous forces produced by the three-dimensional flapping wings of animals. Jensen (1956) measured the mean lift of isolated locust wings. Cloupeau (1979) measured instantaneous lift in tethered locusts, and concluded that unsteady mechanisms must generate extra lift forces. Wilkin (1990) also succeeded in measuring the fluctuating lift forces on tethered locusts flying in a wind tunnel, finding that the peak lift was approximately twice the quasi-steady value. Wilkin (1993) and Wilkin and Williams (1993) produced further estimates of the flight forces of both locusts and moths, determining aerodynamic forces by subtracting estimates of the inertial forces from the measured forces. Dickinson (1996) used flow visualisation and instantaneous force measurements of tethered fruit flies (Drosophila melanogaster) to study the dynamics of force generation during flight, but could not obtain a cohesive picture of their relationship mainly because of the time delay involved in the force measurements.

Numerical studies of the unsteady flow around threedimensional flapping wings are even fewer, largely because of the difficulties in modelling the complicated geometry and in simulating the three-dimensional movements of wings. One popular method that is available for computing the unsteady flow about arbitrary bodies is the potential flow panel method; a review of the various panel methods is given by Katz (1991). More recently, an extension of such a three-dimensional panel methods was developed by Vest (1996), in which the motion of the body is prescribed and each wing is assumed to be rigid and to rotate about a common axis. By using a time-stepping solution procedure, the shape of the trailing wake is determined; all vorticity is assumed to be confined to the boundary layer on the surface of the body and in a thin vortex wake shed behind the body. Smith (1996) also developed an unsteady aerodynamic three-dimensional panel method which
can describe the kinematics of a flapping wing relatively realistically and can also account for wing flexibility using a finite element method in analysing the dynamic structure.

These panel methods are generally coupled with the discrete vortex method, and thus can predict the wake as well as the unsteady force generation. However, by ignoring the viscosity of fluid, they fail to predict reasonably the near-field flow, e.g. a large attached leading-edge vortex that has been recognised recently (Ellington et al. 1996) to play a key role in lift generation for insect flight at Reynolds numbers ( $R e$ ) around $10^{3}$. At such low $R e$ values, flows around flapping wings behave unsteadily, usually demonstrating occurrence/breakdown of vortices, separation and reattachment quite different from the behaviour of a fluid at high Reynolds numbers.

As a long-standing goal of studying the aerodynamics of flapping flight, the best approach is to solve the complete viscous and unsteady near-field flows around the flapping wings of animals. Solutions of the full Navier-Stokes equations for the three-dimensional, unsteady flow fields are challenging, and for the flow around variable-geometry bodies this problem is complicated even further. To understand the unsteady aerodynamics induced by a flapping wing, we have developed a computational fluid dynamic (CFD) model (Liu et al. 1995, 1996; Liu, 1997) designed to study both forward flight and hovering of a three-dimensional virtual wing which can have arbitrary variable geometry and can undergo realistic three-dimensional motions, accurately mimicking the movements of insect/bird wings. This CFD model is based on a robust and effective solver of the three-dimensional, incompressible, unsteady Navier-Stokes equations (Liu et al. 1995, 1996), which incorporates recent techniques. In the present study, by defining the three-dimensional geometry of a Manduca-based robotic wing, and by hovering the object with the three-dimensional movements of the wing of a hovering hawkmoth, we address an overall understanding of viscous and unsteady flows around a three-dimensional flapping wing during the whole process of translational and rotational motions, as well as the corresponding time course of instantaneous force generation.

## Materials and methods

## Resolution of the Navier-Stokes equations

The three-dimensional incompressible unsteady NavierStokes equations in the conservative form of momentum and mass are nondimensionalized in a local wingbase-fixed coordinate system (see Fig. 1A), written in an integral form as:

$$
\begin{equation*}
\frac{\partial}{\partial \tau} \int_{V(t)} \mathbf{q d V}+\oint_{S(t)}\left(\mathbf{F}_{\mathbf{i}}-\mathbf{q} \mathbf{u}_{\mathbf{g}}\right) \times \mathbf{n} \mathrm{d} S=0 \tag{1}
\end{equation*}
$$

where vector $\mathbf{q}=[u, v, w, p]^{\mathrm{T}}$ in which $u, v$ and $w$ are three components of velocity, and $p$ is pressure. The term $\mathbf{F}_{\mathbf{i}}$ expresses flow flux coming entering and leaving the cell boundary surfaces. The term $V(t)$ denotes the volume of the cell

Fig. 1. Schematic diagram of the virtual wing. (A) The local stroke-plane-fixed and the global spacefixed coordinate systems. Note that $r_{00}{ }^{\prime}$ denotes the positional vector of the origin of the local stroke-planefixed system and $0^{\prime}$ represents the centre of the stroke plane (the wing base). The local wingbase-fixed coordinate system $(x, y, z)$ is fixed on the centre of the stroke plane (the wing base) with the $x$-direction normal to the stroke plane, the $y$ direction vertical to the body axis, and the $z$-direction parallel to the stroke plane. (B) Three basic components of flapping motion (positional angle $\phi$ ), elevation motion (elevation angle $\theta$ ), and feathering motion of the fore- and hindwing [angle of attack of the leading edge (forewing) $\alpha_{F}$ and angle of attack of the trailing edge (hindwing) $\left.\alpha_{H}\right]$. These angles of attack are defined relative to the $x-y$ plane. Rotating the local coordinate system by the stroke plane angle ( $\beta$ ) gives the global coordinate system ( $X, Y, Z$ ); $X$ and $Y$ form the horizontal plane, and the $Z$-direction is vertical. Note that the axes $y$ and $Y$ are parallel.

A
Coordinate systems
$(x, y, z)$ : local coordinate system
( $X, Y, Z$ ): global coordinate system


B
Definition of three-dimensional motions

$\phi$, positional angle
$\theta$, elevation angle
$\alpha_{\mathrm{F}}$, angle of attack of the leading edge (forewing)
$\alpha_{\mathrm{H}}$, angle of attack of the trailing edge (hindwing)
$\beta$, inclination of the stroke plane
$(i, j, k)$, a hexahedron constructed from eight grid points, and $S(t)$ are its six boundary surfaces with unit outward normal vectors of $\mathbf{n}$. The influence of the moving grid is contributed by the velocity of the moving cell $\mathbf{u g}$. The term $\tau$ denotes the computational time. The governing equations are built and solved in the local wingbase-fixed coordinate system illustrated in Fig. 1A. A moving grid system is introduced to make grids fit the moving and deforming wing at each physical time step, and therefore to ensure sufficient grid density in resolving the viscous and unsteady flows around the wing surface.

The governing equations are discretized using the finite volume method (FVM) and are solved in a time-marching manner using the pseudo-compressibility technique. The timedependent solution to the governing equations is realised by introducing an inner iteration to allow the divergence of velocity to vanish at each physical time step, and the time derivatives in the momentum equations are differenced using a first-order, two-point, backward-difference implicit formula (Liu et al. 1995).

In developing boundary conditions on the body surface, the
no-slip condition is used for the velocity components: i.e. the velocity of a fluid particle is equal to the velocity of the wing at that point. This means that the wing has a smooth surface, although the roughness of the real hawkmoth wing may result in some discrepancy. For the dynamic effect due to rapid acceleration/deceleration of the wing, pressure divergence at the surface stencils is used for the pressure condition derived from the local momentum equation. At open boundary stencils, to satisfy the conservation of momentum, zero-gradient conditions are utilised for velocity components, which means that the local fluid can enter and leave the domain freely. Pressure is unchangeable at the open boundary. Details relating to the algorithm will be published (H. Liu, in preparation).

## Kinematics of the flapping wing

The kinematics of the hovering wing for CFD analyses are based on the kinematic analysis of a hovering hawkmoth by Willmott and Ellington (1997), which was also used by Van den Berg and Ellington (1997) as the motions for a robotic insect wing model (the flapper). Three-dimensional movements of the wing as illustrated in Fig. 1B consist of three basic motions: (1) flapping in the stroke plane by the positional angle $(\phi)$; (2) rotation of the wing on either side, out of the stroke plane, by the elevation angle ( $\theta$ ); (3) rotation (feathering) of the forewing (leading edge) and hindwing (trailing edge) with respect to the stroke plane by the angle of attack of the forewing $\left(\alpha_{F}\right)$ and the angle of attack of the hindwing $\left(\alpha_{H}\right)$. The positional angle, elevation angle and the angles of attack of the fore- and hindwing are defined (in rad) using the first three Fourier terms in Willmott and Ellington (1997) as illustrated in Fig. 2:

$$
\begin{align*}
\phi(t) & =\sum_{n=0}^{3}\left[\phi_{\mathrm{cn}} \cos (n K t)+\phi_{\mathrm{sn}} \sin (n K t)\right]  \tag{2}\\
\theta(t) & =\sum_{n=0}^{3}\left[\theta_{\mathrm{cn}} \cos (n K t)+\theta_{\mathrm{sn}} \sin (n K t)\right]  \tag{3}\\
\alpha_{\mathrm{F}}(t) & =\sum_{n=0}^{3}\left[\alpha_{\mathrm{Fcn}} \cos (n K t)+\alpha_{\mathrm{Fsn}} \sin (n K t)\right]  \tag{4}\\
\alpha_{\mathrm{H}}(t) & =\sum_{n=0}^{3}\left[\alpha_{\mathrm{Hcn}} \cos (n K t)+\alpha_{\mathrm{Hsn}} \sin (n K t)\right] \tag{5}
\end{align*}
$$

Note that time $t$ is dimensionless and parameter $K$ is the reduced frequency defined by $2 \pi f c_{\mathrm{m}} / 2 U_{\text {ref }}$, where $f$ is flapping frequency, $c_{\mathrm{m}}$ is the mean wing chord length (also used as reference length) and $U_{\text {ref }}$ is a reference velocity at the radius of the second moment of wing area $\left[r_{2}(\mathrm{~s})\right.$ : as a fraction of wing length $R$ ] (Willmott and Ellington, 1997). The coefficients $\phi_{\mathrm{cn}}$, $\phi_{\mathrm{sn}}, \theta_{\mathrm{cn}}, \theta_{\mathrm{sn}}, \alpha_{\mathrm{Hcn}}, \alpha_{\mathrm{Fsn}}, \alpha_{\mathrm{Hcn}}$ and $\alpha_{\mathrm{Hsn}}$ are determined from the empirical kinematic data as in Willmott and Ellington (1997) where $n$ is an integer varying from 0 to 3 . The reference


Fig. 2. The positional angle, elevation angle and the angles of attack of the fore-and hindwing versus time during one complete flapping cycle. The curves are based on the first three Fourier series terms (equations 2-5), which were fitted to measurements of a hovering hawkmoth by Willmott and Ellington (1997).
velocity equals $\bar{\omega} r_{2}(s) R$, where $\bar{\omega}$ is the mean angular velocity of the wing. $\bar{\omega}$ is equal to twice the wingbeat amplitude ( $\Phi$, in rad) multiplied by the wingbeat frequency ( $f$, in $\mathrm{s}^{-1}$ ). The Reynolds number $R e$ is given by:

$$
\begin{equation*}
R e=\frac{c_{\mathrm{m}} U_{\mathrm{ref}}}{v} \tag{6}
\end{equation*}
$$

where $v$ is the kinematic viscosity of air, $1.5 \times 10^{-5} \mathrm{~m}^{2} \mathrm{~s}^{-1}$. For the hawkmoth, $c_{\mathrm{m}}=1.83 \mathrm{~cm}, r_{2}(\mathrm{~s})=0.52, R=4.83 \mathrm{~cm}, \Phi=2.0 \mathrm{rad}$ and $f=26.1 \mathrm{~s}^{-1}$, so $R e$ is between approximately 3000 and 4000 . The reduced frequency parameter $K$ was calculated as 0.37 , resulting in a dimensionless computational period of 8.5. The dimensionless parameters $R e$ and $K$ describing the flow were the same for the real moth, the flapper and the computational case.

## Geometry of the virtual wing and domain discretization

We base our geometry of the object on a tracing of the outline of a fore-and hindwing of a male M. sexta. The flapper wing shape was based on the same tracing (Van den Berg and Ellington, 1997), whose aspect ratio is 5.3. A uniform thickness was used, but with elliptic smoothing at the leading and trailing edges as well as at the tip. On the basis of the kinematics of the hawkmoth, in which the two wings do not clap but maintain a certain distance between them, we model a single virtual wing to mimic the hovering mode employed by insects that do not take advantage of the clap-and-fling mechanism.

Since the main spars of insect wings radiate from the bases of the wings, we constructed our virtual wing in a similar manner. Also, since a hawkmoth wing couple consists of a


B Grid system


Symmetrical plane
Fig. 3. (A) Geometry of the virtual hawkmoth wing. The planform (two-dimensional shape) of the virtual wing is based on a tracing of the outline of a fore- and hindwing of a male Manduca sexta, with an aspect ratio of 5.3. The wing has a constant thickness but with smoothed elliptical curves at the leading and trailing edges as well as at the wing tip. (B) A O-O type grid system that discretizes the physical space in the form of a semi-ellipsoid around the wing. The leading-edge vortex was covered by a sufficiently large number of grid points (15-20) in the streamwise direction such that the vortex structure was modelled with high resolution.
connected forewing and hindwing, a two-block method was developed in which each block of grids corresponded to one of the wings. The two parts were joined by a co-grid line at the co-axis between them (Fig. 3A).

To facilitate resolution of the viscous flow at the leading edge, trailing edge and wing tip as well as to save computing time, an O-O type grid topology was introduced (Fig. 3B). In this scheme, the whole physical domain is a semi-ellipsoid. A grid system with $72000(79 \times 29 \times 29)$ nodes was generated around the wing. Grids were clustered to the wing surface, in particular to the leading edge, the trailing edge and the wing tip. To avoid the unstable reflection of the solution at the open boundary, the distance far from the wing was six times the mean chord length.

To model the moving/deforming boundary during movements of the wing, a special method was developed to regenerate grids explicitly at each time step, which minimizes the computing time in regridding. To deal with large deformations of the wing,
regridding is implemented in two steps: (1) rotation of the grids in the whole domain according to the 'rigid' rotational motion of the wing, i.e. flapping, elevation and feathering, which keeps the qualities of the original grids; followed by (2) nonlinear twisting of the grids to incorporate flexing and camber, and stretching the grid lines to fit the deformed wing completely. In the movements of the flapper (Van den Berg and Ellington, 1997), camber is formed as a result of the difference in angle of attack between the forewing and hindwing. This camber causes shear in the wing membrane, which is particularly pronounced during supination and pronation, and which is relieved by a small spanwise sliding motion of the hindwing. We realise this deformation numerically by first rotating the grids according to the angle of attack of the flexing forewing, and then flexing the hindwing to account for the difference between the angles of attack. To mimic the realistic wing, this flexing of the hindwing is achieved by moving grid points vertically (H. Liu, in preparation).

## Evaluation of forces

The Navier-Stokes equations, once solved, describe the near-field flows and the resultant wake in terms of the velocity components and pressure at discretized grid points or cell centres. The lift and drag forces acting on the wing surface can be evaluated from the pressure and stresses along its surface. The resultant lift and thrust forces are calculated first in the local wingbase-fixed coordinate system $(x, y, z)$, as illustrated in Fig. 1A, and then transformed into the global space-fixed coordinate system $(X, Y, Z)$ by accounting for the stroke plane angle.

The local forces are evaluated by a summation of viscous and inviscid fluxes on the wing surface, which are built and saved during computation, leading to three force components in the $x$ - ,y- and $z$-directions (Fig. 1A); this can minimise the numerical error arising from integrating the projection of pressure and stresses. All the force-related quantities are nondimensionalized with respect to the reference velocity $U_{\text {ref }}$, the reference length $c_{\mathrm{m}}$ and the platform area of the wing $S_{\text {wing }}$ such that:

$$
\begin{align*}
& C_{\mathrm{L}}=\frac{L}{\frac{1}{2} \rho U_{\mathrm{ref}^{2} S_{\mathrm{wing}}}}  \tag{7}\\
& C_{\mathrm{T}}=\frac{T}{\frac{1}{2} \rho U_{\mathrm{ref}^{2} S_{\mathrm{wing}}}} \tag{8}
\end{align*}
$$

where $L$ is lift, $T$ is thrust, $C_{\mathrm{L}}$ and $C_{\mathrm{T}}$ are the lift coefficient and the thrust coefficient, respectively, and $\rho$ is the air density.

To assess the vertical force component that supports the insect's weight, we need to transform the lift and thrust into the global coordinate system. Considering the inclination angle $(\beta)$ of the stroke plane with respect to the horizontal plane, we can obtain the vertical $\left(C_{\mathrm{v}}\right)$ and horizontal $\left(C_{\mathrm{h}}\right)$ force coefficients respectively as

$$
\begin{equation*}
C_{\mathrm{v}}=C_{\mathrm{L}} \sin (\beta)+C_{\mathrm{T}} \cos (\beta) \tag{9}
\end{equation*}
$$

and

$$
\begin{equation*}
C_{\mathrm{h}}=C_{\mathrm{L}} \cos (\beta)-C_{\mathrm{T}} \sin (\beta) \tag{10}
\end{equation*}
$$

The force balance of hovering requires the mean vertical force to equal the weight, and the mean horizontal force to be zero. In addition to inserting the observed stroke plane angle $\beta$ into equations 9 and 10 , therefore, we can also calculate $\beta$ such that:

$$
\begin{equation*}
\tan \beta \frac{\overline{C_{\mathrm{L}}}}{\overline{C_{\mathrm{T}}}}, \tag{11}
\end{equation*}
$$

where $\overline{C_{\mathrm{L}}}$ and $\overline{C_{\mathrm{T}}}$ are the mean values of $C_{\mathrm{L}}$ and $C_{\mathrm{T}}$, respectively.

## Results and discussion

## Validation

A series of validation studies have been undertaken and have shown that this computational model is robust and capable of reasonably estimating unsteady fluid-structure interactions in biomechanical problems (Liu et al. 1995, 1996; H. Liu, in preparation). To establish further the validity of the model in simulating the aerodynamics of hawkmoth hovering, we present below a comparison between our computed flows and the experimental results of Van den Berg and Ellington (1997). Details of this comparison will be published (H. Liu, in preparation).

Van den Berg and Ellington (1997) used video and 35 mm photographs to record the flow around the flapper using smoke released from the leading edge. The visualised flows were given at five spanwise cross sections at distances of $0.25 R$, $0.5 R, 0.63 R, 0.75 R$ and $0.87 R$ from the base, respectively. The core positions of the leading-edge vortices and the reattachment points are shown in Fig. 4. The flow at three positional angles $\phi$ during the downstroke with values of $30^{\circ}$, $0^{\circ}$ and $-36^{\circ}$ is also illustrated in Fig. 4. For comparison, the computed flows were visualised at the same three positions, and the instantaneous streamlines are plotted in top and side views relative to the stroke plane (Fig. 5). Pressure contours over the wing are coloured: red indicates high pressure, while blue represents low pressure. There is good qualitative agreement between our CFD analysis (Fig. 5) and the experimental results (Fig. 4) in terms of three-dimensional leading-edge vortex flow. The CFD results show clear axial flow at the core of the leading-edge vortex during the middle and late downstroke, giving the vortex a spiral conical shape. Also, the negative pressure region over the wing surface near the leading edge matches quite well the location of the measured cores of the leading-edge vortices. Additionally, a spanwise velocity gradient can be seen in Fig. 6. The shed vortex from the early half of the downstroke can still be seen above the wing, which is in good agreement with the smokevisualised flow in Fig. 4B (the red-coloured vortex). A strong tip vortex with large velocity magnitudes (Fig. 6) is detected at the position where the leading-edge vortex breaks down and is shed from the wing tip.

In contrast, the computed leading-edge vortex is slightly smaller than the experimental one (Figs 4,5). In a study of the visualised airflow around a tethered hawkmoth in a wind tunnel
(Willmott and Ellington, 1997), the leading-edge vortex was also observed to be small at low near-hovering airspeeds. Note that streaklines, not streamlines, were observed in the flapper and hawkmoth experiments.

We had no measured time course of instantaneous forces to validate the computed force-related quantities. With the good qualitative agreement of the flows between the simulation and the measurements, however, we think that the present CFD model can give a reasonable understanding of the complicated unsteady fluid phenomena in insect flight. In the next section, we address an overall understanding of how the viscous and unsteady flows near the wing behave and how the instantaneous forces are produced during the course of a complete flapping cycle.

## CFD-visualised flows during a flapping cycle

## During downstroke

As illustrated in Fig. 5, a large leading-edge vortex is readily produced during most of the downstroke. During the early downstroke (Fig. 5A), a coherent leading-edge vortex (LEVI) stretches from the base to approximately $60-75 \%$ of the wing length. LEV1 is quite two-dimensional in structure, although some axial flow is visible, with the swirls closely attached to the leading edge of the upper surface and with the core enlarging towards the wing tip.

As the wing moves to a horizontal position (Fig. 5B), LEVI becomes a large, spiralling vortex with strong axial flow at the core, towards the wing tip. The average angle of attack relative to the local flow at this instant is approximately $50^{\circ}$, ignoring the mean induced velocity. This is much higher than the angle, approximately $20-30^{\circ}$, at which stall is initiated for a stationary hawkmoth wing (Willmott and Ellington, 1997). LEV1 is very probably created by dynamic stall. Note that LEV1 is very three-dimensional in structure, consisting of a conical spiral, enlarging as it is swept along the wing. Under LEV1, there is a region of negative pressure (coloured blue) on the wing surface, which corresponds to the diameter and location of the vortex and which will augment the lift force (Fig. 5B).

The axial (spanwise) flow is probably closely related to the spanwise pressure gradient resulting from the spanwise velocity gradient along the flapping wing. The axial flow is accelerated by the spanwise pressure gradient to approximately $50-75 \%$ of the wing length, where a negative pressure island is observed (Fig. 5B). The low-pressure region is quite threedimensional in structure where the spanwise pressure gradient reverses. This corresponds to a large iso-speed area, where the axial flow may reach its peak (Fig. 6) and then starts to decelerate due to a reverse pressure gradient (Fig. 5B). At approximately $75 \%$ of the wing length, the axial flow is reduced to zero (Fig. 5B). These results strongly support those of Van den Berg and Ellington (1997), who found that the largest axial flow velocities were comparable with the mean wing tip velocity and were reached at approximately $50-60 \%$ of the wing length.


## B



Fig. 4. Smoke-visualised flows from Van den Berg and Ellington (1997) during the downstroke at positional angles of (A) $\phi=30^{\circ}$, (B) $\phi=0^{\circ}$ and (C) $\phi=-36^{\circ}$. The smoke is released from a stiff brass smoke rake extending along the leading edge. A large spiral leading-edge vortex is clearly observable in B and C (coloured blue). Top views (left) from Van den Berg and Ellington (1997) illustrate the location and diameter of the leading-edge vortices at the three positional angles; the dashed lines show reattachment points. Note that the area coloured red is the leading-edge vortex observed in the early downstroke and the blue area is the leading-edge vortex in the middle of the downstroke. R, wing length.


## During downstroke

Immediately after the middle of the downstroke, the core of LEV1 breaks down at $75 \%$ of the wing length, and the tip region separates from the wing early in the second half of the
downstroke. We think that this breakdown and separation of LEV1 into the tip vortex is because of the instability of the flow with the reverse pressure gradient combined with the onset of

Fig. 5. Top and side views relative to the stroke plane of CFDvisualised flows at three positional angles during the downstroke at (A) $\phi=30^{\circ}$, (B) $\phi=0^{\circ}$ and (C) $\phi=-36^{\circ}$. Pressure contours on the wing surface are plotted; red denotes high pressure while blue represents low pressure. Instantaneous streamlines are released at the leading edge from both the upper and lower surfaces of the wing, and are followed until the longest ones leave the computational domain. Two large, coherent leading-edge vortices (LEV1 and LEV2) with strong axial flow are present in B and C, which show very good agreement with the experimental results (see Fig. 4). In A and B, a spanwise pressure gradient is observed, which reverses direction near the wing tip. The opposing pressure gradients stop the axial flow at $80 \%$ and $50 \%$ of the wing length (B and C), respectively, at which points the leading-edge vortices break down. - press. island, negative pressure island.
wing deceleration after the middle of the downstroke. $L E V 1$ does not show a significant change from the base to the $75 \%$ position.

Towards the end of the downstroke, a new leading-edge
vortex ( $L E V 2$ ) is created between the wing tip and the brokendown position (Fig. 5C). LEV2 also shows a spiral axial flow, but directed towards the base, and it connects to the original LEV1. This reverse axial flow is apparently created by the reverse pressure gradient originally generated by the tip vortex. $L E V 2$ is strongly affected by the tip vortex and is relatively unstable; the reverse pressure gradient meeting the spanwise gradient leads to a weak axial flow.

As the wing approaches the end of the downstroke and starts supinatory rotation, $L E V 2$ begins to be pushed off the leading edge because of the deceleration of the wing, and the breakdown point of $L E V 1$ moves in to $50 \%$ of the wing length (Fig. 5C). Note that $L E V 2$ looks like a free vortex but is not shed, maintaining a constant vorticity and staying connected to the tip vortex because of the axial flow.

## During supination

When the positional angle of the wing reaches its minimum $\left(-45^{\circ}\right)$, i.e. at the bottom of the stroke (Fig. 7), the angles of

## Top view



## Iso-speed contours and instantaneous streamlines

Fig. 6. Top view of iso-velocity contours in a plane cutting the leading edge of the wing together with instantaneous streamlines at $\phi=0^{\circ}$. There is a spanwise velocity gradient from the base to the tip of the wing, but the flow becomes more complicated near the point of breakdown of the leading-edge vortex. The shed vortex of the early downstroke is still visible above the wing. A strong tip vortex with high velocity is detected where the leading-edge vortex (LEVI) breaks down and is shed.
attack of the fore- and hindwing have risen to $25^{\circ}$ and $10^{\circ}$ (Fig. 2), respectively, resulting in a cambered profile. The $L E V$ s produced during the downstroke and the tip vortex appearing during early supination are not shed yet but, with a slight deformation, turn into a 'hook-shaped vortex' (Fig. 7B). The hook-shaped vortex stays attached to the leading edge and wraps around the wing tip, producing an island at the centre of the 'hook' where all the reattachment (and/or attachment) flows meet. Hence, there is a stagnation point at the centre, resulting in a positive pressure region. Additionally, a shearlayer vortex ( $S L V$, a vortex created by the steep gradient of the shear layer close to the wing surface) is observed on the lower surface of the wing, running from the base to the wing tip, causing a region of negative pressure (Fig. 7C).

During the latter half of supination, when the wing translates upwards, rotates, flexes and increases its angle of attack, the hook-shaped vortex is strongly deformed and very quickly collapses beyond the mid-span joint of the two LEVs. LEV1 is pushed onto the upper surface of the wing with a straight line of axial flow, but is virtually separated at the mid-span and connects to a large flux of flow going over the upper surface and shedding from the trailing edge. This shedding over the trailing edge during late supination is also observed in the flowvisualisation experiments of a tethered peacock butterfly Inachis io (Brodsky, 1991). LEV2 rolls over the leading edge onto the lower surface, connects to the $S L V$ and is eventually shed from the trailing edge.

## During upstroke

Immediately after shedding of the hook-shaped vortex at the end of supination, a very small leading-edge vortex appears at the wing tip at a positional angle of $-36^{\circ}$ (Fig. 8A). It is not separated, like a tip vortex. The vortex is quite twodimensional in structure, although there is some spiral axial flow inside. We did not observe a separate starting vortex in the early upstroke. The leading-edge vortex is limited to a narrow region close to the wing tip and barely affects force generation at this instant (see below).

By the time that the wing reaches the middle position (Fig. 8B), the vortex extends from the wing tip to the base. The vortex still has a two-dimensional structure and is very small, probably because of the small angle of attack with respect to the local flow. The vortex is tightly attached to the leading edge but merely leads to a very small negative pressure region at the wing tip. The flow follows both the upper and lower surfaces smoothly. The axial flow at the core of the vortex initially travels from the wing tip to the base, but reverses direction during the latter half of the upstroke.

After the middle of the upstroke, the leading-edge vortex grows rapidly and hence enlarges the negative pressure region. When the wing reaches a positional angle of $51^{\circ}$ (Fig. 8C), the vortex dimensions are comparable with those observed at early downstroke. Just as during the later part of the downstroke, a reverse pressure gradient and a reverse axial flow run from the break-down point of the upstroke leading-edge vortex to the wing tip. The vortex breaks down at approximately $60-70 \%$
of the wing length, but there is no significant shedding of the tip vortex, which is quite different from the downstroke. We believe that, as in the downstroke, the position of breakdown results from the balance between the spanwise pressure gradient and the reverse pressure gradient at the wing tip.

## During pronation

During pronation, the wing has a small velocity as the positional angle reaches its peak $\left(65^{\circ}\right)$ and the angles of attack of the fore-and hindwing approach zero (Fig. 2). The near-field flow around the wing is visualised in top and side views in Fig. 9. The upstroke $L E V$ remains attached to the leading edge of the lower wing surface (Fig. 9A).

A trailing-edge vortex (TEV) is also detected (Fig. 9B,C) below the lower surface, which is probably due to wing rotation during the first half of pronation. This vortex runs from the base to the tip, is larger than the $L E V$ and lies below it. Note that the $L E V$ spirals to the wing tip, crosses the lower surface of the wing and eventually connects to the TEV. This leads to a large area of flow attachment and hence a positive pressure region (Fig. 9B). Furthermore, a shear-layer vortex (SLV) (Fig. 9C) considerably larger than that at supination covers the upper surface and leads to a large region of negative pressure (Fig. 9C).

As the wing continues to translate and rotate, changing its angle of attack, the separated region of the $S L V$ gradually grows and moves towards the trailing edge, where it is eventually shed into the wake. As the $T E V$ is shed into the wake, the $L E V$ breaks down below the wing with a large flux of flow at the midwing. At the end of pronation, when the wing is about to start the downstroke, air flows smoothly over the lower surface but leaves a large messy flow from the shed SLV of the upper surface. This implies that all the vortices observed during pronation are shed before the downstroke and thus that, in order to enhance lift generation, the wing must produce a new leading-edge vortex on the downstroke.

## Estimation of force generation

To link the CFD-visualized flows to the time course of instantaneous forces, the vortex system is illustrated in Fig. 10. The time variation curves (Fig. 11) of the vertical and horizontal forces are given in the global space-fixed coordinate system (see Fig. 1A). The mean horizontal force must be zero in hovering, and substitution of the computed forces into equation 11 suggests that a stroke plane angle $(\beta)$ of $23.6^{\circ}$ is required to satisfy the force balance. This value is in excellent agreement with the range of approximately $20-25^{\circ}$ reported by Willmott and Ellington (1997) for hovering Manduca sexta and it has been used in equations 9 and 10 .

Comparing Fig. 10 with Fig. 11, we see that the shedding of all the vortices at the end of pronation apparently leads to a small decrease in vertical force. The first half of the downstroke shows a steep increase in lift, and the vertical force coefficient rises almost linearly to a peak of approximately 0.8 . This is probably due to delayed stall, and the increasing size, and hence strength, of the leading-edge vortex (LEV1 in

Fig. 7. Top and side views of CFDvisualised flows with instantaneous streamlines and surface pressure contours during supination. Red denotes high pressure, and blue denotes low pressure. (A) Top view of the flow showing that the downstroke leadingedge vortices (LEV1 and LEV2) are still attached to the leading edge and connected to each other, breaking down at the mid-span. (B) Side view of the upper surface of the wing showing a high-pressure island near the wing tip and a 'hook-shaped vortex'. (C) Side view of the lower surface of the wing showing a shear-layer vortex ( $S L V$ ) covering most of the front of the wing.

A
Top view

B
Side view (upper surface)


## C

Side view (lower surface)

B
Side view
(upper surface)


During supination

Top view Side view


## During downstroke

Fig. 8. Top and side views of CFD-visualised flows with instantaneous streamlines and surface pressure contours during the upstroke at positional angles of (A) $\phi=-36^{\circ}$, (B) $\phi=30^{\circ}$ and (C) $\phi=51^{\circ}$. Red denotes high pressure; blue denotes low pressure. A very small leading-edge vortex ( $L E V$ ) is observed, quite two-dimensional in structure during the first half of the upstroke, but it gradually grows into a larger threedimensional spiral vortex during the second half of the upstroke. Note that the upstroke $L E V$ is considerably smaller and weaker than the downstroke $L E V$.

Fig. 9. CFD-visualised flows with instantaneous streamlines and surface pressure contours during pronation. Red denotes high pressure; blue denotes low pressure. (A) Top view of the flow showing the upstroke leading-edge vortex ( $L E V$ ) still attached to the leading edge but breaking down at $60-75 \%$ of the wing length. (B) Side view of the lower surface of the wing with a high-pressure region near the wing tip. A trailing-edge vortex (TEV) connects to the broken-down leading-edge vortex. (C) Side view of the upper surface showing a large shear-layer vortex ( $S L V$ ) covering most of the fore- and hindwing and leading to a lowerpressure region that contributes to lift generation.

## A Top view



B<br>Side view (upper surface)



## C <br> Side view (lower surface)



During pronation

Fig. 5A,B) produces an increasing negative pressure region. In contrast, the lift shows relatively non-linear features during the latter half of the downstroke (Fig. 11) but maintains a very high value. We believe that these forces are predominantly
produced by the two leading-edge vortices LEV1 and LEV2 (Fig. 5C), which are also created by delayed stall. LEV2, with reverse axial flow originating from the wingtip vortex with strong non-linearity, rapidly increases its strength and hence its

Fig. 10. Diagram of the vortex system during the complete wingbeat cycle. The shaded area at pronation denotes the morphological lower wing surface on the insect diagram (insets). A large leading-edge vortex (LEV) with strong axial flow is observed during the downstroke. This LEV is still present during supination, but turns into a hook-shaped vortex. A small $L E V$ is also detected during the early upstroke, and gradually grows into a large vortex in the latter half of the upstroke. This $L E V$ is still observed closely attached to the wing during the subsequent pronation, where a trailingedge vortex (TEV) and a shear-layer vortex (SLV) are also formed, together forming a complicated vortex system.

fractional contribution to lift production. Therefore, the aerodynamics of the flapping wing, particularly during the latter half of the downstroke, is strongly dependent upon the unsteady three-dimensional movements of the wing.

During the upstroke, the lift coefficient shows a moderate increase, from a slightly negative value immediately after supination to a peak of approximately 0.4 just prior to pronation (Fig. 11). A negative horizontal force, or thrust, is produced throughout the upstroke, which balances the backwardly directed horizontal force of the downstroke. During the first half of the upstroke, therefore, the dominant forces are very likely to be drag-based (both pressure and friction drag). In the late upstroke (Fig. 8C), we see a $L E V$ with axial flow developing quite quickly, and this non-linearises the force variation (Fig. 11) as pronation is approached.

To investigate the extent to which the translational motion is responsible for force production during one complete flapping cycle, we calculated the mean vertical and horizontal forces during the downstroke and upstroke by integrating the instantaneous forces. Mean vertical and horizontal force coefficients are respectively 0.46 and -0.31 during the downstroke, and 0.14 and 0.31 during the upstroke. Note that most of the vertical force, nearly $77 \%$ of the total in one cycle,
is produced during the downstroke, but $23 \%$ is still produced during the upstroke. The backward thrust force during the downstroke is completely cancelled out by a forward thrust force during the upstroke because of the stroke plane angle calculated using equation 11.

The complex vortex structure during the upstroke, with the $L E V$, the $T E V$ and the $S L V$ (Fig. 9), complicates force production during pronation. On the lower wing surface, the interaction between the $L E V$ and the $T E V$ results in a large region of positive pressure (Fig. 9C); on the upper surface, we see a large region of negative pressure at the $S L V$ core. Note that the lift force remains positive during pronation (Fig. 11). With the calculated stroke plane angle of $23.6^{\circ}$, we see a large instantaneous vertical force coefficient of approximately 0.35 immediately after the highest wing position, which is even larger than the mean value of 0.3 during one complete cycle (Fig. 11). Because pronation is so brief, however, it contributes only slightly to lift production.

Analysis of the aerodynamics during pronation suggests that the different three-dimensional movements (Fig. 2) of the wing during supination are of great importance in avoiding negative lift production. The asymmetric kinematics of supination creates a complex 'hook-shaped' vortex on the upper surface (Fig. 7B) with a small SLV on the lower surface (Fig. 7C),


Fig. 11. Coefficients of vertical and horizontal forces versus positional angle. Arrows for each phase of the wingbeat cycle indicate the direction of time. The mean vertical force coefficient is 0.3 , equivalent to a vertical force of approximately 11.05 mN and sufficient to support half the weight of a hawkmoth $(7.8 \mathrm{mN})$.
which is quite different from that seen during pronation (Fig. 9). Therefore, little negative lift and thrust forces are produced during supination (Fig. 11).

To assess whether the vertical force from the present computation is capable of supporting the hovering moth, we further integrated the vertical coefficients during one complete flapping cycle and obtained a mean value of 0.3 . Note that the force coefficients are nondimensionalised by normalization to the maximum velocity during one flapping cycle. Given the reference velocity $U_{\text {ref }}=2.6 \mathrm{~m} \mathrm{~s}^{-1}$ and the surface area $S_{\text {wing }}=8.8$ $\mathrm{cm}^{2}$ of a real Manduca sexta wing (Willmott and Ellington, 1997), the vertical force $F_{\mathrm{v}}$ is equal to:

$$
\begin{equation*}
F_{\mathrm{v}}=0.5 r U_{\mathrm{ref}}{ }^{2} S_{\mathrm{wing}} C_{\mathrm{v}} \tag{12}
\end{equation*}
$$

where the density of air $\rho$ is taken as $1.225 \times 10^{-6} \mathrm{~kg} \mathrm{~m}^{-3}$. The total vertical force is therefore equal to 11.05 mN for one wing. The mean force required per wing is half the weight of the hawkmoth (mass 1.58 g ) or approximately 7.8 mN . Hence, the calculated mean force in a complete flapping cycle is 1.41 times that required to support the weight of the hawkmoth. The insect body may interact with the flow, but it is very unlikely that this would result in an almost $41 \%$ reduction of the vertical force.

## Leading-edge vortices during up- and downstroke

Large leading-edge vortices that enhance the circulatory lift and that are likely to feature prominently in the delayed stall of insect wings are commonly observed in two-dimensional model experiments at appropriate Reynolds numbers (e.g. Newman 1977; Saharon and Luttges, 1989; Dickinson and Götz, 1993). However, these large two-dimensional leadingedge vortex mechanisms can only give approximate explanations of insect flight because they lack the axial flow generated by the more sophisticated three-dimensional


Fig. 12. The angles of attack relative to the local flow during one complete flapping cycle. The angles are calculated for the span position $r_{2}(s) R$. Note that the effect of the downwash is not taken into account. The relative angle of attack in most of the downstroke is roughly flat with a value of approximately $50^{\circ}$, which would be reduced by approximately $15^{\circ}$ by the downwash.
mechanism that couples both three-dimensional motions and the geometry of the wing.

A leading-edge vortex is observed (Figs 4B, 5B) and a large lift is detected (Fig. 11) during the downstroke, but how is the leading-edge vortex created? Using the instantaneous velocity based on the kinematic data (Fig. 2), we first calculated the angles of attack with respect to the local flow at the span position $r_{2}(s) R$ and plotted them in Fig. 12. These values do not include the effect of the downwash from the induced velocity field. The angle of attack is roughly flat during most of the downstroke with a value of approximately $50^{\circ}$, which would be reduced by approximately $15^{\circ}$ by the downwash (Willmott and Ellington, 1997). It is during this period that the large vortices (LEV1 and LEV2) are closely attached to the leading edge on the upper wing surface. Compared with the stall angle of attack (approximately $20-30^{\circ}$ ) of a hawkmoth wing in steady flow (Willmott and Ellington, 1997), this indicates that the leading-edge vortices are created by delayed stall. The constancy of the angle of attack further implies that it might be optimal for creating the leading-edge vortex (Fig. 5) and hence the large lift production (Fig. 11).

Why is the leading-edge vortex spiral? The pressure gradient due to the velocity gradient and/or spanwise centrifugal acceleration may well have been responsible for the observed axial flow. However, these conditions also apply to helicopter rotors and wind turbine blades, but large-scale spanwise flows have not been observed for them (De Vries, 1983). So why is the spiral leading-edge vortex not formed for rotary wings whereas it is clearly present for flapping wings?

On the basis of our analysis given above, we think that there may be two essential conditions for the existence of a three-
dimensional vortex with axial flow: vorticity and a pressure gradient at the core of the vortex. Flapping insect wings at a large angle of attack can produce a strong leading-edge vortex very probably by delayed stall. At the low Reynolds numbers at which insects fly, this $L E V$, when it occurs, would usually maintain chordwise flow (flow from the leading-edge to the trailing-edge) without shedding, which would further increase its strength. The steep spanwise pressure gradient, which is probably due to the velocity gradient, can produce the strong axial flow that concentrates the $L E V$, preventing it from accumulating into a large vortex that would be unstable, as observed in previous two-dimensional experiments relevant to insect flight (Edwards, 1982; Dickinson, 1996).

In helicopter rotors and wind turbine blades, the first condition is probably not satisfied. The high Reynolds numbers (up to approximately $10^{6}$ ) together with a constant small angle of attack will not result in a strong and stable vortex; even if a vortex were generated during dynamic stall at high angles of attack, it would not be able to resist the very strong chordwise flow and would immediately collapse. Thus, even though the second condition may be fulfilled, we observe only a small radial velocity component (Chee, 1990).

How is the reverse pressure gradient at the wing tip (Fig. 5B) produced? The large angle of attack of the wing usually leads to a steep velocity gradient at the wing tip and thus produces a pressure gradient between the lower and upper surfaces (Fig. 5B). As a result, as is often seen in flows around a delta wing, a wing tip vortex is observed. Differences in velocities at the wing tip during the downstroke therefore lead to a reverse pressure gradient against the spanwise gradient produced by the velocity gradient (Figs 5B, 6). Note that both flow and pressure distribution at the wing tip are very much three-dimensional in structure and therefore are strongly dependent upon both the local geometry and the wing motions. Combining with the spanwise pressure gradient, the reverse pressure gradient decelerates the axial flow to zero at approximately the $75 \%$ wing length (Fig. 5A,B). During the latter half of the downstroke, the wing decelerates and hence the velocity gradient decreases, leading to a reduced spanwise pressure gradient. In addition, with increasing positional angle, the velocity gradient over the wing tip between the upper and lower surfaces may become steeper, which could result in an increase in the reverse pressure gradient. As a result, the reverse pressure gradient becomes increasingly dominant and the point of breakdown is continuously pushed towards the base of the wing. At the end of the downstroke, it is located near the middle of the wing (Fig. 5C). This gives a good explanation of what happens in the dark region from the midspan to the wing tip as seen in the smoke-visualised flow in Fig. 4C.

## Aerodynamics during pronation and supination

The presence of the $L E V$ during pronation as well as supination poses a question: how can a $L E V$ created during previous translational motion remain attached to the wing and
not be shed? This is a general question that can be applied to the flapping flight of insects and other animals that do not take advantage of the clap-and-fling mechanism (Weis-Fogh, 1972). As described in previous sections, we believe that this is because of the appropriate coupling of unsteady motions involving the deceleration, the elevation and the rotational motion, which in toto delays shedding of the vortex during pronation and supination (Fig. 10).

Additionally, the appearance of the shear-layer vortex (SLV) can be explained by the fact that the rotational motion and deceleration of the wing lead to the separation point of the $L E V$ rolling over the leading edge and attaching onto the upper surface, which means that the leading edge cuts into the vortex. Additionally, with the help of the elevation motion, flow within the separated region on the upper surface of the wing would be accelerated, which could also enlarge this region of suction and lead to the production of the large shear-layer vortex. Note that the vortex shows a three-dimensional conical structure. Therefore, the region of suction leads to the production of a large negative pressure region covering most of the upper surface of the wing which, together with the positive pressure region on the lower surface, may contribute to some extent to lift production during pronation, depending upon the orientation of the wing.

Through our CFD analysis, we believe that the rotational flow structures are apparently dependent on the history of the aerodynamics, i.e. the leading-edge vortex created during previous translational motion, and also on the complex threedimensional motions of the wing. The complicated vortex system observed during pronation and supination could not occur in the absence of the upstroke and the downstroke. The rotational motion seems to capture and deform the existing vortex, but not create a new leading-edge vortex. For insects taking advantage of the clap-and-fling mechanism, the clap at the top of the stroke would probably shed the leading-edge vortex generated during the upstroke, and the quick fling of the wings would produce a large new leading-edge vortex on the upper surface that would enhance the circulation and lift on the downstroke. Although many insects could use the circulation created by a fling/peel motion, most seem to shun the mechanism in spite of the aerodynamic benefits. If nothing else, there must be significant mechanical wear and damage to the wings caused by repeated clapping (Ellington, 1995). For most insects that use a near fling or near peel, where the wings remain separated by a fraction of the chord length and do not actually touch, however, it is obvious that they receive aerodynamic benefit from the previous translational motion.

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