# Fruit shape diversity in the Brassicaceae is generated by varying patterns of anisotropy 

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#### Abstract

Fruits exhibit a vast array of different 3D shapes, from simple spheres and cylinders to more complex curved forms; however, the mechanism by which growth is oriented and coordinated to generate this diversity of forms is unclear. Here, we compare the growth patterns and orientations for two very different fruit shapes in the Brassicaceae: the heart-shaped Capsella rubella silicle and the near-cylindrical Arabidopsis thaliana silique. We show, through a combination of clonal and morphological analyses, that the different shapes involve different patterns of anisotropic growth during three phases. These experimental data can be accounted for by a tissuelevel model in which specified growth rates vary in space and time and are oriented by a proximodistal polarity field. The resulting tissue conflicts lead to deformation of the tissue as it grows. The model allows us to identify tissue-specific and temporally specific activities required to obtain the individual shapes. One such activity may be provided by the valve-identity gene FRUITFULL, which we show through comparative mutant analysis to modulate fruit shape during post-fertilisation growth of both species. Simple modulations of the model presented here can also broadly account for the variety of shapes in other Brassicaceae species, thus providing a simplified framework for fruit development and shape diversity.


KEY WORDS: Brassicaceae, Capsella, Arabidopsis, Fruit shape, Modelling, Anisotropic growth

## INTRODUCTION

Despite the great diversity in plant organ shapes, it has been proposed that common principles may underlie shape determination (reviewed by Sluis and Hake, 2015). Based on inheritance studies, it was recognised from the early days of genetics that genes regulate organ size and shape determination (Emerson and East, 1913; Freeman, 1919; Dale, 1925; Sinnott and Kaiser, 1934). In fact, Sinnott's work on Cucurbita pepo fruit growth showed that it is possible to genetically differentiate between activities that regulate shape and activities promoting growth (Sinnott, 1935). More recently, key genetic factors involved in determining fruit shape in

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domesticated fruit crops such as tomato, melon and pepper have been uncovered (Tanksley, 2004; Paran and van der Knaap, 2007; Monforte et al., 2014). Furthermore, tissue-level models of leaf and petal growth have led to the suggestion that shape depends on patterns of specified anisotropic growth that are oriented by a polarising field (Green et al., 2010; Kuchen et al., 2012; SauretGueto et al., 2013). Conflicts generated by regions growing with different rates or orientations lead to changes in curvature and shape. However, it is unclear whether such models could account for the growth patterns and diversity of 3D fruit shapes. Here, we address this problem by analysing the growth and development of two very different fruit shapes in the Brassicaceae.

Although the overall composition and organisation of fruit tissues are highly conserved among members of the Brassicaceae family, huge diversity exists in their shape, which include, for example, cylindrical, disc-formed, spherical and heart-shaped structures (Langowski et al., 2016). In many cases it is not immediately evident what advantages the different shapes provide for fitness and dispersal. It is also unclear how such variation in form can evolve when coordination of tissue growth and specification is of such pivotal importance for timely development and seed release. Comparative analysis of fruit development in well-studied species with different fruit shapes, such as Arabidopsis thaliana and its relative Capsella rubella, might provide a framework for addressing these issues.

In common with most angiosperms, Arabidopsis fruits are derived from united carpels that encapsulate the developing seeds. The German author and philosopher Johann Wolfgang von Goethe proposed that all lateral plant organs are modifications of the same archetypal organ (von Goethe, 1790). In line with Goethe's hypothesis, carpels have been shown to have a leaf-like origin (Scutt et al., 2006). The lateral part of the Arabidopsis fruit develops into valves (the walls of the seed pod) that are fused to a medial replum. Between the valves and the replum, narrow strips of tissue made up of a few cell files form the valve margin where fruit dehisces to release the seeds upon maturity (Ferrándiz et al., 1999; Seymour et al., 2013). A style topped with stigmatic papillae develops at the apex of the fruits (Fig. 1A). The development and growth of the fruit are precisely coordinated across these diverse tissues to ensure the timely release of seeds upon maturity.

Some of the key regulators of fruit development in Arabidopsis have been identified and genetic interactions between them established. FRUITFULL (FUL) and REPLUMLESS (RPL) genes specify valve and replum formation, respectively, and they do so at least partly by restricting the expression of valve margin identity genes such as SHATTERPROOF1 (SHP1), SHP2, INDEHISCENT (IND) and ALCATRAZ (ALC) (Liljegren et al., 2004; Dinneny et al., 2005).

Fruits from members of the Capsella genus have the same overall tissue composition as Arabidopsis, including two valves, a replum and style. However, the valves of mature Capsella fruits are
extended at the distal end resulting in a heart-shaped appearance of the organ. In 1914, George Harrison Shull crossed the tetraploid Capsella bursa-pastoris (heart-shaped fruits) with a natural variant of C. bursa-pastoris, named 'heegeri', which has cylindrical fruits. Shull found a $15: 1$ segregation in the F2 generation of heart to cylinder (Shull, 1914), leading him to suggest that two genetic loci contribute to the trait. This observation agrees with Sinnott's hypothesis two decades later that while certain genes will promote organ growth, others will be required to establish shape (Sinnott, 1935).

Here, we compare the formation of the heart-shaped fruit of Capsella with the cylindrical fruit of Arabidopsis to understand how organ shape is controlled and thus how the different fruit forms can emerge. Morphological and clonal analyses reveal patterns of anisotropic growth (when the ratio of growth rate in length to growth rate in width differs from 1) that can vary in both space and time between the species. We describe different phases during Capsella and Arabidopsis development, each including consecutive developmental stages (Roeder and Yanofsky, 2006). Arabidopsis shows similar levels of anisotropy during all phases of development, whereas Capsella shows a more complex pattern of anisotropy that changes from one phase to the next. Based on these findings we develop a model that accounts for both the resultant patterns of anisotropy and the fruit shape in each species. Given the conservation
of tissue identities among Brassicaceae fruits, we also compare the role of the valve-identity factor FUL in fruit shape development and show that it exerts its effects during the late phase of growth. Our findings thus provide a framework for understanding the development of diverse fruit shapes within the Brassicaceae family.

## RESULTS

To determine when and how the shapes of Arabidopsis and Capsella diverge, we first compared the growth rates in overall length and width. We chose a starting point when the gynoecium primordia are similar in shape and size, $\sim 40 \mu \mathrm{~m}$ in length. This stage is referred to as 0 days after initiation (DAI) and is equivalent to stage 6 of Arabidopsis flower development (Roeder and Yanofsky, 2006). From 0-2 DAI defines an initial phase of high growth rate preferentially along the longitudinal axis of the gynoecium in both Capsella and Arabidopsis (Table 1). After this early phase of anisotropic growth, there is a drop in both growth rate in length and anisotropy in Capsella (Table 1, Fig. 1B,C), whereas in Arabidopsis anisotropy is maintained while growth rate in length is less reduced (Table 1, Fig. 1B,D). Thus, the development of Capsella and Arabidopsis fruits can be divided into two phases: an early phase of relatively high growth rate in length, followed by a second phase during which this growth rate is lower. Growth in width is constant during these two phases (Table 1).


Fig. 1. Fruit growth analysis. (A) Mature fruits from Arabidopsis (left) and Capsella (right) with tissues indicated as s (style), v (valve) and r (replum). Mediolateral and proximodistal orientations are indicated. (B) Fruit width plotted against length during Capsella (black diamonds) and Arabidopsis (grey crosses) fruit development (natural logarithm scales). The gradient for the fitted line for Arabidopsis (orange) is 0.49 (growth in length>width). There are two distinct gradients for Capsella: an early phase of 0.33 (green line, growth in length>width) and a later phase of 1.14 (blue line, growth rate in width>length). Red dashed line shows a gradient of 1 for comparison. (C) Capsella fruit length (black diamonds) and width (grey crosses) plotted against time from initiation to maturity. (D) Arabidopsis fruit length (black diamonds) and width (grey crosses) against time from initiation to maturity. In $C$ and $D$ the mean shapes of the fruit at each of the given stages are shown. Scale bars: 1 mm in C,D.

Table 1. Growth rates (\%/h) during development of Capsella and Arabidopsis fruits

| Plant | Early phase (0-2 DAI) |  | Second phase (2-18 DAI) |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Growth rate | Anisotropy | Growth rate | Anisotropy |
| Capsella |  |  |  |  |
| Length | 3 | 2.73 | 1 | 0.91 |
| Width | 1.1 |  | 1.1 |  |
| Arabidopsis |  |  |  |  |
| Length | 2.2 | 3.67 | 1.3 | 2.17 |
| Width | 0.6 |  | 0.6 |  |

Anisotropy is calculated by length/width.

To determine the shape changes during these two phases we used optical projection tomography (OPT) and scanning electron micrographs (SEMs) to image different stages. In the early phase (0-2 DAI) the shapes of the Capsella and Arabidopsis gynoecia are similar: they initiate as an oval ridge with a central groove that grows into a hollow cylinder by 2 DAI (Fig. 2A-C,J). However, between 2 and 8.5 DAI the gynoecia of Capsella and Arabidopsis become morphologically distinct. The Arabidopsis gynoecium continues to elongate as a cylindrical shape throughout development (2-18 DAI), resulting in a long thin fruit (Fig. 2K,L,N,O) of near-circular circumference (Fig. 2M,P). By contrast, the Capsella gynoecium develops into a more rounded structure with an oval circumference and topped by a narrow style (8.5 DAI, Fig. 2D-F). This shape is known as an oblate spheroid (Hilbert and Cohn-Vossen, 1999). From 8.5 to 11.5 DAI, the base of the Capsella fruit becomes increasingly tapered and the distal part of the valves grows larger to produce a heart shape (Fig. 2G,H) that is flattened in cross-section (Fig. 2I). 9 DAI corresponds to the fertilisation stage (stage 13 of Arabidopsis flower development), and the characteristic heart shape of Capsella fruits therefore forms while the seeds develop inside. Based on these shape changes, the second growth phase in Capsella (Table 1) is divided into a middle (oblate spheroid) and late (heartshape) phase, whereas in Arabidopsis the second phase shape is constant throughout development.

## Approach to measuring and modelling growth

The observed changes in fruit shape could be generated by many different growth patterns. Consider a simplified example of a 2D square piece of tissue that grows into a vertically elongated rectangle (Fig. 3). This transformation could be generated by a pattern of uniform anisotropic growth, in which growth rate along the vertical axis is higher than that along the horizontal axis. An initially square grid or set of marked circles would then be uniformly stretched (Fig. 3A,B). The vertical growth rate of each region (circle or square) would be:

$$
\begin{equation*}
\mathrm{K}_{\max }=\left(\ln \mathrm{Y}_{1}-\ln \mathrm{Y}_{0}\right) / \mathrm{T} \tag{1}
\end{equation*}
$$

where $T$ is time, $Y_{0}$ is the length of the vertical axis at $T_{0}$, and $Y_{1}$ is the length of the vertical axis at $\mathrm{T}_{1}$, while the horizontal growth rate would be:

$$
\begin{equation*}
\mathrm{K}_{\min }=\left(\ln \mathrm{X}_{1}-\ln \mathrm{X}_{0}\right) / \mathrm{T} \tag{2}
\end{equation*}
$$

The square could also be transformed into an elongated rectangle by a pattern of non-uniform anisotropic growth, with higher growth rate at the bottom than the top (Fig. 3C). Sections in the original grid would then have different sizes in the resultant elongated rectangle. The growth rates of each region could again be estimated by taking the difference in the natural logarithms, although these values would no longer be uniform over the tissue.

Similar to marking the tissue with circles in the grid, individual cells could be marked in a biological system to capture the distribution of cellular growth patterns across a tissue. We used a Cre-Lox heat shock-inducible system, Brother of Brainbow (BOB) (Wachsman et al., 2011), to mark randomly distributed cells with either CFP or RFP upon induction. We marked cells at various times and imaged resultant clone patterns at specified lengths of the gynoecium: $300 \mu \mathrm{~m}, 500 \mu \mathrm{~m}, 1 \mathrm{~mm}, 2 \mathrm{~mm}$ and 4 mm , using florescence or confocal microscopy. We assumed an initial cell size of $7 \times 7 \mu \mathrm{~m}$ based on measurements at 0 DAI in Arabidopsis and 4-6 DAI in Capsella. In Capsella, cell sizes were similar between 4 and 6 DAI and so it was assumed that cell size was maintained at $7 \mu \mathrm{~m}$ from 0 DAI (Table S1). As with the circles in the grid example (Fig. 3), assuming that the initial cells are of uniform size and isodiametric shape, growth rates along different axes can be estimated from the dimensions of the resultant clones.

The transformation of a square into a rectangle in 2D is more straightforward than the growth of a tissue, which can curve and deform in 3D as a result of mechanical constraints. In this situation, computational modelling is needed to relate the observed clonal patterns to the underlying specified growth patterns. We used the Growing Polarised Tissue (GPT) framework, in which growth rates can be specified by factors that are distributed across the tissue (Green et al., 2010; Kennaway et al., 2011; Kuchen et al., 2012; Sauret-Gueto et al., 2013). The tissue is modelled as a continuous sheet, termed the canvas, that is mechanically connected and can deform in 3D. A polarity field allows anisotropic growth to be incorporated. Polarity is specified with a diffusible factor, POLARISER (POL), which propagates from regions of high to low concentration (Fig. 3A-Diii). The gradient of POL is used to specify a local polarity, allowing parallel ( $\mathrm{K}_{\mathrm{par}}$ ) or perpendicular ( $\mathrm{K}_{\text {per }}$ ) growth rates to be separately specified.

We distinguish between specified growth (inputs to the model) and resultant growth (output) (described by Kennaway et al., 2011). The specified growth rate of a region is the rate at which that region would grow if it were free from any mechanical constraints of surrounding tissue. The resultant growth rate is the rate at which that region grows when mechanical constraints of neighbouring tissue are taken into account. If the tissue has uniform isotropic growth rates, or all tissue grows with the same anisotropic growth rate in the same orientation (Fig. 3B,C), then there is no tissue conflict and specified and resultant growth are the same. In most other cases, conflicts between connected regions that are specified to grow at different rates or orientations generate deformations and curving of tissue (rotations) that are not explicit in the specified growth pattern but emerge through the mechanical conflicts. For example, if a square shape is grown with a higher $\mathrm{K}_{\text {per }}$ in the middle than at the top and bottom, the shape will bulge in the middle (Fig. 3D). The initial square grid has become curved and polarity is no longer uniformly vertical. The curvature (regional rotation) was not part of the specified growth but emerges as the result of tissue conflicts. If curvature does not fully resolve the conflicts, residual stresses are also generated. In our models, we assume that these residual stresses are dissipated during growth (Kennaway et al., 2011). Experimentally observed clone sizes and orientations do not give specified growth rates (inputs to the model) but can be compared with virtual clones or resultant growth rates generated as the result of running the model (outputs). For example, virtual clones (circles) in Fig. 3Dii splay out at the edge of the bulge (arrowed). This reorientation is not an explicit part of the initial specified growth pattern but emerges from the resultant growth and connectivity of the tissue.


Fig. 2. SEM and OPT images of gynoecium shape development in Capsella and Arabidopsis. (A-I) Capsella rubella gynoecium and fruit. (A) SEM of gynoecium at 2 DAI. (B,C) Virtual sections at 0.5 DAI in the longitudinal $(\mathrm{B})$ and transverse (C) planes. A central groove is indicated (arrow). (D-F) As in A-C, but at 8.5 DAI. (G-I) As in A-C, but at 11.5 DAI.
(J-P) Arabidopsis thaliana gynoecium and fruit. (J) SEM of gynoecium at 2 DAI.
(K) SEM at 9 DAI. (L,M) Virtual sections at 9 DAI in the longitudinal ( L ) and transverse (M) planes. (N-P) As in K-M, but at 11 DAI. Shapes of gynoecium/fruit OPT crosssections are indicated with red circles (C,F,I,M,P). The background in the OPT images in C,E,F,H,I,L,M,O,P was set to white using the software package VolViewer. st, stigma; s, style; v, valve; r, replum. Scale bars: $50 \mu \mathrm{~m}$ in A-C,J; $250 \mu \mathrm{~m}$ in D-I,K-P.

Each model is composed of three components: a starting canvas shape (loosely based on the size and shape of the gynoecium at 0 DAI, simplified as a short oval cylinder) with regional factors, a growth regulatory network and a polarity system (Fig. 4C-E). The connectedness of the tissue results in shapes and features, such as curvature, that were not specified in the model and result from regional growth conflicts. Rather than match all the details of the clones and fruit shape changes, we tried to capture the general character of the clones and shape transitions in each phase.

## Early phase

The early phase is characterised by high growth rates in length and a cylindrically shaped gynoecium in both species. Because we were unable to easily image clones at 2 DAI, we imaged them at 4 DAI ( $300 \mu \mathrm{~m}$ length), which covers the early phase and beginning of the middle phase. We imaged epidermal clones for multiple samples and collated them onto a mean shape of the organ at 4 DAI to generate a clone map (Fig. 4). The mean
shapes of the Capsella and Arabidopsis gynoecia have already started to diverge at 4 DAI: Capsella has a wider and more rounded shape (Fig. 4Ai) than Arabidopsis (Fig. 4Bi). This difference in shape is most likely generated in the middle phase (see below).

Consistent with length/width (L/W) growth rates, the clones that capture the early phase of growth ( $0-2 \mathrm{DAI}$ ) are elongated along the longitudinal axis in both Capsella and Arabidopsis (Fig. 4Aii,Bii). Comparing Capsella and Arabidopsis clones induced at 0 DAI and imaged at 4 days after induction gave an average L/W ratio of 5.2 and 7.7, respectively. This anisotropic shape of the clones is correlated with cell division rates, with two to three rounds of cell division along the longitudinal axis and zero or one round of cell division along the circumferential axis in both species. Growth is mostly uniform across the gynoecium in both species. However, clones near the base and the apex in Capsella and Arabidopsis are shorter, suggesting slower growth along the proximal distal axis in these regions (Fig. 4Ai,Bi).


Fig. 3. Growing a 2D square. (A) Starting 2D square at $T_{0}$ marked with a grid (i), virtual clones (ii) and polarity field (iii). (B) Resultant rectangle shape after uniform anisotropic growth: grid has deformed uniformly (i) and virtual clones have uniform size and shape (ii). (C) Resultant rectangle shape as in B, but with non-uniform anisotropic growth (higher growth at the bottom). The grid has deformed non-uniformly (i) and the virtual clones differ in size and shape across the rectangle (ii). (D) With higher $\mathrm{K}_{\mathrm{per}}$ in the middle than at the top and bottom, the shape will bulge in the middle and give rise to a rounded shape. This curvature was not specified but emerges as the result of tissue conflicts. Arrows (Dii) indicate clones that splay out at the edge of bulge. Scale bars: 1 mm .

To determine how the growth rate of the clones compares to whole-organ growth values, the average growth rates of the clone major axis $\left(\mathrm{K}_{\max }\right)$ and minor axis $\left(\mathrm{K}_{\min }\right)$ were calculated (Table 2) based on growth rates in defined regions (Table S3). Since the clones are anisotropic along the longitudinal axis of the gynoecium, $\mathrm{K}_{\max }$ is aligned with the longitudinal axis of the gynoecium and $\mathrm{K}_{\text {min }}$ is aligned with the circumference. The values of $\mathrm{K}_{\max }$ are comparable to high growth rates in length for the early and middle phases in both Arabidopsis and Capsella (Table 2). However, the values of $\mathrm{K}_{\min }$ are lower than the whole-organ growth rates in width in both species (Table 2). This could be explained if the cells were not isodiametric in shape at the time of induction. For example, if the cells were smaller than $7 \mu \mathrm{~m}$ in width, growth rates would be underestimated. Overall, the clone patterns show that the high longitudinal growth in the early stages of development is distributed throughout the gynoecium of both species and slightly lower towards the base and style.

To model this anisotropic growth during the early phase using the GPT framework, we created a longitudinal gradient of POL in the initial canvas. This was achieved by having a region of POL production at the base. The result is a proximodistally oriented polarity field (Fig. 4C). To account for the observed anisotropy in growth, the specified growth rates are higher parallel to the polarity than perpendicular to the polarity (for Capsella $\mathrm{K}_{\mathrm{par}}=1.4 \% / \mathrm{h}$ and $\mathrm{K}_{\mathrm{per}}=1.15 \% / \mathrm{h}$ and for Arabidopsis $\mathrm{K}_{\mathrm{par}}=1.3 \% / \mathrm{h}$ and $\mathrm{K}_{\text {per }}=0.6 \% / \mathrm{h}$ ). These growth rates were specified based on $\mathrm{L} / \mathrm{W}$ growth rate ratios during the individual growth phases of the gynoecium and fruit. To enhance longitudinal growth during the early phase, we introduced a factor (EPHASE) that promotes $\mathrm{K}_{\text {par }}$ from 0-2 DAI (Fig. 4E). As the clonal analysis spans 0-4 DAI, EPHASE is inactive during the 34 DAI period. In addition, the fact that both species only have a few clones near the base and presumptive style suggests lower growth in these regions, and so we introduced two additional factors active during 3-4 DAI: BASE, which inhibits $\mathrm{K}_{\mathrm{par}}$ and $\mathrm{K}_{\mathrm{per}}$; and STYLE, which inhibits $\mathrm{K}_{\text {per }}$ (Fig. 4D,E). Growth specified in this way causes the canvas to deform to give resultant sizes and shapes that broadly match those of the gynoecia observed at 4 DAI (Fig. 4F,G). The output shape for both models tapers towards the base and style because of the inhibition of $\mathrm{K}_{\text {per }}$ in these regions, which creates a conflict in growth rate between these regions and the adjoining valve (Fig. 4H). The Capsella shape tapers more than the Arabidopsis shape because of the higher rate of $\mathrm{K}_{\mathrm{per}}$.

To determine whether the model could account for the experimental pattern of clones, virtual clones (circular regions) were introduced into the models at 0 DAI . The resultant virtual clone shapes (Fig. 4F,G) are broadly similar to the experimental clones (Fig. 4Ai,Bi): they are anisotropic in shape, elongated parallel to the proximodistal axis and are slightly wider in the model for Capsella compared with Arabidopsis. In addition, the growth rates and anisotropy of clones in the model are similar to those of experimental clones (Table S2). Thus, a proximodistal polarity field combined with a set of growth rules that are similar between the species can explain both gynoecium forms during the early phase and early part of the middle phase.

## Middle phase

The middle phase is characterised by a reduced growth rate in length compared with the early phase (Table 2). During the middle phase, Capsella produces a rounded gynoecium with a flattened crosssection and Arabidopsis produces a longer and cylindrically shaped gynoecium. To capture the growth patterns that generate this divergence of shape, clones were induced at 2.5-3 DAI and imaged 6 days later when the gynoecia reached $\sim 1 \mathrm{~mm}$ in length (Fig. 5A,B). At this stage, distinct regions and tissue types become evident at the fruit surface in both species. As with other members of the Brassicaceae family, Arabidopsis and Capsella fruits develop lateral valves that are attached to a medial replum and the structure is topped with a style and stigmatic tissue (Fig. 2) (Roeder and Yanofsky, 2006). To simplify the analysis, we considered clones induced in the style, replum and valve tissues individually.

Clones induced in the style of both species are elongated along the proximodistal axis (Fig. 5Ai,Bi). This is captured by calculating the average L/W ratio of the clones induced in the style in Capsella as $8.4( \pm 0.04$ s.d., $N=2)$ and $3.1( \pm 0.2, N=5)$ in Arabidopsis (Table S3). This anisotropy is correlated with two to three rounds of cell division along the major axis and no cell division along the minor axis.

Similar to the clones in the style, clones induced in the replum in both species exhibit clear elongation along the proximodistal axis


Fig. 4. Gynoecium clonal analysis and modelling of early phase and beginning of middle phase. (Ai) Sector map with shapes and positions of clones induced at 0 DAI and imaged 4 days after induction in Capsella gynoecia. Clones were imaged from dissected gynoecia and warped onto an average gynoecium shape using a different colour for each gynoecium.
(Aii) Image of a Capsella gynoecium epidermal clone (highlighted by a blue box in Ai ). ( Bi ) Sector map with clones induced at 0 DAI and imaged 4 days after induction in Arabidopsis gynoecia. (Bii) Image of an Arabidopsis gynoecium epidermal clone (highlighted by a red box in Bi). (C) Canvas at 0 DAI for both Capsella and Arabidopsis models. The polarity field (arrows)
depends on the production of a factor POL in the PROXORG region and degradation of POL everywhere at a constant rate.
(D) Distribution of factors STYLE and BASE on the canvas at 0 DAI. (E) Growth regulatory network for both Capsella and Arabidopsis models. The basic rates of $\mathrm{K}_{\mathrm{par}}$ and $\mathrm{K}_{\mathrm{per}}$ differ in each model. BASE and STYLE are active during 3-4 DAI.
(F) Capsella model outcome at 4 DAI showing virtual clone shapes and patterns. (G) Arabidopsis model outcome at 4 DAI showing virtual clone shapes and patterns. (H) $\mathrm{K}_{\text {par }}$ and $\mathrm{K}_{\text {per }}$ (colour key represents specified growth rates, $\% / \mathrm{h}$ ) with polarity field (arrows) plotted on Capsella (left) and Arabidopsis (right) models at 4 DAI. Scale bars: $10 \mu \mathrm{~m}$ in Aii,Bii; $50 \mu \mathrm{~m}$ in C,D; $100 \mu \mathrm{~m}$ in $\mathrm{Ai}, \mathrm{Bi}, \mathrm{F}-\mathrm{H}$.
(Fig. 5Aii,Bii). The average $\mathrm{L} / \mathrm{W}$ ratio of the clones induced in the replum is $2.8( \pm 1.0, N=21)$ for Capsella and $5.7( \pm 2.0, N=5)$ for Arabidopsis (Table S3). The anisotropic shape of the clones is correlated with higher cell division rates along the major axis of the clones (two to three rounds) compared with the minor axis (zero or one round). Overall, during the middle phase in both Capsella and Arabidopsis the growth in the style and the replum is anisotropic, with a higher growth rate along the proximodistal axis.

Unlike clones in the style and the replum, clones induced in the valves show a divergent pattern of growth during the middle phase in Capsella and Arabidopsis. In Capsella, these valve clones are uniform in size and mostly isotropic in shape (Fig. 5Ai,iii). In

Table 2. Growth rates of clones (\%/h) during early and middle stages of fruit development

|  |  | Middle phase (2.5-8.5 DAI in <br> Capsella, 3-9 DAI in <br> Arabidopsis) |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Plant | Early and middle (0-4 DAI) | Style | Replum | Valves |
| Capsella |  |  |  |  |
| $\mathrm{K}_{\text {max }}$ | $2.0(3)$ | 1.9 | 0.8 | $1.0(1)$ |
| $\mathrm{K}_{\text {min }}$ | $0.4(1.1)$ | 0.2 | 0.2 | $1.0(1.1)$ |
| Arabidopsis |  | 1.3 | 1.3 | $1.1(1.3)$ |
| $\mathrm{K}_{\text {max }}$ | $2.3(2.2)$ | 0.5 | 0.6 | $0.4(0.6)$ |
| $\mathrm{K}_{\text {min }}$ | $0.1(0.6)$ |  |  |  |

Numbers in parentheses indicate growth in length and width taken from Table 1.

Arabidopsis, valve clones are also uniform in size but elongated along the proximodistal axis of the gynoecium (Fig. 5Bi,iii). The average L/W ratios of the clones are $1.0( \pm 0.4, N=22)$ in Capsella and $3.0( \pm 0.9, N=83)$ in Arabidopsis (Table S3). This is correlated with differences in cell division patterns, as in Capsella there are one to two rounds of cell division along both axes (Fig. 5Aiii), whereas in Arabidopsis there are two to three rounds of cell division along the proximodistal axis and one round of cell division along the mediolateral axis (Fig. 5Biii). The anisotropic shape of the clones is also correlated with differences in cell expansion, as valve cells are no longer isodiametric but wider in Capsella (Fig. 5Aiii) and longer in Arabidopsis (Fig. 5Biii).

To determine how growth rates vary between regions during the middle phase, the growth rates of clones in the style, replum and valve regions were calculated (Table 2). For Capsella, $\mathrm{K}_{\max }$ is similar for valves and replum but higher in the style, whereas for Arabidopsis $\mathrm{K}_{\max }$ is highest in the replum (Table 2). By contrast, $\mathrm{K}_{\text {min }}$ in Capsella (along the circumferential axis) is lower in the replum and style than in the valves (Table 2), whereas $\mathrm{K}_{\text {min }}$ in Arabidopsis is similar across all three tissues. The growth rates in the valves of both species match the whole-organ L/W growth rates (Table 2).

When calculating the growth rates using the major and minor axes of the clones in valves of Capsella, the orientations of the clones did not always align parallel to the proximodistal axis of the gynoecium. Instead, the clones in the valves diverge away from the base and converge back towards the style (Fig. S1A). By contrast, in


Fig. 5. Gynoecium clonal analysis and modelling of the middle phase. (Ai) Sector map with clones induced at 2.5 DAI and imaged 6 days after induction in Capsella gynoecium. (Aii,Aiii) Images of Capsella gynoecium epidermal clones in replum (green box in Ai) and valve (blue box in Ai), respectively. (Bi) Sector map with shapes and positions of clones induced at 3 DAI and imaged 6 days after induction in Arabidopsis gynoecium. (Bii,Biii) Images of Arabidopsis epidermal clones in replum (red box in Bi ) and valve (orange box in Bi ), respectively. (C) Canvas at 0 DAI for both Arabidopsis and Capsella models showing the distribution of factors REP and MIDVALVE. (D) Growth regulatory network for both Capsella and Arabidopsis models covering early and middle phase. All factors except for EPHASE are specific to the middle phase. The basic rates of $K_{p a r}$ and $K_{\text {per }}$ differ in each model. (E) Capsella model outcome at 8.5 DAI showing virtual clone shapes and patterns. (F) Arabidopsis model outcome at 9 DAI showing virtual clone shapes and patterns. (G) Specified $\mathrm{K}_{\text {par }}$ and $\mathrm{K}_{\text {per }}$ (colours) with polarity field mapped onto Capsella canvas at 8.5 DAI (i) and Arabidopsis canvas at 9 DAI (ii). (H) Cross-sections of models with $\mathrm{K}_{\text {per }}$ inhibited only in style and base (i) and with $\mathrm{K}_{\mathrm{per}}$ inhibited in style, base, replum and midvalve as well as promotion of $\mathrm{K}_{\mathrm{par}}$ in midvalve (ii). Coloured chart represents resultant growth rates (\%/h). Scale bars: $10 \mu \mathrm{~m}$ in Aii,iii,Bii,iii; $50 \mu \mathrm{~m}$ in $\mathrm{C} ; 100 \mu \mathrm{~m}$ in $\mathrm{Ai}, \mathrm{Bi}, \mathrm{E}-\mathrm{H}$.

Arabidopsis valves the major axes of the clones align with the proximodistal axis of the gynoecium (Fig. 5Bi). Thus, clone patterns in the valves of Capsella show uniform isotropic growth with a divergent then convergent pattern, whereas for Arabidopsis they show uniform anisotropic growth parallel to the proximodistal axis.

Models of the middle phase need to account for the oblate spheroid shape of Capsella and the cylindrical shape of Arabidopsis gynoecium by 8-9 DAI. They must account for the proximodistal anisotropic clone patterns in the style and the replum in both species, and for the valve clones, which are wider with a divergent and convergent pattern in Capsella, as opposed to the narrow, parallel clone patterns in Arabidopsis.

These gynoecium shapes and clone patterns cannot be accounted for by continuing with the simple growth interactions established in
the early phase (0-2 DAI, Fig. S2). To account for the clone patterns and growth rates during the middle phase we inactivated general promotion of Kpar (EPHASE is switched off). In addition to STYLE and BASE, we introduced a factor, REP, into the model. REP is expressed in a central band and inhibits $\mathrm{K}_{\text {per }}$ (Fig. 5C,D). This interaction was proposed to account for clones in the replum being highly anisotropic along the proximodistal axis (Fig. 5Aii, Bii). The canvas was grown to 8.5 DAI for Capsella and 9 DAI for Arabidopsis. The longitudinal views of the modelling outputs broadly match the observed gynoecium sizes and shapes at a similar stage (Fig. 5E,F). In addition, the virtual clones in the style and replum regions resemble the anisotropic shape of the observed clones in these regions. The growth rates and anisotropy of the virtual clones are similar to those observed in the middle phase
(Table S3). In both models, the shape tapers at the base and style because of inhibition of $\mathrm{K}_{\text {per }}$ in these regions, although this is more extreme for Capsella. This differential growth creates a conflict that results in deformation of the polarity field so that it diverges from the base and converges towards the style, accounting for the virtual clones in the valve showing a similar pattern (Fig. 5Ai,E,Gi, Fig. S2). Virtual clones in the Arabidopsis model also run parallel to the polarity, which is parallel to the proximodistal axis of the model, matching the observed clones (Fig. 5Bi,F,Gii). Therefore, to account for the gynoecium shape changes and observed clone patterns during the middle phase it is sufficient to reduce the rate of $\mathrm{K}_{\text {per }}$ in the style, base and replum regions, while continuing with higher value of $\mathrm{K}_{\mathrm{per}}$ in Capsella compared with Arabidopsis established during the early phase.

These regional growth interactions can account for the observed clone patterns and many of the gynoecium shape features by the end of the middle phase. However, a major difference between the model and experimental observations is evident from cross-sections of Capsella gynoecia, which reveal a flattened oval that contrasts with the rounded shape obtained with the model (Fig. 2F, Fig. 5Hi). This reflects the gynoecium having an oblate spheroid rather than a spherical shape. Given the oblate spheroid shape of the valve, the distance from the style to the base is greater when following the
middle of the valve than when following the replum (Fig. S3). We therefore hypothesised that enhanced growth along the midvalve might be needed to account for this shape. To test this idea, we introduced a factor, MIDVALVE, into the Capsella model. MIDVALVE is active in a thin band down the middle of the valves (Fig. 5C). This observation was included in the model such that MIDVALVE promotes $\mathrm{K}_{\text {par }}$ giving rise to narrower sectors close to the midvalve (Fig. 5E). To stop the midvalve from becoming a wide region, $\mathrm{K}_{\mathrm{per}}$ was inhibited by MIDVALVE. Higher $K_{p a r}$ in the midvalve creates a conflict with the rest of the valve that tends to flatten the shape. The resultant cross-sectional shape of the Capsella model at 11.5 DAI broadly matches the flattened oval shape of the gynoecium at this stage (Fig. 5Hii).
Taken together, this analysis shows that the observed shape changes and clone patterns during the middle phase can be accounted for using regional factors in the midvalve, style and replum to alter local specified growth rates parallel or perpendicular to an initial proximodistal polarity.

## Late phase

The late phase is characterised by a transformation in Capsella from an oblate spheroid to a heart-shaped fruit. In Arabidopsis, no major change in shape is observed during the late phase. However, in both


Fig. 6. Clonal analysis and modelling the late phase. (A-C) Sector map of Capsella fruit with clones induced at (A) 3.5 DAI and imaged 6 days after induction, (B) 5.5 DAl and imaged 6 days after induction and (C) 6 DAl and imaged 8 days after induction. Orange area in $A$ and $B$ indicates a region near the base that is enriched for clones that are elongated along the proximodistal axis. (D,E) Sector maps of Arabidopsis fruit with clones induced at (D) 3 DAI and (E) 5.5 DAI and imaged 8 days after induction. (F) Specified $\mathrm{K}_{\text {par }}$ and $\mathrm{K}_{\mathrm{per}}$ (colours) with polarity field mapped onto Capsella canvas at 14 DAI (left) and Arabidopsis canvas at 13.5 DAI (right). (G) Growth regulatory network for the Capsella model. Factors GDIST and GPROX are only active in the late phase. GMIDVALVE plays a similar role to MIDVALVE in promoting Kpar in the late phase. (H,I) Capsella model outcome at 11.5 DAI. Virtual clones were induced at 3.5 DAI and 5.5 DAI , respectively. (J) Capsella model outcome at 14 DAI. Virtual clones were induced at 6 DAI. (K) Arabidopsis model outcome at 11 DAI. Virtual clones were induced at 3 DAI. (L) Arabidopsis model outcome at 13.5 DAI. Virtual clones were induced at 5.5 DAI. Coloured chart represents resultant growth rates (\%/h). Scale bars: $250 \mu \mathrm{~m}$ in A,B,D,H,I,K; $500 \mu \mathrm{~m}$ in C,E,F,J,L.
species overall growth rates in length and width are maintained at similar rates to the middle phase. To capture the growth patterns in Capsella during the late phase we induced clones at 3.5, 5.5 and 6 DAI (middle phase) and imaged 6 or 8 days after induction when the fruit length had reached 2 mm (Fig. 6A,B) and 4 mm (Fig. 6C), respectively. Similarly, in Arabidopsis we induced clones at 3 and 5.5 DAI and imaged 8 days after induction when the fruit length had reached 2 or 4 mm . The clones reflect growth at the end of the middle phase and the late phase and, at the time of induction, cell shapes could not be assumed to be isodiametric. For this reason, we did not analyse growth rates of clones during the late phase but focussed on clone shapes and distributions.

The clone patterns in the style and replum are similar throughout the middle and late phases, being elongated parallel to the longitudinal axis of the fruit in both species. However, clone patterns in the valves in Capsella differ between the middle and late phase. Whereas middle phase clones are nearly isotropic (Fig. 5Aiii), clones that grew during the late phase are highly anisotropic (Fig. 6B,C). The orientation of late phase clones varies across the valves in Capsella, with clones near the base being elongated more along the longitudinal axis but clones in the middle and distal regions being elongated more diagonally (most clearly observed in Fig. 6C). The clone patterns during the late phase therefore reveal a dynamic redistribution of anisotropic growth in the Capsella valves as the fruit undergoes the transition from oblate spheroid to a heart-shaped structure. By contrast, clone shapes and orientations in the valves of Arabidopsis remained similar between the middle and late phases (Fig. 5Biii, Fig. 6D,E).

A model of the late phase in Capsella needs to account for the shape change of the fruit and for the anisotropy and orientation of the clones. Continuing to grow the Capsella model to later stages with the same interactions as discussed above cannot account for these shape changes and clone patterns (Fig. S4). By contrast, when the Arabidopsis canvas continues to grow based on the interactions detailed in the middle phase, the resultant shapes and clone patterns resemble the observed fruit shapes and clone patterns of the same stages (Fig. 6D,E,K,L). Additional growth interactions are therefore needed in the Capsella model to generate the heart shape, whereas the Arabidopsis model can remain the same in the middle and late phases.

The clone patterns suggest that the additional growth interactions needed in the Capsella fruit during the late phase differ for the proximal and distal regions. To distinguish the proximal region and the distal region we introduced two factors, GPROX and GDIST, which are distributed in opposing linear gradients in the valves (Fig. S5). These factors only influence growth rates after 8 DAI. Clones near the base are elongated more along the longitudinal axis, suggesting more growth parallel to the polarity. Therefore, GPROX promotes $\mathrm{K}_{\text {par }}$ and inhibits $\mathrm{K}_{\text {per }}$ (Fig. 6G). In the distal region, the polarity field curves to converge on the style (Fig. 6F) and clones are elongated perpendicular to this polarity. We therefore postulated that GDIST inhibits $\mathrm{K}_{\text {par }}$ (Fig. 6G). These specified growth patterns create a conflict between the proximal region with relatively low $\mathrm{K}_{\text {per }}$ (and high $\mathrm{K}_{\mathrm{par}}$ ) and the distal region with relatively high $\mathrm{K}_{\mathrm{per}}$ (and low $\mathrm{K}_{\mathrm{par}}$ ). A factor GMIDVALVE was introduced as a linear gradient in the midvalve region (Fig. S5). Similar to MIDVALVE in the middle phase, GMIDVALVE promotes $\mathrm{K}_{\mathrm{par}}$ to maintain the flattened cross-sectional shape. In addition, a factor APEX was introduced that inhibits $\mathrm{K}_{\mathrm{par}}$ specifically in the midvalve at the apex of the shoulders to prevent isotropic growth in the shoulder region (Fig. S5). The resultant shapes generated by the model are similar to those of the Capsella fruit at equivalent stages (Fig. 6A-C,H-J).

Consistent with the experimental data, virtual clones are elongated longitudinally in the proximal region and diagonally in the distal and middle regions (Fig. 6H). As the canvas grows the virtual clones diverge increasingly towards the shoulders of the valve (Fig. 6J). Overall, the model postulates a change in specified growth rates after the middle phase, with $\mathrm{K}_{\mathrm{par}}$ promoted near the base and $\mathrm{K}_{\mathrm{per}}$ promoted in the distal regions, and this can account for the final fruit form and the clone patterns of the Capsella fruit during the late phase.

## FRUITFULL modifies growth during the late phase

In Capsella during the late phase, growth patterns change from the middle phase to transform an oblate spheroid into a heart-shaped fruit. The model predicts that genetic factors active after $\sim 8$ DAI will be important for generating the heart form. A gene known to be important at the later stages of fruit development in Arabidopsis is FRUITFULL (AtFUL), which encodes a member of the MADS-box transcription factor family (Gu et al., 1998). Mutations in AtFUL affect fruit growth, as valve cells fail to elongate after fertilisation (Ferrándiz et al., 2000). We identified a likely Capsella FUL orthologue ( $C r F U L$ ) in the genome sequence of the diploid C. rubella (Slotte et al., 2013). To test whether this gene has a similar effect on growth at late stages of Capsella fruit development as observed in Arabidopsis, we set out to identify ful mutant alleles in Capsella. We generated a mutant population in C. rubella by EMS mutagenesis. This population formed the basis for both a forward genetic screen and a targeted induced local lesions in genomes (TILLING) platform for reverse genetics. We screened mutant lines for fruit shape deformities and identified two mutants by forward genetic screening with a ful-like fruit phenotype. Mutations in the CrFUL gene in these two individuals were confirmed by sequencing and the effect of these mutations on the phenotype was confirmed by lack of complementation in F1 plants originating from crosses between the alleles (Fig. S6). These two alleles were named crful-1 and crful-2. A third allele, crful-3 was identified by TILLING and displayed a partial phenotype (Fig. S6). As in wild type, the gynoecium of crful-1 develops with an oblate spheroid shape before fertilisation, but with a longer style than wildtype gynoecia (Fig. 7A-D). After fertilisation, when the shoulders develop in wild-type fruits, the crful-1 fruits remain rounded (Fig. 7E,F). This rounded shape becomes slightly elongated but is retained at all subsequent stages of fruit development. This is consistent with the phenotype of ful mutant alleles in Arabidopsis, where gynoecia are largely indistinguishable from wild type until fertilisation (Fig. 7G-J), and the phenotype only becomes clearly evident during post-fertilisation fruit growth (Fig. 7K,L). These data show that CrFUL influences Capsella fruit shape mainly by modulating growth during the late phase.

To test which factors in the model could represent the activities of $F U L$, we compared the phenotype of a weak crful mutant allele (crful-3) at two developmental stages with a model in which the activity of GDIST is removed and overall growth ( $\mathrm{K}_{\text {par }}$ and $\mathrm{K}_{\text {per }}$ ) reduced (gdist mutant) (Fig. 8). Similar to the crful-1 allele, crful-3 gynoecium forms an oblate spheroid shape before fertilisation (Fig. 8A, Fig. S6), which is also observed at the end of the middle phase in $g d i s t$ (Fig. 8B). After fertilisation, the crful-3 fruit, like the wild type, develops a tapered base, but fails to generate the shoulders of the heart (Fig. 8C). The shape of gdist in late phase broadly matches that of the crful-3 fruit (Fig. 8D). However, one difference between crful-3 and gdist is the longer style of crful-3, which cannot be accounted for by simply removing GDIST from the model. This experiment suggests that GDIST and promotion of


Fig. 7. CrFUL is necessary for the late phase growth in Capsella and Arabidopsis. (A,C,E) Capsella wild-type gynoecium at 6, 8.5 and 11.5 DAI, respectively. (B,D,F) crful-1 at corresponding stages to wild type based on morphological features of the flower. Arrows indicate elongated style compared with wild type (D) or absence of the distal tips in crful-1 fruit (F). (G,I,K) Arabidopsis wild-type gynoecium at 6, 8.5 and 11.5 DAI, respectively. (H,J,L) atful-2 at corresponding stages to wild type. Scale bars: $100 \mu \mathrm{~m}$ in A,B,G,H; $250 \mu \mathrm{~m}$ in C-F,I-L.
overall growth represents at least some of the activities of $F U L$ during the late phase.

## Varying regional growth rates can explain much of the fruit shape diversity in the Brassicaceae

To test if this model of fruit development can account for other fruit shapes in the Brassicaceae we simplified the model to consider each subregion in turn. Consider the simplest growth pattern: isotropic growth of a cylinder with reduced $\mathrm{K}_{\text {per }}$ in the style and base gives rise to a spherical form (Fig. S2). Spherical fruits are present in the Brassicaceae, such as Neslia paniculata (Francis and Warwick, 2003), broadly matching the characteristics of this simple model.

Another common fruit shape observed in the Brassicaceae is the oblate spheroid form, similar to the gynoecium of Capsella before fertilisation. This spheroid form can be flattened either laterally, as for mature fruits from Lepidium campestre, or medially, as for Alyssum maritimum mature fruits. We have already shown that when $\mathrm{K}_{\mathrm{par}}$ is relatively high in the midvalve (in Capsella) the model is flattened laterally (Fig. 5Hii). We found that if we continued to
grow the model with MPHASE rather than introducing LPHASE, the model broadly accounts for the shape of laterally flattened spheroid fruit such as in Ledipium (Fig. 9A,B, Fig. S3). To test whether the replum could also be important for controlling fruit flatness, we promoted $K_{\text {par }}$ by REP. The resulting form is flattened medially (Fig. 9C), with the replum tissue around the rim of a flattened spheroid, similar to the mature fruit of Alyssum (Fig. 9D). Therefore, relative rates of $\mathrm{K}_{\mathrm{par}}$ in the midvalve or replum are important for controlling the flatness of the model to generate a spheroid shape. Overall, varying the model framework developed for Arabidopsis and Capsella fruits can account for at least basic fruit shape diversity in the Brassicaceae.

## DISCUSSION

The wide variation in organ morphology among otherwise closely related species makes the Brassicaceae family an excellent subject for comparing mechanisms underlying organ shape formation (Hay and Tsiantis, 2006). In this study, we combine experimental analysis of growth patterns with computational modelling to understand how


Fig. 8. CrFUL has overlapping activities with GDIST. (A,C) SEM images of crful-3 fruit before and after fertilisation. (B,D) Capsella model with GDIST removed (gdist) at corresponding stages. Models are shown for 8 DAI (B) and 14 DAI (D). Scale bars: $100 \mu \mathrm{~m}$ in B; $200 \mu \mathrm{~m}$ in A; $500 \mu \mathrm{~m}$ in C,D.
dynamic changes in specified growth patterns can lead to the different shapes of fruits from A. thaliana (cylindrical fruits) and C. rubella (heart-shaped fruits). Our analysis covers specific stages of fruit development, and both qualitative and quantitative observations from these experiments were used to evaluate models for growth at each stage and for both types of fruit.

The models presented here make six key predictions that can explain the difference in fruit shapes observed in the Brassicaceae and can be further tested experimentally. (1) A common proximodistal polarity field is established early and deforms with the tissue (Fig. S7). (2) Different patterns of anisotropic growth are oriented by the polarity field, with growth rates being specified as parallel $\left(\mathrm{K}_{\mathrm{par}}\right)$ or perpendicular ( $\mathrm{K}_{\mathrm{per}}$ ) to the local polarity. (3) Anisotropic specified growth patterns switch at different growth phases: early, middle and late. (4) The tapered shape is due to relatively low $\mathrm{K}_{\text {per }}$ in the base and style in both models, but is more extreme for Capsella. (5) Relative specified growth rates in the narrow vertical regions within the fruit (midvalve or replum) are important for creating tissue conflicts that generate the crosssectional shape. When $\mathrm{K}_{\mathrm{par}}$ is promoted in these regions the shape is flattened, generating an oblate spheroid shape. In the case where $\mathrm{K}_{\mathrm{par}}$ is promoted in the midvalve (like Capsella) the shape is flattened laterally (Fig. 5), whereas if $\mathrm{K}_{\mathrm{par}}$ is promoted in the replum the shape is flattened medially (Fig. 9). (6) The heart shape of Capsella is formed after the oblate spheroid has been established, where the polarity field in the valve converges towards the style and provides a potential angle for the shoulders of the fruit to form. Together with a redistribution of $\mathrm{K}_{\mathrm{par}}$ and $\mathrm{K}_{\text {per }}$ in a graded pattern in the valve, these conflicts can generate a heart shape, as observed in Capsella.


Fig. 9. Changes to the model can explain the shape of fruits from other Brassicaceae species. (A,C) Models showing oblate spheroid-shaped fruits obtained via promotion of $\mathrm{K}_{\text {par }}$ in the midvalve (A) and replum (C) regions. View is facing the replum. Value of $\mathrm{K}_{\text {par }}$ is indicated by the colour key. (B,D) SEM images of mature fruit from Lepidium campestre ( B ) and Alyssum maritimum (D). The view in $B$ is facing the replum, while that in $D$ is facing the midvalve. Replum (r), valves (v), style (s) and base (b) are indicated. Scale bars: $500 \mu \mathrm{~m}$.

In this model of Capsella, the divergent/convergent pattern of growth is explained by a proximodistal polarity field that deforms with the growing tissue (Fig. S7). This type of polarity organisation is similar to a model of Arabidopsis leaf development in which a proximodistal polarity field deforms during growth leading to a divergent polarity field at the base and then convergent field at the tip (Kuchen et al., 2012). The same type of polarity organisation can also explain the parallel growth patterns of the Arabidopsis fruit. This common feature of polarity organisation between leaves and carpels might be a result of the evolutionary origin of the carpel from two fused leaves (Scutt et al., 2006).

A key question is how genes control the factors in the model. Several candidate genes may be involved in specifying the spatiotemporal pattern of factors in the models of Arabidopsis and Capsella. Some known genes have similar expression patterns and could carry out the roles of the hypothesised factors in the models. For example, genes encoding NGATHA and STYLISH transcription factors are expressed in the distal region from the earliest stages of gynoecium initiation (Kuusk et al., 2006; Trigueros et al., 2009; Alvarez et al., 2009). They act redundantly, and when all are knocked out the style does not develop. Similarly, expression of the replum identity factors REPLUMLESS, BREVIPEDICELLUS and WOX13 is tightly constrained to the replum (Roeder et al., 2003; Alonso-Cantabrana et al., 2007; Romera-Branchat et al., 2012). We are not aware of any genes that are specifically expressed or inhibited in the midvalve region of the Arabidopsis fruit. However, development of the main vein in this region sets it apart from the rest of the valve. Gradients of factors such as GPROX and GDIST exist in the Arabidopsis fruit. These include miRNA156 and members
of the SPL family, which - when misexpressed - can alter fruit shape (Xing et al., 2013). It is therefore possible that genes known to regulate fruit development control factors in the model.

The shape changes of the Capsella gynoecium and fruit are regulated in developmental time. First, there is a transition from early to middle phase, giving rise to the oblate spheroid shape. Second, a transition occurs upon fertilisation from middle to late phase, leading to formation of the heart shape. Time-varying growth patterns have also been proposed for the Arabidopsis leaf and petal, where basic patterns of growth are established early on but are then gradually modulated over time (Kuchen et al., 2012). Similarly, a model for the complex Antirrhinum flower postulates a switch in growth patterns during development (Green et al., 2010).

A candidate gene for modulating gynoecium growth in time is $F U L$, which has been shown to be essential for proper fruit development in several angiosperms (Gu et al., 1998; Pabon-Mora et al., 2012; Wang et al., 2014). AtFUL expression is restricted to the valves of the Arabidopsis fruit, where it promotes valve identity and expansion after fertilisation (Ferrándiz et al., 2000). In terms of the model presented here, $A t F U L$ may be needed for promotion of growth parallel to the polarity $\left(\mathrm{K}_{\mathrm{par}}\right)$ during the late phase in Arabidopsis. The CrFUL gene in Capsella also mainly affects growth in the late phase, as the crful- 1 mutant attains the oblate spheroid shape during middle phase but fails to form the heart shape after fertilisation. Interestingly, there is a strong resemblance between fruits from the crful- 1 mutant identified here and the C. bursa-pastoris 'heegeri' variant (Shull, 1914), suggesting that it might be the two CrFUL genes of the tetraploid C. bursa-pastoris that are mutated in 'heegeri'. CrFUL may be required to promote differential growth, leading to the heart shape. In agreement with this, the shape of crful-3 fruit broadly matches a model in which GDIST, which inhibits $\mathrm{K}_{\mathrm{par}}$ at the distal end, is removed and overall growth reduced. $\mathrm{K}_{\mathrm{per}}$ is reduced at the distal end (by removing GDIST). It is unclear whether the difference between $A t F U L$ and $C r F U L$ action reflects differences in these genes or the species context. For example, $A t F U L$ and $C r F U L$ might both act as general valve growth and identity factors and it is other factors, which differ between the species, that are responsible for controlling the growth pattern that leads to the different fruit shapes. Candidates for these factors could be identified through screening for additional fruit shape mutants in Capsella.

The Brassicaceae family contains a richness of species with divergent fruit shapes. Some species have almost spherical fruits, such as Neslia paniculata (Francis and Warwick, 2003), a close relative of Capsella. Others have rounded fruits that are flattened laterally, such as Lepidium campestre, or in a medial orientation, such as Alyssum maritimum (Bowman, 2006) (Fig. 9). Using the models generated in this study, we found that the switch between lateral and medial flatness can be controlled simply by promoting $\mathrm{K}_{\mathrm{par}}$ in the midvalve or replum regions, respectively (Fig. 9). This simple difference in growth patterns between the two types of fruit might explain the multiple incidents of evolutionary switches between medially and laterally flattened fruits in the Brassicaceae (Mummenhoff et al., 2005). As in Arabidopsis and Capsella, timing of regional anisotropic growth patterns might also be an important parameter in the coordination of fruit growth in other Brassicaceae members. In $A$. linifolium the gynoecium has a rounded crosssection before fertilisation and then becomes flattened medially during post-fertilisation growth. This might be achieved through promotion of $\mathrm{K}_{\mathrm{par}}$ in the replum during the late phase.

It is possible that constraints, such as crossing connections between fruit walls, also contribute to fruit shape. A limitation of the modelling software used here is that such internal cross-connections
are not modelled. However, even with this limitation, simple modulations of the model presented here can broadly account for the growth dynamics of Capsella and Arabidopsis and the variety of fruit shapes of other Brassicaceae species. Our model raises many further questions, including how regions such as the midvalve are defined and growth patterns established. Therefore, the model provides a simplified framework for fruit development that can be further tested experimentally to provide insight into the specific controls of growth phases and regional dynamics.

## MATERIALS AND METHODS

## Plant material and growth

Arabidopsis thaliana ecotype Col-0 and Capsella rubella Cr22.5 were used in all experiments. The atful- 2 mutant is in the Col-0 background. Plants were grown in glasshouse conditions at $\sim 22^{\circ} \mathrm{C}, 16 \mathrm{~h}$ photoperiod. Plants for clonal analysis and growth curve were grown in controlled environment rooms at $20^{\circ} \mathrm{C}$ (A. thaliana) or $22^{\circ} \mathrm{C}$ (C. rubella) in long-day conditions ( 8 h dark and 16 h light under fluorescent light at a photon fluence rate of $100 \mathrm{mmol} \mathrm{m}^{-2} \mathrm{~s}^{-1}$ ) and $80 \%$ humidity.
Alyssum maritimum fruits were a kind gift from J. M. Stacey and collected in her garden.
Arabidopsis and Capsella were transformed by floral dipping as described (Clough and Bent, 1998). Heat shocking of plant inflorescences was performed as described in the supplementary Materials and Methods.

## Growth curve

Capsella and Arabidopsis plants were grown on soil in a controlled environment room. The plants were standardised by selecting those at a similar stage. Whole inflorescences were collected and fixed for propidium iodide staining at 2 -day intervals at about the same time of day, starting from 19-32 days after sowing. This method was developed from a protocol for staging Arabidopsis flower buds (Sauret-Gueto et al., 2013). Further details are provided in the supplementary Materials and Methods.

## Clonal analysis

Transgenic C. rubella Cr22.5 lines expressing pBOB (Wachsman et al., 2011) or HS-Cre (Gallois et al., 2002) were prepared. Lines with single copies of CrHS-Cre and CrBOB were crossed. For details, see the supplementary Materials and Methods.

## Computational modelling

For details of each of the models see the supporting model description and Table S4 in the supplementary Materials and Methods. All modelling was carried out with GPT-framework, implemented in the MATLAB (MathWorks) toolbox GFtbox (Kennaway et al., 2011) (http://cmpdartsvr3. cmp.uea.ac.uk/wiki/BanghamLab/index.php/GFtbox).

## Optical projection tomography

Samples were collected in $100 \%$ ethanol and rehydrated $(80 \%, 60 \%, 40 \%$, $20 \%$ ethanol, twice in $\mathrm{H}_{2} \mathrm{O}$ for 30 min each at room temperature) before being embedded in $1 \%$ low melting point agarose as described (Sharpe et al., 2002). Mounted specimens were dehydrated overnight in $100 \%$ methanol and cleared for 24 h in a 1:2 mixture of benzyl alcohol and benzyl benzoate (Sigma-Aldrich). Specimens smaller than 1 cm in width were scanned with a prototype OPT device as described previously (Lee et al., 2006). Specimens $1-2 \mathrm{~cm}$ in width were scanned using a Bioptonics 3001 scanner.

To visualise the OPT scans in 3D the freely available software package VolViewer (http://cmpdartsvr3.cmp.uea.ac.uk/wiki/BanghamLab/ index.php/Software\#Viewing_and_measuring_volume_images:_VolViewer) was used.

## Scanning electron microscopy

Samples were fixed in FAA ( $50 \%$ ethanol, $5 \%$ acetic acid, $3.7 \%$ formaldehyde) for 24 h , washed in $50 \%$ ethanol, dehydrated in an ethanol series $(50 \%, 70 \%, 80 \%, 90 \%$, four times in $100 \%$ ethanol for 30 min each at room temperature), and critical point dried using a Leica EM CPD300. Gynoecia were dissected from dried samples and mounted on stubs for
coating in gold using an Agar Scientific high-resolution sputter coater and imaged using a Zeiss Supra 55VP FEG scanning electron microscope.

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## Competing interests

The authors declare no competing or financial interests.

## Author contributions

T.E., E.S.C. and L. $\varnothing$. conceived the experiments. T.E., Ł.Ł., N.S., F.J., L.M. and A.S. performed the experiments. T.E., Ł.Ł., N.S., F.J., L.M., A.S., R.K., P.S., M.L., E.S.C. and L.Ø. analysed the data. T.E., E.S.C. and L.Ø. wrote the manuscript and $Ł . Ł$., N.S., F.J., L.M., A.S. and M.L. commented on it. All authors read and approved the manuscript.

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## Data availability

Model files are accessible from the following website: http://cmpdartsvr3.cmp.uea. ac.uk/wiki/BanghamLab/index.php/Software; and can be downloaded using the link: http://cmpdartsvr1.cmp.uea.ac.uk/downloads/software/OpenSourceDownload_Dev_
Eldridge_2016/Fruit_Shape_Brassicaceae.zip.

## Supplementary information

Supplementary information available online at
http://dev.biologists.org/lookup/doi/10.1242/dev.135327.supplemental

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## SUPPLEMENTARY MATERIALS AND METHODS

## Clonal analysis

For clonal analysis the plants were grown in the same conditions as those used for the growth curve. Following heat shock treatment (see below), plants were returned to the growth room and left for 4,6 or 8 days before imaging. The gynoecia were imaged in water using a Leica DM6000 compound microscope, a Zeiss LSM 5 EXCITER Laser Scanning Confocal Microscope, or the Zeiss LSM 780 Laser Scanning Confocal microscope.

Clones of the Capsella and Arabidopsis fruit were analysed using Sector Analysis Toolbox implemented in MATLAB (http://www.uea.ac.uk/cmp/research/cmpbio/Sector AnalysisToolbox). The organ outline and individual clones were segmented manually in Image J software. For each fruit project, fruits were warped to a mean fruit shape by placing 50 points around the segmented fruit outlines, with five points following the replum and several reference points. For $300 \mu \mathrm{~m}$ there were four reference points, one on each corner of the rectangular shape. For gynoecia larger than $300 \mu \mathrm{~m}$ there were seven reference points with two at the base, two where the style met the valves, two on the corners of the style and one at the apex of the style in line with the replum. These placed points were subjected to Procrustes Alignment (Gower, 1975) and normalised for scale. For clones were warped to the corresponding mean shape using a Piecewise Linear Warp (Goshtasby, 1986). The area of clones was calculated from the outline in image J , and the length and width were measured using the line tool in Image J.

## Heat shocking plant inflorescences

Pots containing a single plant of either Arabidopsis or Capsella were covered in Clingfilm. A small cross-shaped hole was pierced through the Clingfilm and the young plant inflorescence ( $1-3 \mathrm{~cm}$ in height) was threaded through the hole. The inflorescences were heat-shocked by turning the whole plant upside down in a $37^{\circ} \mathrm{C}$ water bath for varying times between 30 s and 4 min .

## Gynoecium growth curves

Capsella plants were grown in a controlled environment room on soil. The plants were standardised by selecting those at a similar stage, for example the plants that had 4 leaves at the same time. Whole inflorescences were collected and fixed for PI staining at two day intervals at about the same time of day starting from 19 to 32 days after sowing. This method was developed from a protocol for staging Arabidopsis flower buds: whole inflorescences were PI stained and imaged using OPT. Arabidopsis inflorescences were collected and
imaged (Sauret-Gueto et al., 2013).
The timing of the first flower of the main inflorescence was given in exact time in hours after sowing (HAS). The timing for subsequent flowers on the same inflorescence was calculated using the plastochron (timing interval between initiation of successive flower primordia) and the flower position. The plastochron was calculated by counting the number of newly open flowers in a 24 h period on 10 inflorescences and averaged over several days. Under these conditions the plastochron of Capsella was 4.8 h . The position of the individual flowers is the order that the flowers were initiated; so that the first flower on the inflorescence (oldest) would be at position 1 , the second flower (second oldest) would be at position 2 . Since, the flower at position 2 is initiated one plastochron after the first flower ( 456 HAS ), the timing of the second flower would be $456 \mathrm{~h}+4.8 \mathrm{~h}=460.8 \mathrm{HAS}$.

The length and width along the mediolateral axis of gynoecia were measured using the measuring tool in Volviewer. For later stages, when inflorescences were too large for imaging by OPT, the individual fruits along the inflorescence were imaged using Leica M205C stereo microscope and measured in the Leica LAS V4 software. Gynoecium initiation, 0 days after initiation ( 0 DAI ) was assumed to be when the gynoecium is $\sim 40 \mu \mathrm{~m}$ in length which corresponds to 450 HAS.

## Supporting Model Description

## Basic Factors and Functions

Growth patterns are determined by the pattern of factors distributed over the tissue, termed the canvas (Kennaway et al. 2011). Factors have one value for each segment or vertex of the canvas and are denoted by capital letters in the text. In the equations, factors that are fixed to the canvas are denoted by i subscripted with the factor name, while those that propagate through the canvas are denoted by the bold letter s subscripted with the factor name. For instance, the mobile factor GPROX is described by $\mathbf{s}_{\text {gprox }}$ in the equations. It is assumed that factor levels do not dilute with growth.

Factors may promote growth rates through the linear function pro, defined as:

$$
\begin{equation*}
\operatorname{pro}\left(p_{f}, \mathbf{x}_{f}\right)=1+p_{f} \mathbf{x}_{f}, \tag{1.1}
\end{equation*}
$$

Where $\mathbf{x}_{f}$ is a factor, F , and $\mathbf{x}$ denotes $\mathbf{i}$ or $\mathbf{s} . p_{f}$ is a promotion coefficient for that factor.
Factors may inhibit growth through the function inh, denoted as:

$$
\begin{equation*}
\operatorname{Inh}\left(h_{f}, \mathbf{x}_{f}\right)=1 /\left(1+h_{f} \mathbf{x}_{f}\right), \tag{1.2}
\end{equation*}
$$

Where $h_{f}$ is a inhibition coefficient for that factor. Values of all coefficients are given in Table S4.

## Models

2D fruit models were specified using the growing polarised tissue framework as implemented in the MATLAB application GFtbox. Full details are available in Kennaway et al. 2011 and GFtbox can be downloaded from (https://www.uea.ac.uk/cmp/research/cmpbio/Gftbox). The pattern of deformation depends on growth-modulating factors, whose initial distribution is established during setup ( -1 DAI to 0 DAI). Factors have one value for each vertex and values between vertices are linearly interpolated across each finite element. In the models described here, the initial canvas is oriented with regard to the external xyz-coordinate system such that the canvas base is parallel to the $x y$-axis and the long axis is parallel to the $z$-axis. The initial gynoecium primordium canvas consists of 2,000 elements and is locally subdivided at 160h at the midvalve generating a mesh of 2960 elements. The initial canvas size is $40 \mu \mathrm{~m}$ length and $80 \mu \mathrm{~m} \times 60 \mu \mathrm{~m}$ width (value of $z=-20 \mu \mathrm{~m}$ at the base of the canvas). Each model has two interconnected networks: the Polarity Regulatory Network (PRN) specifies tissue polarity and hence specified orientations of growth, and the Growth rate Regulatory Network (KRN) determines how factors influence specified growth rates. In total, growth interactions are specified in three equations, one for PRN and two for KRN. These networks determine the specified polarity and growth fields across the canvas. Due to the connectedness of the canvas, this specified growth differs from the resultant growth by which the system is deformed. The time step of each model corresponds to 4 h of developmental time. Models take about 20 min to run on a $\operatorname{CORE}^{\mathrm{TM}} \mathrm{i} 7$ laptop for 84 steps.

## PRN

The models involve growth orientations being established by POLARISER (POL, Fig. S7) propagation from a +organiser, which is expressed at the canvas base in the PROXORG region. The identity factor, PROXORG is fixed at 1 at the base of the canvas (purple line Fig. $4 \mathrm{C})$ and 0 everywhere else. The value of POL is fixed at $1\left(b_{p o l}\right)$, where PROXORG is expressed. POL diffuses according to the equation:
$\partial \mathbf{s}_{p o l} \partial t=\mathrm{D}_{p o l} \nabla^{2} \mathbf{s}_{p o l}-\mu_{p o l} \mathbf{s}_{p o l}$,
where $\mathrm{D}_{\text {pol }}$ is the diffusion rate and $\mu_{\text {pol }}$ the decay rate of POL throughout the tissue. Parameter values are given in Table S4. POL distribution is allowed to establish during the setup phase for 6 time steps before the commencement of growth.
POL continues to propagate and the polarity field readjusts according to POL levels throughout growth. The polarity field deforms during growth because changes in tissue geometry affect the way POL becomes distributed.

## KRN

There is a basic specified growth rate parallel to the polarity gradient, $K_{p a r}\left(b_{K p a r}\right)$ and a basic specified growth rate perpendicular to the polarity gradient, $K_{p e r}\left(b_{K p e r}\right)$ (values in Table S4). The canvas also grows in thickness, $K_{k n o r}$, which is maintained at the same rate in all models.

## Phases

The timing of the phases was specified by growth factors $\mathbf{i}_{\text {EPHASE }}, \mathbf{i}_{\text {MPHASE }}$ and $\mathbf{i}_{\text {LPHASE }} . \mathbf{i}_{\text {EPHASE }}$ is expressed at 1 everywhere in the canvas $\geq 0 \mathrm{~h}<48 \mathrm{~h}$ and 0 after this, $\mathbf{i}_{\text {MPHASE }}$ is expressed at a level of 1 everywhere in the canvas at $\geq 48 \mathrm{~h}<208 \mathrm{~h}$ (Capsella) or 216h (Arabidopsis) and 0 before and after this and $\mathbf{i}_{\text {LPHASE }}$ is expressed at a level of 1 everywhere in the canvas at $\geq$ 208h (Capsella) or 216h (Arabidopsis) and 0 before this.

Model 1 - E Phase and early M Phase (Capsella and Arabidopsis models)
STYLE and BASE were set up as short gradients (Fig 4D) during the set up phase with a maximum value of 1 . During the set up phase the gradients established by propagating from a region of production and then the values were fixed at each vertex once the set up phase was finished. The interactions described in Fig. 4E which set the values for $K_{p a r}$ and $K_{p e r}$ can be captured mathematically in the following equations:

$$
\begin{aligned}
K_{\text {par }}= & b_{\text {Kpar }} \\
& . \operatorname{pro}\left(p_{E P H A S E}, \mathbf{i}_{\text {EPHASE }}\right) \\
& . \operatorname{inh}\left(h_{\text {BASE }}, \mathbf{i}_{\text {BASE. }} \mathbf{i}_{\text {MPHASE }}\right) \\
K_{\text {per }}= & b_{\text {Kper }} \\
& . \operatorname{inh}\left(h_{\text {STYLE }}, \mathbf{i}_{\text {STYLE. }} \mathbf{i}_{\text {MPHASE }}\right) \\
& . \operatorname{inh}\left(h_{\text {BASE }}, \mathbf{i}_{\text {BASE. }} . \mathbf{i}_{\text {MPHASE }}\right)
\end{aligned}
$$

$$
K_{k n o r}=0.01
$$

The basic value of $K_{\text {par }}$ is promoted by $\mathbf{i}_{\text {EPHASE }}$ and inhibited by $\mathbf{i}_{\text {BASE }}$ when $\mathbf{i}_{\text {MPHASE }}$ is present. The basic value of $K_{p e r}$ is inhibited by $\mathbf{i}_{\text {STYLE }}$ and $\mathbf{i}_{\text {BASE }}$ when $\mathbf{i}_{\text {MPHASE }}$ is present. The model was run for 24 time steps (4 DAI).

Model 2 - E and M phase (Capsella model)
Model 2 has the same set up as model 1 with the addition of MIDVALVE which is set up as a domain illustrated in Fig. 5C. The interactions described in Fig. 5D which set the values for $K_{p a r}$ and $K_{p e r}$ can be captured mathematically in the following equations:
$K_{p a r}=b_{\text {Kpar }}$
. $\operatorname{pro}\left(p_{\text {EPHASE }}, \mathbf{i}_{\text {EPHASE }}\right)$
. $\operatorname{inh}\left(h_{\text {BASE }}, \mathbf{i}_{\text {BASE }} . \mathbf{i}_{\text {MPHASE }}\right)$
.pro(pMIDVALVE, $\left.\mathbf{i}_{\text {MIDVALVE. }} \mathbf{i}_{\text {MPHASE }}\right)$

```
Kper = b \kper
    .inh(hSTYLE , i_\TyLE. imphase)
    .inh(h_hASE,
    .inh(h}\mp@subsup{h}{REP}{,},\mp@subsup{\mathbf{i}}{\mathrm{ REP. }}{
    .inh(h)
```

$$
K_{k n o r}=0.01
$$

The model was run for 51 time steps (8.5 DAI). During expression of MPHASE the basic value of $K_{\text {par }}$ is promoted by $\mathbf{i}_{\text {MIDVALVE }}$ and inhibited $\mathbf{i}_{\text {BASE }}$. The basic rate of $K_{\text {per }}$ is inhibited by $\mathbf{i}_{\text {BASE }}, \mathbf{i}_{\text {STYLE, }} \mathbf{i}_{\text {REP }}$ and $\mathbf{i}_{\text {MIDVALVE }}$ when MPHASE is expressed.

Model 3 - E, M and L phase (Capsella model)
GDIST, GPROX and GMIDVALVE were set up as linear gradients and APEX was set up in small patches in the proximal region of the midvalve (Fig. S4). These three factors have a maximum value of 1 and a minimum value of 0 . During the set up phase the gradients established through region of production (fixed at 1 ) and a region of removal (fixed at 0 ) and then the values were fixed at each vertex once the set up phase was finished. The interactions described in Fig. 6F which set the values for $K_{p a r}$ and $K_{p e r}$ can be captured mathematically in the following equations:

$$
\begin{aligned}
K_{\text {par }}= & b_{\text {Kpar }} \\
& . \operatorname{pro}\left(p_{\text {EPHASE }}, \mathbf{i}_{\text {EPHASE }}\right)
\end{aligned}
$$

```
    .inh(h hASE},\mp@subsup{\mathbf{i}}{\mathrm{ BASE. }}{}\mp@subsup{\mathbf{i}}{\mathrm{ MPHASE }}{}
.pro(pMIDVALVE, , imIDVALVE. i
.inh(h (hASE , i
.inh(hSTYLE , i
.pro(p}\mp@subsup{p}{\mathrm{ GMIDVALVE },}{,}\mp@subsup{\mathbf{i}}{\mathrm{ GMIDVALVE. i}}{\mathrm{ LPPASE }
```



```
.pro(pGPROX , i}\mp@subsup{\mathbf{i}}{\mathrm{ GPROX. }}{\mathrm{ i iPHASE }
```

```
Kper }=\mp@subsup{b}{\mathrm{ Kper }}{
    .inh(h_hASE,
```



```
    .inh( }\mp@subsup{h}{\mathrm{ REP }}{},\mp@subsup{\mathbf{i}}{\mathrm{ REP. }}{}\mp@subsup{\mathbf{i}}{\mathrm{ MPHASE }}{
    .inh(h)
    .inh(hBASE , i
    .inh(hSTYLE , isTYLE. i
```



```
    .inh(hMIDVALVE , i
    .inh(}\mp@subsup{h}{\mathrm{ GPROX }}{},\mp@subsup{\mathbf{i}}{\mathrm{ GPROX. }}{
```

$K_{k n o r}=0.01$
The model was run for 84 time steps ( 9 DAI ). During expression of LPHASE the basic value of $K_{\text {par }}$ is promoted by $\mathbf{i}_{\text {GMIDVALVE }}$ and $\mathbf{i}_{\text {GPROX }}$ and inhibited by $\mathbf{i}_{\text {BASE }}, \mathbf{i}_{\text {STYLE }}, \mathbf{i}_{\text {MIDVALVE }}$ and $\mathbf{i}_{\text {GDIST. }}$ The basic rate of $K_{\text {per }}$ is promoted by $\mathbf{i}_{G D I S T}$ and inhibited by $\mathbf{i}_{\text {BASE }}, \mathbf{i}_{\text {STYLE }}, \mathbf{i}_{\text {REP }}, \mathbf{i}_{\text {MIDVALVE }}$ and $\mathbf{i}_{\text {GPROX }}$ when LPHASE is expressed.

Model 4 - E, M and L phase (Arabidopsis model)
The interactions for the Arabidopsis model described in Fig. 5H and Fig. 6F, which set the values for $K_{p a r}$ and $K_{p e r}$ can be captured mathematically in the following equations:

$$
\begin{aligned}
K_{p a r}= & b_{\text {Kpar }} \\
& . \operatorname{pro}\left(p_{E P H A S E}, \mathbf{i}_{\text {EPHASE }}\right) \\
& . \operatorname{inh}\left(h_{\text {BASE }}, \mathbf{i}_{\text {BASE }} . \mathbf{i}_{\text {MPHASE }}\right) \\
& . \operatorname{inh}\left(h_{\text {BASE }}, \mathbf{i}_{\text {BASE. }} \mathbf{i}_{\text {LPHASE }}\right) \\
& . \operatorname{inh}\left(h_{\text {STYLE }}, \mathbf{i}_{\text {STYLE. }} \mathbf{i}_{\text {LPHASE }}\right)
\end{aligned}
$$

$$
\begin{aligned}
K_{\text {per }}= & b_{\text {Kper }} \\
& . \operatorname{inh}\left(h_{\text {BASE }}, \mathbf{i}_{\text {BASE. }} \mathbf{i}_{\text {MPHASE }}\right) \\
& . \operatorname{inh}\left(h_{S T Y L E}, \mathbf{i}_{\text {STYLE }} \mathbf{i}_{\text {MPHASE }}\right) \\
& . \operatorname{inh}\left(h_{\text {REP }}, \mathbf{i}_{\text {REP. }} \mathbf{i}_{\text {MPHASE }}\right) \\
& . \operatorname{inh}\left(h_{\text {BASE }}, \mathbf{i}_{\text {BASE. }} \mathbf{i}_{\text {LPHASE }}\right) \\
& . \operatorname{inh}\left(h_{\text {STYLE }}, \mathbf{i}_{\text {STYLE. }} \mathbf{i}_{\text {LPHASE }}\right) \\
& . \operatorname{inh}\left(h_{\text {REP }}, \mathbf{i}_{\text {REP. }} \mathbf{i}_{\text {LPHASE }}\right)
\end{aligned}
$$

$$
K_{k n o r}=0.01
$$

When MPHASE or LPHASE are expressed $K_{p a r}$ is inhibited by $\mathbf{i}_{B A S E}$ and $K_{p e r}$ is inhibited by $\mathbf{i}_{\text {BASE }}, \mathbf{i}_{\text {STYLE }}$ and $\mathbf{i}_{\text {REP }}$. The only difference in growth interactions for LPHASE is that $K_{p a r}$ is inhibited be $\mathbf{i}_{\text {STYLE }}$ when LPHASE is expressed. The model was run for 54 time steps (9 DAI) in Fig. 5 and for 81 time steps (13.5 DAI) in Fig. 6.

Model 5 - E, M and L phase (Spherical model)
The interactions for the Spherical model shown in Supp. Fig. 2 and Fig. 9, which set the values for $K_{p a r}$ and $K_{p e r}$ can be captured mathematically in the following equations:

$$
\begin{aligned}
K_{\text {par }}= & b_{\text {Kpar }} \\
& . \operatorname{pro}\left(p_{E P H A S E}, \mathbf{i}_{\text {EPHASE }}\right) \\
& . \operatorname{inh}\left(h_{\text {BASE }}, \mathbf{i}_{\text {BASE. }} \mathbf{i}_{\text {MPHASE }}\right) \\
& . \operatorname{inh}\left(h_{\text {BASE }}, \mathbf{i}_{\text {BASE. }} \mathbf{i}_{\text {LPHASE }}\right) \\
K_{\text {per }}= & b_{\text {Kper }} \\
& . \operatorname{inh}\left(h_{\text {BASE }}, \mathbf{i}_{\text {BASE. }} \mathbf{i}_{\text {MPHASE }}\right) \\
& . \operatorname{inh}\left(h_{S T Y L E}, \mathbf{i}_{\text {STYLE. }} \mathbf{i}_{\text {MPHASE }}\right) \\
& . \operatorname{inh}\left(h_{R E P}, \mathbf{i}_{\text {REP. }} \mathbf{i}_{\text {MPHASE }}\right) \\
& . \operatorname{inh}\left(h_{\text {BASE }}, \mathbf{i}_{\text {BASE. }} \mathbf{i}_{\text {LPHASE }}\right) \\
& . \operatorname{inh}\left(h_{S T Y L E}, \mathbf{i}_{\text {STYLE. }} \mathbf{i}_{\text {LPHASE }}\right) \\
& . \operatorname{inh}\left(h_{\text {REP }}, \mathbf{i}_{\text {REP. }} \mathbf{i}_{\text {LPHASE }}\right)
\end{aligned}
$$

$$
K_{k n o r}=0.01
$$

The model is run for 48 time steps (8 DAI) in Supp. Fig 2 and 84 time steps ( 14 DAI) in Fig. 9. When MPHASE and LPHASE are expressed the basic rate of $K_{p a r}$ is inhibited by $\mathbf{i}_{\text {BASE }}$ and the basic rate of $K_{p e r}$ is inhibited by $\mathbf{i}_{B A S E}, \mathbf{i}_{S T Y L E}$ and $\mathbf{i}_{\text {REP }}$.

Model 6 - E, M and L phase (Laterally flattened Spheroid model)
The interactions for the laterally flattened Spheroid model (like Capsella) shown in Fig. 9, which set the values for $K_{p a r}$ and $K_{p e r}$ can be captured mathematically in the following equations:

```
Kpar = b <par
    .pro(p}\mp@subsup{p}{\mathrm{ EPHASE }}{},\mp@subsup{\mathbf{i}}{\mathrm{ EPHASE }}{
    .inh(h}\mp@subsup{h}{\mathrm{ BASE }}{},\mp@subsup{\mathbf{i}}{\mathrm{ BASE. }}{}\mp@subsup{\mathbf{i}}{\mathrm{ MPHASE }}{}
    .pro(pMIDVALVE, i
    .inh(h (hASE , i
    .inh(hSTYLE , i
    .pro(pMIDVALVE , i
```

```
Kper }=\mp@subsup{b}{\mathrm{ Kper }}{
    .inh( }\mp@subsup{h}{\mathrm{ BASE }}{},\mp@subsup{\mathbf{i}}{\mathrm{ BASE. }}{}\mp@subsup{\mathbf{i}}{\mathrm{ MPHASE }}{}
    .inh(}\mp@subsup{h}{\mathrm{ STYLE }}{},\mp@subsup{\mathbf{i}}{\mathrm{ STYLE. }}{}\mp@subsup{\mathbf{i}}{\mathrm{ MPHASE }}{}
```



```
    .inh(hMIDVALVE,}\mp@subsup{\mathbf{i}}{\mathrm{ MIDVALVE. }}{\mathbf{i}
    .inh(hBASE , i
    .inh(hSTYLE , isTYLE. i
```



```
    .inh(}\mp@subsup{h}{\mathrm{ MIDVALVE , i}}{\mathbf{MIDVALVE. i}
```

When MPHASE and LPHASE are expressed the basic rate of $K_{\text {par }}$ is promoted by $\mathbf{i}_{\text {MIDVALVE }}$ and inhibited by $\mathbf{i}_{\text {BASE }}$ and the basic rate of $K_{\text {per }}$ is inhibited by $\mathbf{i}_{\text {BASE }}, \mathbf{i}_{\text {STYLE }}, \mathbf{i}_{\text {REP }}$ and $\mathbf{i}_{\text {MIDVALVE }}$. The model is run for 84 time steps ( 14 DAI ).

Model 7 - E, M and L phase (Medially flattened Spheroid model).
The interactions for the Spherical model shown in Fig. 9, which set the values for $K_{p a r}$ and $K_{p e r}$ can be captured mathematically in the following equations:
$K_{p a r}=b_{\text {Kpar }}$

```
    .pro(p}\mp@subsup{p}{\mathrm{ EPHASE }}{},\mp@subsup{\mathbf{i}}{\mathrm{ EPHASE }}{}
    .inh(hBASE ,}\mp@subsup{\mathbf{i}}{\mathrm{ BASE. }}{
    .inh(h (hASE , i
    .inh(hSTYLE , isTYLE. i
    .pro(p}\mp@subsup{p}{REP}{,},\mp@subsup{\mathbf{i}}{\mathrm{ REP. }}{}\mp@subsup{\mathbf{i}}{\mathrm{ LPHASE }}{
Kper }=\mp@subsup{b}{\mathrm{ Kper }}{
    .inh(hBASE},\mp@subsup{\mathbf{i}}{\mathrm{ BASE. }}{
    .inh(}\mp@subsup{h}{\mathrm{ STYLE }}{},\mp@subsup{\mathbf{i}}{\mathrm{ STYLE. }}{
```



```
    .inh(h)
```




```
    .inh( }\mp@subsup{h}{\mathrm{ REP }}{,},\mp@subsup{\mathbf{i}}{\mathrm{ REP. }}{}\mp@subsup{\mathbf{i}}{\mathrm{ LPHASE }}{
    .inh(hMIDVALVE, , imIDVALVE. i
```

When MPHASE and LPHASE are expressed the basic rate of $K_{p a r}$ is promoted by $\mathbf{i}_{R E P}$ and inhibited by $\mathbf{i}_{\text {BASE }}$ and the basic rate of $K_{p e r}$ is inhibited by $\mathbf{i}_{\text {BASE }}, \mathbf{i}_{\text {STYLE }}, \mathbf{i}_{\text {REP }}$ and $\mathbf{i}_{\text {MIDVALVE }}$. The model is run for 84 time steps ( 14 DAI ).

Model 8 - Same as Model 3 except that GDIST activity is removed and $\mathrm{K}_{\mathrm{par}}$ and $\mathrm{K}_{\mathrm{per}}$ are inhibited during the late phase.

## Diffusion

Details on how diffusion equations are solved can be found in Kennaway et al. (2011). The time steps were chosen to optimise the running time of the model, but the results are the same for smaller time steps. When building the model, the end of the set-up phase was chosen as when the signalling factors that diffused through the canvas had reached an equilibrium. For most factors at this step the diffusion was stopped and so the gradients were established before the growth steps began (e.g. GDIST, GPROX, GMIDVALVE). Fig. S7 depicts the distribution of polariser and the polarity field.

We do not use finite differences, but a finite element method which is capable of stably solving the transient diffusion problem even when $2 \mathrm{D} \mathrm{dt} / \mathrm{dx}^{2}$ greatly exceeds 1 . It also has the
advantage of not requiring any regularity in the arrangement of the vertices.
The actual values that arise in the simulations are $\mathrm{dt}=4, \mathrm{dx}=$ the typical diameter of a finite element $=$ between 1.6 and 6 in the initial state (however, these values increase during growth), and values of D ranging from 0.25 to 15 (all in consistent units). No instability is observed.

Note that the only morphogen that continues to diffuse throughout the simulation is the polariser, with a D of 5 , giving $2 \mathrm{D} \mathrm{dt/dx}{ }^{2}$ of 1.1 to 16 . Test examples with much larger values of $2 \mathrm{D} \mathrm{dt} / \mathrm{dx}^{2}$ show no instability and converge over time to the steady state solution. The other diffusible morphogens only diffuse during the setup phase that establishes the initial conditions of the growth simulation. Their distribution during the final steps of the setup phase indicates that they are near steady state by the beginning of the growth phase.

## Models Parameter List

The models parameter list is presented in Supp. Table 1.

## SUPPLEMENTARY FIGURES



Figure S1. Gynoecium clonal analysis in the middle phase.
(A,B) Sector maps of Capsella gynoecium with clones imaged at 8.5 DAI induced at 0 (A) and 2.5 (B). In A, the clones in the valves diverge away from the base and converge back towards the style.

Scale bar, $200 \mu \mathrm{~m}$.


Figure S2. Models with continued growth interactions established in the early phase models.
(A) Capsella model outcome at 8.5 DAI showing virtual clone shapes and patterns and (B) cross-section shape is rounded. (C) Arabidopsis model outcome at 9 DAI showing virtual clone shapes and patterns and (D) cross-section shape is rounded.
Scale bar $200 \mu \mathrm{~m}$. STYLE, yellow, BASE, pink.


Figure S3. Length of midvalve and replum in Capsella gynoecia 8.5 DAI.
(A) Cross section view. White dotted line shows the cross section shape of the gynoecium.
(B) Line drawn down the middle of the valve is longer than a line drawn down the replum. Scale bar, $500 \mu \mathrm{~m}$


Figure S4. Capsella model with continued growth interactions established in the middle phase.
(A) Capsella model outcome at 14 DAI showing virtual clone shapes and patterns and (B) cross-section shape. Scale bar $500 \mu \mathrm{~m}$. STYLE, yellow, REP, pink, MIDVALVE, green.


Figure S5. Distribution of Late Phase factors on Capsella model at 8 DAI.
(A) GDIST. (B) GPROX. (C) GMIDVALVE. (D) APEX.

Scale bars $200 \mu \mathrm{~m}$.


Figure S6. Allelism test of crful alleles.
(A) Whole-mount photo of mature fruit from C. rubella wild type (left), crful-3 (centre) and crful-1 (right). Scale bar, 1 mm .
(B) SEM of fruits from crful-1 and crful-3 alleles before (upper) and after (lower) fertilisation. Scale bars, $100 \mu \mathrm{~m}$ (upper), $200 \mu \mathrm{~m}$ (lower).
(C) SEM of fruits from F1 plants originating from the indicated crosses before (upper) and after (lower) fertilisation. See Fig. 2D,G for comparison to wild type at these stages. Scale bars, $100 \mu \mathrm{~m}$ (upper), $200 \mu \mathrm{~m}$ (lower).


Figure S7. Distribution of POLARISER and orientation of Polarity field on models.
(A) Capsella (B) Arabidopsis. Scale bars $100 \mu \mathrm{~m}$.

Supplementary Table S1. Cell lengths ${ }^{1}$ and widths ${ }^{2}(\mu \mathrm{~m})$ in gynoecium of Capsella and Arabidopsis.


[^1]Supplementary Table S2. Growth rates of clones (\%/hr) during 0-4 DAI of fruit development and model.

|  | Average | Standard deviation | L/W ratio | Standard deviation | No. clones measured |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Capsella |  |  |  |  |  |
| $\mathrm{K}_{\text {max }}$ | 2.0 | 0.40 | 5.4 | 3.0 | 8 |
| $\mathrm{K}_{\text {min }}$ | 0.4 | 0.30 |  |  |  |
| Model |  |  |  |  |  |
| $\mathbf{K}_{\text {max }}$ | 1.9 | 0.26 | 2.7 | 0.7 | 50 |
| $\mathrm{K}_{\text {min }}$ | 0.9 | 0.16 |  |  |  |
| Arabidopsis |  |  |  |  |  |
| $\mathrm{K}_{\text {max }}$ | 2.2 | 0.44 | 7.7 | 3.8 | 7 |
| $\mathrm{K}_{\text {min }}$ | 0.2 | 0.26 |  |  |  |
| Model |  |  |  |  |  |
| $\mathrm{K}_{\text {max }}$ | 1.7 | 0.44 | 3.1 | 0.8 | 50 |
| $\mathrm{K}_{\text {min }}$ | 0.6 | 0.13 |  |  |  |

Supplementary Table S3. Growth rates of clones (\%/hr) during middle phase* of fruit development and model.

|  |  | Mean | Standard deviation | $\begin{aligned} & \mathrm{L} / \mathrm{W} \\ & \text { ratio } \end{aligned}$ | Standard deviation | No. Clones Measured |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Capsella |  |  |  |  |  |  |
| Style | $\mathrm{K}_{\text {max }}$ | 1.8 | 0.06 | 8.4 | 0.04 | 2 |
|  | $\mathrm{K}_{\text {min }}$ | 0.3 | 0.03 |  |  |  |
| Model | $\mathrm{K}_{\text {max }}$ | 1.1 | 0.10 | 3.2 | 0.60 | 20 |
|  | $\mathrm{K}_{\text {min }}$ | 0.3 | 0.10 |  |  |  |
| Replum | $\mathrm{K}_{\text {max }}$ | 0.8 | 0.20 | 2.3 | 0.8 | 9 |
|  | $\mathrm{K}_{\text {min }}$ | 0.3 | 0.2 |  |  |  |
| Model | $\mathrm{K}_{\text {max }}$ | 1.1 | 0.20 | 2.8 | 1.0 | 21 |
|  | $\mathrm{K}_{\text {min }}$ | 0.4 | 0.30 |  |  |  |
| Valve | $\mathrm{K}_{\text {max }}$ | 1.0 | 0.27 | 1.0 | 0.4 | 22 |
|  | $\mathrm{K}_{\text {min }}$ | 1.0 | 0.16 |  |  |  |
| Model | $\mathrm{K}_{\text {max }}$ | 1.1 | 0.20 | 1.8 | 0.8 | 81 |
|  | $\mathbf{K}_{\text {min }}$ | 0.8 | 0.40 |  |  |  |
| Arabidopsis |  |  |  |  |  |  |
| Style | $\mathrm{K}_{\text {max }}$ | 1.3 | 0.08 | 3.1 | 0.2 | 5 |
|  | $\mathrm{K}_{\text {min }}$ | 0.5 | 0.06 |  |  |  |
| Model | $\mathrm{K}_{\text {m }}$ | 1.3 | 0.10 | 3.7 | 0.6 | 14 |
|  | $\mathrm{K}_{\text {min }}$ | 0.3 | 0.10 |  |  |  |
| Replum | $\mathrm{K}_{\text {max }}$ | 1.8 | 0.27 | 5.7 | 2.0 | 5 |
|  | $\mathrm{K}_{\text {min }}$ | 0.6 | 0.17 |  |  |  |
| Model | $\mathrm{K}_{\text {max }}$ | 1.1 | 0.35 | 3.9 | 1.5 | 22 |
|  | $\mathrm{K}_{\text {min }}$ | 0.2 | 0.12 |  |  |  |
| Valve |  |  |  | 3.0 | 0.9 | 10 |
|  | $\mathrm{K}_{\text {min }}$ | 0.4 | 0.16 |  |  |  |
| Model | $\mathrm{K}_{\text {max }}$ | 1.2 | 0.30 | 2.9 | 0.9 | 83 |
|  | $\mathrm{K}_{\text {min }}$ | 0.5 | 0.20 |  |  |  |

[^2]
## Supplementary Table S4. Model parameter list.

| Parameter | Description | Value |
| :---: | :---: | :---: |
| PRN |  |  |
| Polariser |  |  |
| $\boldsymbol{b}_{p o l}$ | $\mathbf{s}_{\text {POL }}$ production by $\mathbf{i}_{\text {PROXORG }}$ (maximum value) | 1 |
| $D_{\text {pol }}$ | $\mathbf{S}_{\text {POL }}$ diffusion constant | $0.005 \mathrm{~mm}^{2} \mathrm{~h}^{-1}$ |
| $\mu_{\text {pol }}$ | $\mathbf{S P O L}^{\text {decay rate }}$ | $0.0001 \mathrm{~h}^{-1}$ |
| KRN |  |  |
| Basic growth rates |  |  |
| $b_{\text {Kpar }}$ | Capsella, spherical, laterally flattened spheroid and medially flattened spheroid models | $1.2 \% h^{-1}$ |
| $b_{\text {Kper }}$ | Capsella, laterally flattened spheroid models | 1.2\% $h^{-1}$ |
| $b_{\text {Kpar }}$ | Arabidopsis model | 1.3\% ${ }^{-1}$ |
| $b_{\text {Kper }}$ | Arabidopsis model | $0.6 \% h^{-1}$ |
| $b_{\text {Kper }}$ | medially flattened spheroid model | $1.25 \% h^{-1}$ |
| Setting up gradients |  |  |
| $\boldsymbol{b}_{\text {BASE }}$ | $\mathbf{S}_{\text {STYLE }}$ production by $\mathbf{i}_{\text {STYLE }}$ (maximum value) | 1 |
| $\mathrm{D}_{\text {STVLE }}$ | $\mathbf{s}_{\text {STYLE }}$ diffusion rate | $0.25 \mu \mathrm{~m}^{2} \mathrm{~h}^{-1}$ |
| $\boldsymbol{b}_{\text {BASE }}$ | $\mathbf{s}_{\text {BASE }}$ production by $\mathbf{i}_{\text {BASE }}$ (maximum value) | 1 |
| $D_{\text {BASE }}$ | $\mathbf{s}_{\text {BASE }}$ diffusion rate | $0.25 \mu \mathrm{~m}^{2} \mathrm{~h}^{-1}$ |
| $\boldsymbol{b}_{\text {GPROX }}$ | $\mathbf{s}_{\text {GPROX }}$ production by $\mathbf{i}_{\text {GPROX }}$ (maximum value) | 1 |
| $D_{\text {GPROX }}$ | $\mathbf{s}_{\text {GPROX }}$ diffusion rate | $5 \mu \mathrm{~m}^{2} h^{-1}$ |
| $\boldsymbol{b}_{\text {GOIST }}$ | $\mathbf{s}_{G D I S T}$ production by $\mathbf{i}_{\text {GDIST }}$ (maximum value) | 1 |
| $\mathrm{D}_{\text {GDIST }}$ | $\mathbf{s}_{\text {GDIST }}$ diffusion rate | $15 \mu \mathrm{~m}^{2} \mathrm{~h}^{-1}$ |
| $\boldsymbol{b}_{\text {GmidValve }}$ | $\mathbf{s}_{\text {GMIDVALVE }}$ production by $\mathbf{i}_{\text {GMIDVALVE }}$ (maximum value) | 1 |
| D Gmidvalve | $\mathbf{s}_{\text {GMIDVALVE }}$ diffusion rate | $15 \mu \mathrm{~m}^{2} \mathrm{~h}^{-1}$ |
| Promotion coefficients |  |  |
| $p_{\text {EPHASE }}$ | growth promotion by $\mathbf{i}_{\text {EPHASE }}$ | 2 |
| $p_{\text {midalve }}$ | growth promotion by $\mathbf{i}_{\text {MIVVALVE }}$ | 0.2 |
| $p_{\text {gmidvalve }}$ | growth promotion by $\mathbf{i}_{\text {GMIDVALVE }}$ | 0.5 |
| $p_{\text {GPROX }}$ | growth promotion by $\mathbf{i}_{\text {GPROX }}$ | 2 |
| $p_{\text {GOIST }}$ | growth promotion by $\mathbf{i}_{\text {GDIST }}$ | 0.2 |
| $p_{\text {REP }}$ | growth promotion by $\mathbf{i}_{\text {REP }}$ | 0.15 |
| Inhibition coefficients |  |  |
| $h_{\text {STYLE }}$ | growth inhibition by $\mathbf{i}_{\text {STYLE }}$ | 3 |
| $h_{\text {BASE }}$ | $K_{\text {par }}$ inhibition by $\mathrm{i}_{\text {BASE }}$ | 5 (mphase), 100 (lphase) |
| $h_{\text {BASE }}$ | $K_{\text {per }}$ inhibition by $\mathbf{i}_{\text {BASE }}$ | 1 |
| $h_{\text {REP }}$ | growth inhibition by $\mathbf{i}_{\text {REP }}$ | 5 |
| $h_{\text {MIDVALVE }}$ | growth inhibition by $\mathbf{i}_{\text {MIDVaLVE }}$ | 1 |
| $h_{\text {GPROX }}$ | growth inhibition by $\mathbf{i}_{\text {GPROX }}$ | 2 |
| $h_{\text {GOIST }}$ | growth inhibition by $\mathbf{i}_{\text {GIIST }}$ | 4 |
| $h_{\text {APEX }}$ | growth inhibition by $\mathrm{i}_{\text {APEX }}$ | 100 |


[^0]:    ${ }^{1}$ John Innes Centre, Norwich Research Park, Norwich NR4 7UH, UK. ${ }^{2}$ Biosciences Eastern and Central Africa - International Livestock Research Institute (BecA-ILRI) Hub, P.O. Box 30709, Nairobi 00100, Kenya. ${ }^{3}$ Institute for Biochemistry and Biology, University of Potsdam, Potsdam 14476, Germany. ${ }^{4}$ University of East Anglia, Norwich NR4 7TJ, UK.
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[^1]:    ${ }^{1}$ Cell length was measures parallel to the long axis of the gynoecium
    ${ }^{2}$ Cell width was measure parallel to the circumferential axis of the gynoecium

[^2]:    * Capsella middle phase clones were induced at 2.5 and imaged at 8.5 DAI and Arabidopsis clones were induced at 3 DAI and imaged at 9 DAI.

